

# $\Sigma^+$ hyperon in Gamov states

poor men hypernucleus

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Experiments : FINUDA, AMADEUS

Description of Gamov states : S.W.

Related physics: open

# $\Sigma$ Hyperon momenta from $K^-$ - ${}^6\text{Li}$

FINUDA

Low momentum peak, only with  $\Sigma^+$

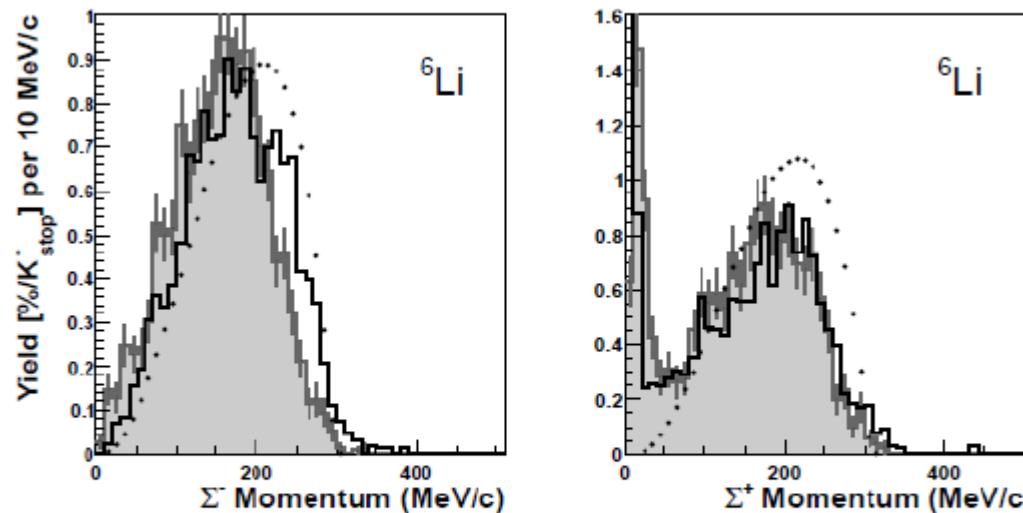


Fig. 5. Momentum distributions of sigmas from the  ${}^6\text{Li}(K^-_{stop}, \pi^\pm \Sigma^\mp) A'$  reactions. The grey-filled histograms are the measured distributions. The distributions of Monte-Carlo generated sigmas are depicted by full dots, and with open diagrams are represented the M-C generated sigmas being reconstructed by FINUDA.

# The origin of lower peak ?

- \* Initial FINUDA interpretation - stopping in the target
- \*\* AMADEUS - thin targets  
Trapping of  $\Sigma^+$  into Gamov states

# Low Peak versus Main Peak

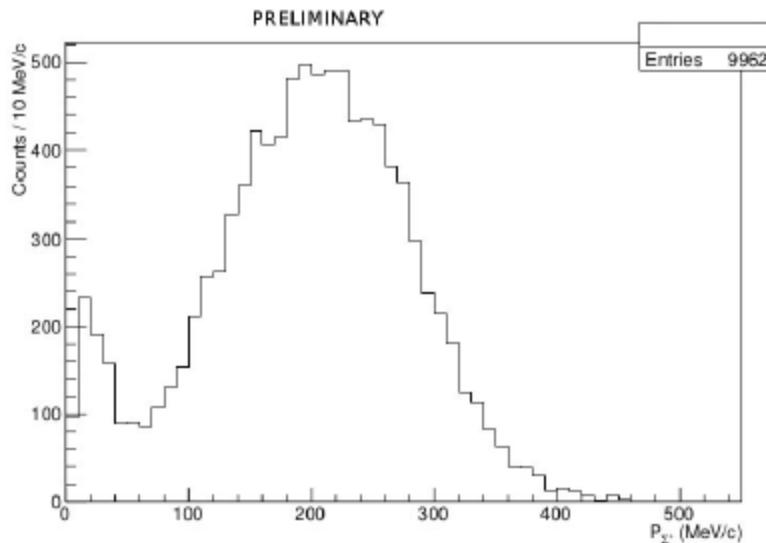
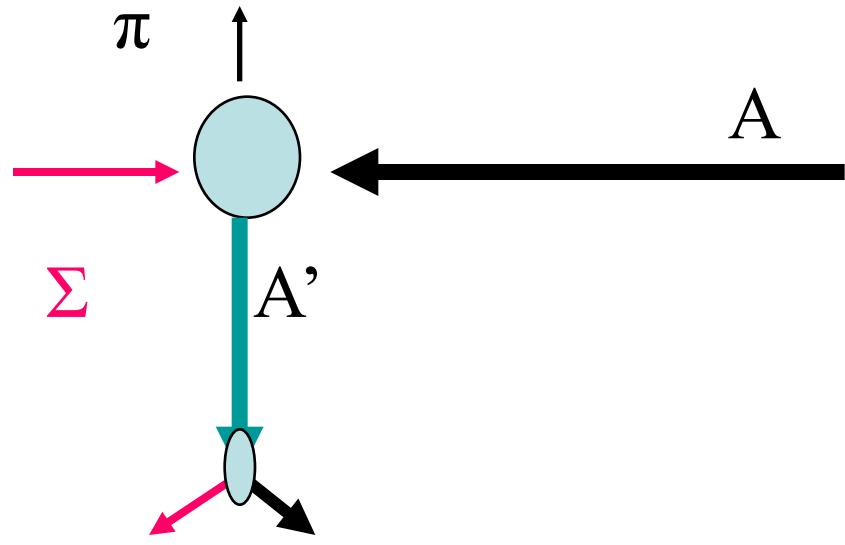


Figure 4.  $\Sigma^+$  momentum distribution, from  $K^-$  captures in  $^{12}C$  giving rise to  $\Sigma^+\pi^-$  formation

AMADEUS peaks seen in K- meson capture at rest and also in-flight

# Expectation

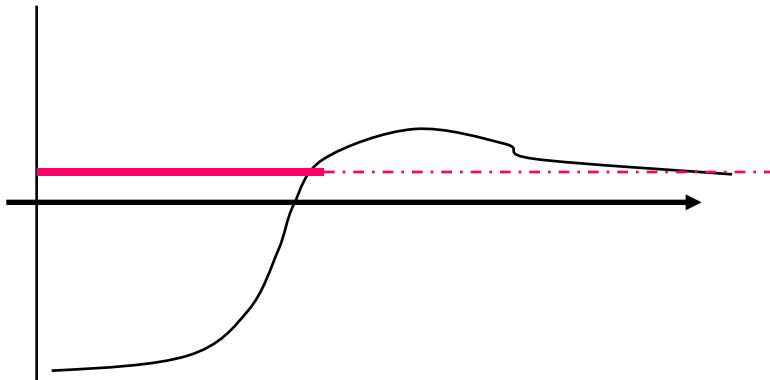
- K



$\Sigma^+ + A' =$  quasi bound large object decays with „zero” momentum, propagates large distance

# Gamov state

Nuclear +Coulomb potential



A quasi -discrete decaying state in the continuum  
– outgoing wave conditions

# Gamov states of $\Sigma^+$

In light nuclei - exist if  $\Sigma^+$  is almost bound

$$\Phi = \frac{R(r)}{r}$$

$$-\frac{1}{2M} \frac{dR}{d^2r} + (V_c + V_n)R = ER$$

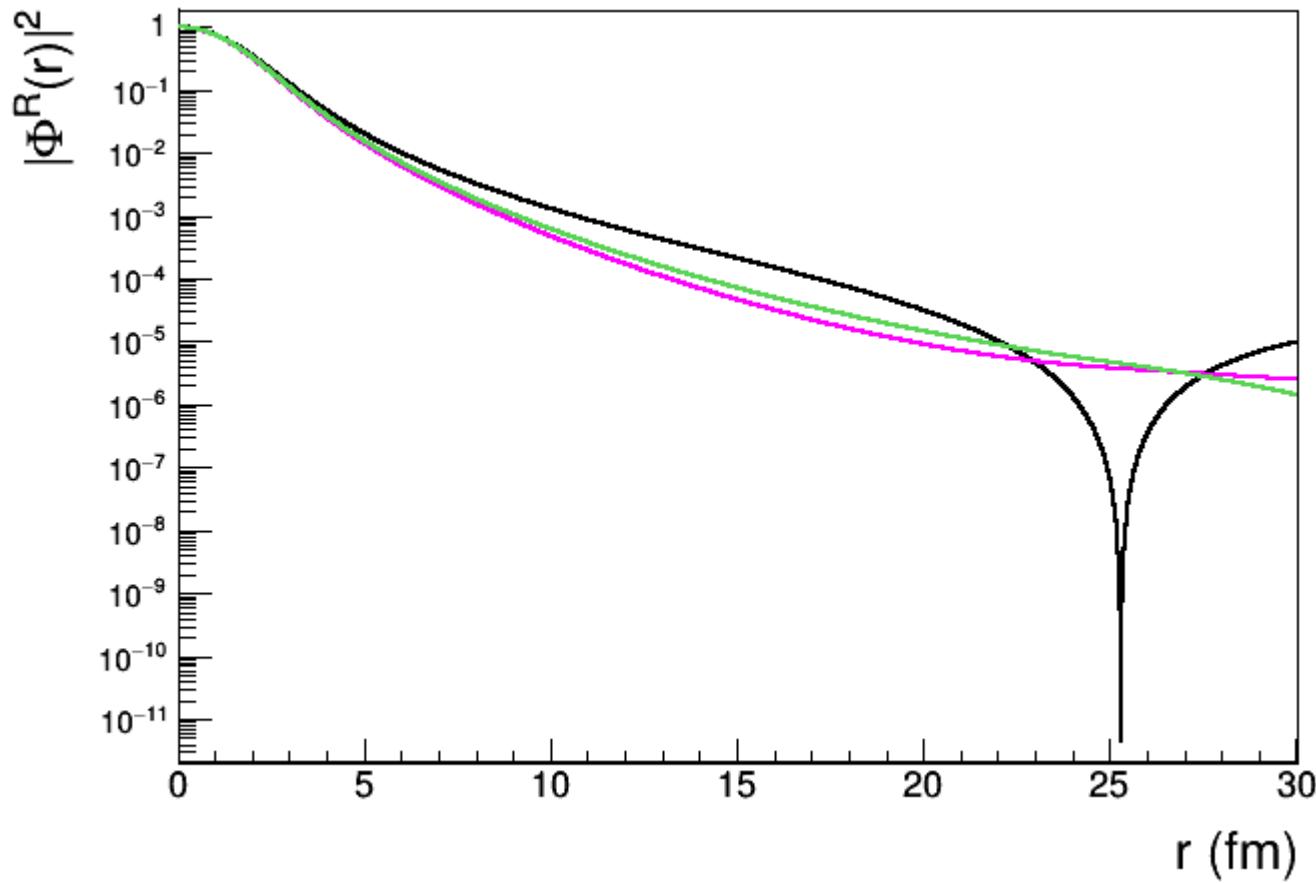
Solutions for real potential  $V_{\text{Coulomb}} + V_{\text{nuc}}$

# Densities in Gamov states, examples

C

B

He



# K- Capture in $^{12}\text{C}$

## Gamov states in $^{11}\text{B}$ :examples

$E$ [MeV]	$R_{\text{ms}}$ [fm]	$\Gamma$ [keV]
0.013	5.1	0.49
0.38	9.1	17

Limits  $\Sigma$  potential well depth to  $\pm 0.4$  MeV

Trapping time  $\sim 10^4 \cdot \Sigma$  formation time

# Technical description of Gamov states

# DESCRIPTION OF GAMOV STATE

TWO POTENTIALS

$$V_{\text{LONG}} = V^{\text{CULOMB}} + V^{\text{NUCLEAR}}$$

$iW_{\text{SHORT}}$ :  $\Sigma \rightarrow \Lambda$

GREEN'S FUNCTION FOR  $V_{\text{LONG}}$

$$G_L = \frac{\phi^R(\tau_L) \phi^+(\tau_S)}{W[\phi^R \phi^+]} \frac{1}{\tau_S - \tau_L}$$

↓      ↘      ↘  
REGULAR    OUTGOING    WRONSKI

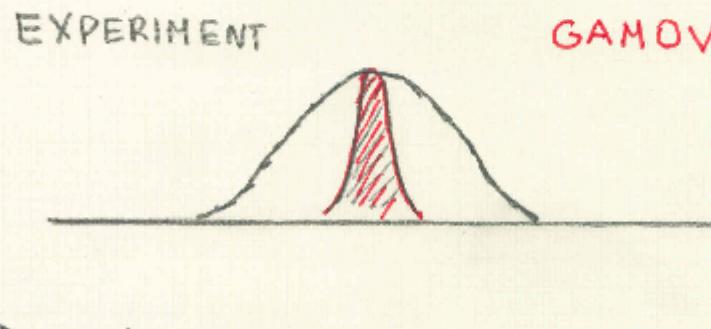
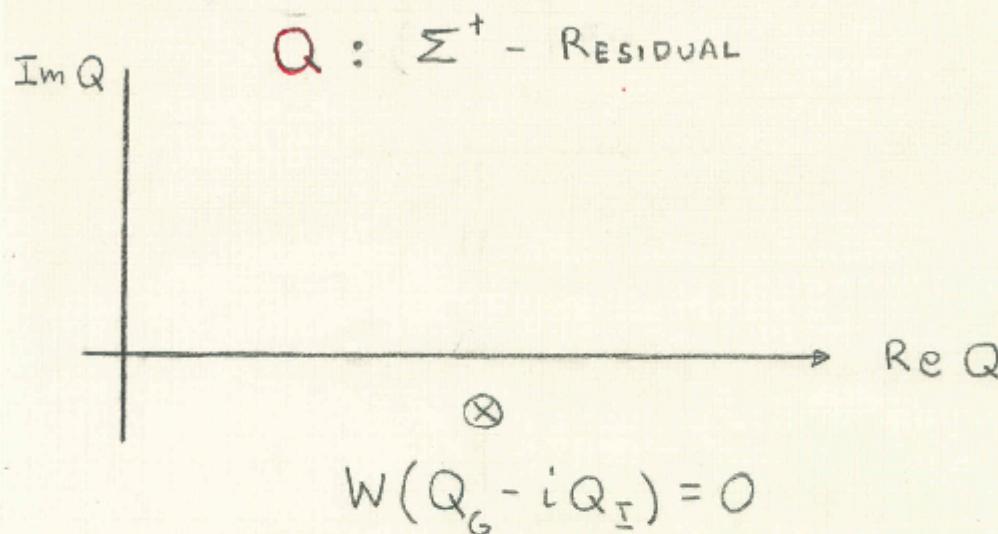
NEAR SINGULARITIES = GAMOV STATES

FULL

$$G = G_L + G_{\text{WG}} G_L$$



# COMPLEX MOMENTUM PLANE

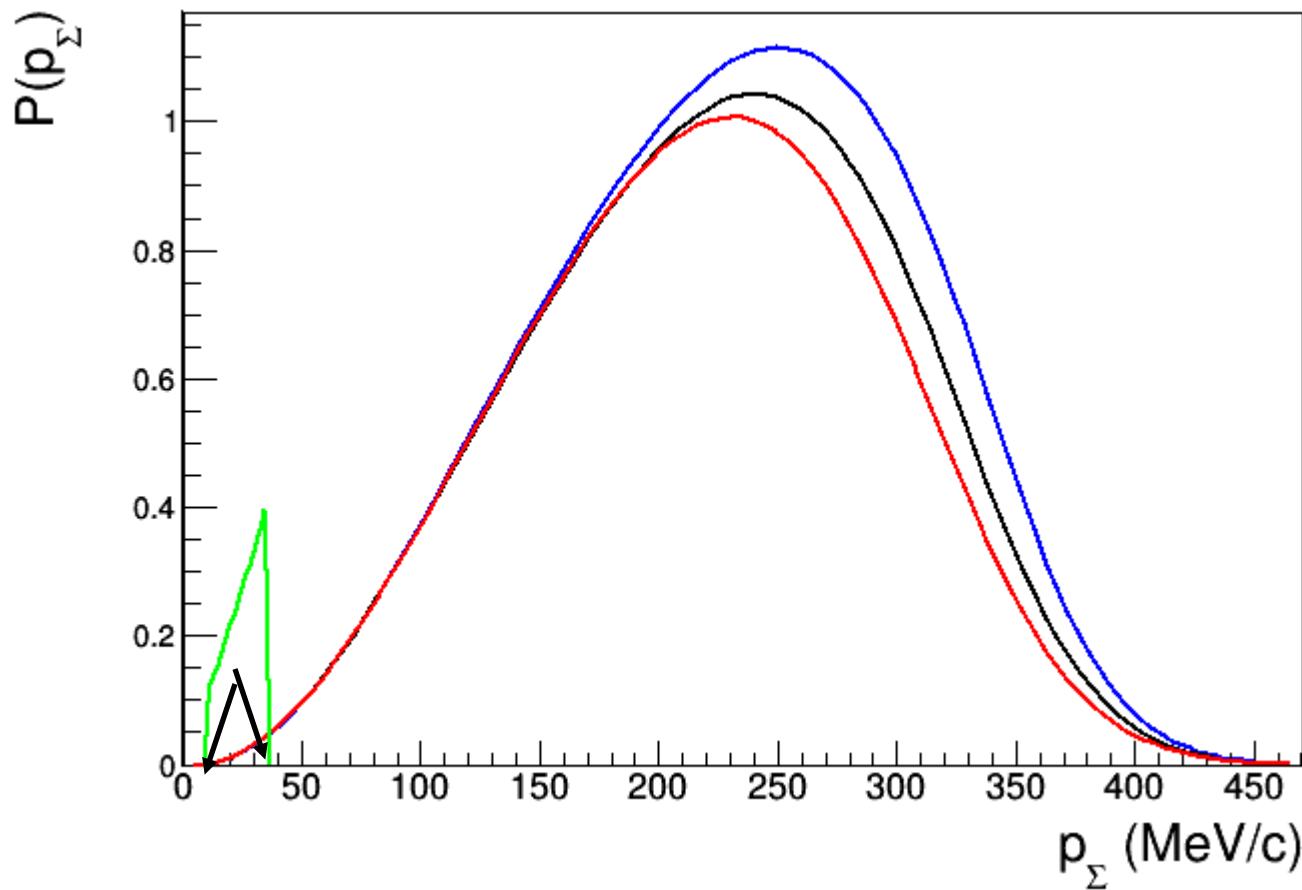


$$\vec{p}_\Sigma \sim \vec{Q}_G + \frac{m_\Sigma}{m_\Sigma + m_R} \vec{p}_\pi$$

# Hyperon momentum spectra

delayed

fast processes



# What is learned from Gamov peak

Energy level  $\rightarrow$  depth of  $\Sigma$  potential well

precisely  $2M \int dr r V(r) \approx \pi/2$

widths  $\rightarrow$  level

strengths  $\rightarrow$   $K, \Sigma$  absorption parameters

difficult to extract

# Extraction of nuclear parameters

The existence of the peak determines

If simple potential well : if  $V = V_o \rho(r)$

$^{12}\text{Carbon}$  ( $^{11}\text{B}$ )  $V_o \sim -18.6 \pm 0.4$  MeV

$^6\text{Lithium}$  ( $^5\text{He}$ )  $V_o \sim -26 \pm 0.5$  MeV

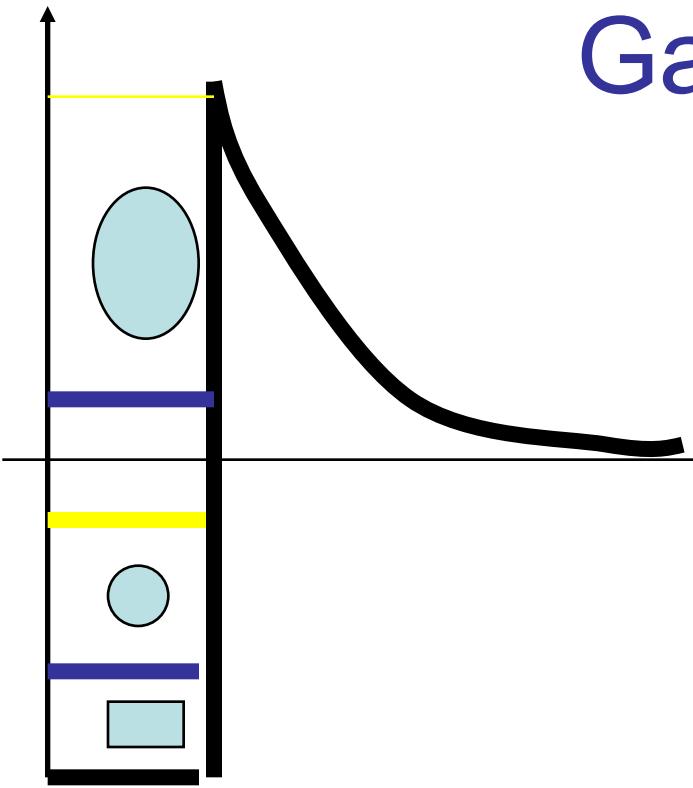
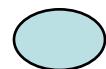
But potential is strongly nonlinear in  $\rho$

# Relation to $\Sigma$ Hypernuclei

# Hypernuclear region



Gamov region



# Optical potential for $\Sigma$

Scattering amplitudes : isospin 3/2, 1/2

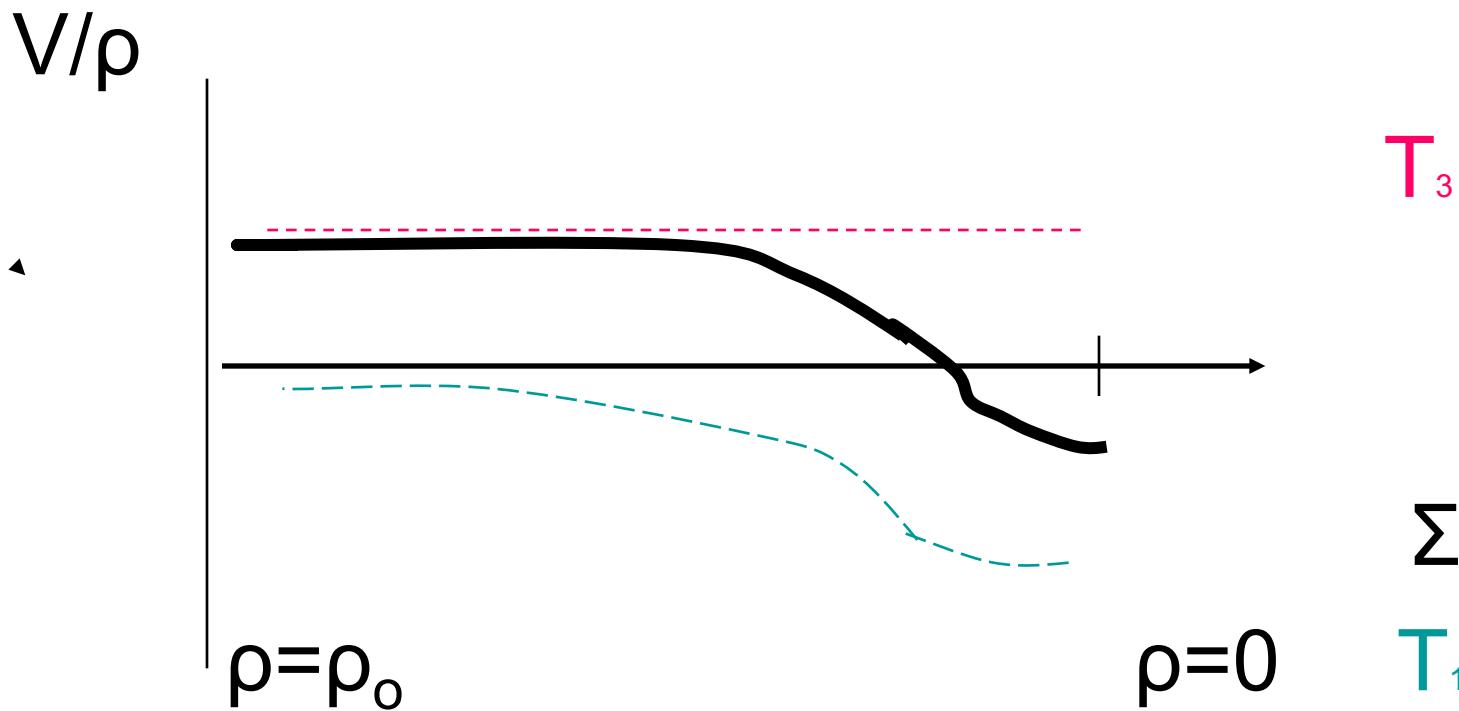
$$T(\Sigma^- p) = T(\Sigma^+ n) = \frac{1}{3}T_3 + \frac{2}{3}T_1$$

$$T(\Sigma^- n) = T(\Sigma^+ p) = T_3$$

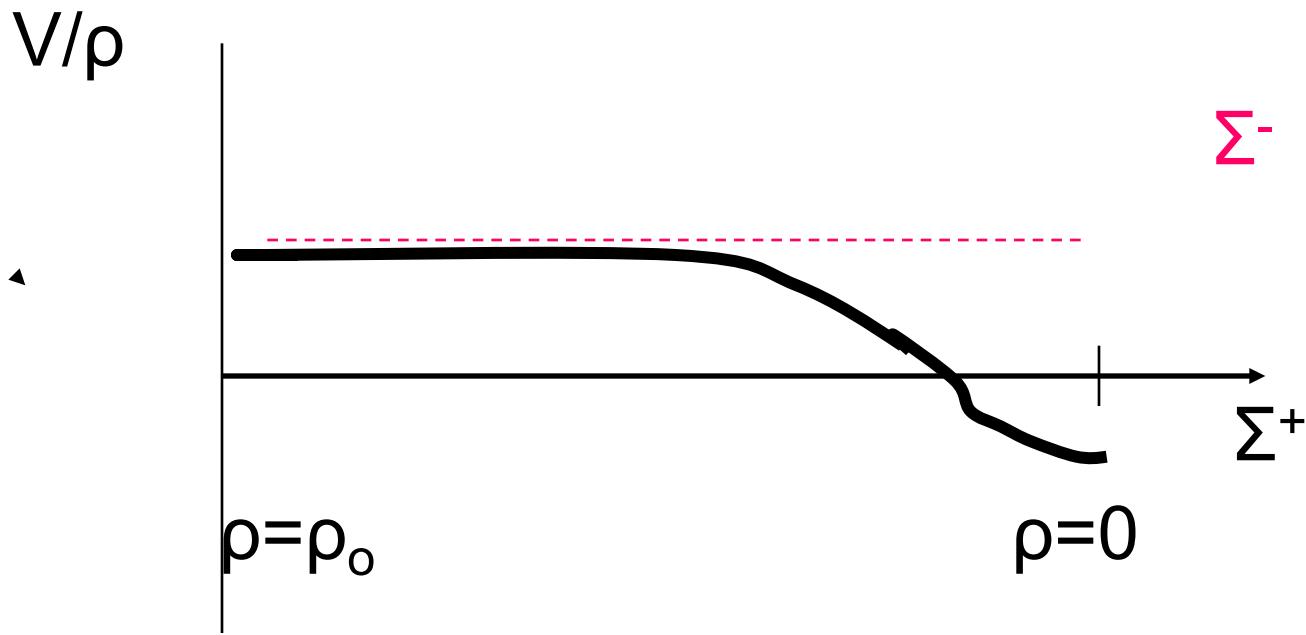
$T_1$  attractive ( virtual state, changes in nuclear matter )

$T_3$  repulsive

# Symmetric N=Z nuclei



# Hypothetical nuclei made of neutrons only



Fair chances for  $\Sigma^+$  Gamov states (or Hypernuclei) in neutron excess nuclei , but  $A > 16$  not tested

# outlook

Nuclei with strong neutron tails and  
small or medium  $Z$  may attract  $\Sigma^+$   
hyperons in Gamov  
( or hypernuclear ) states

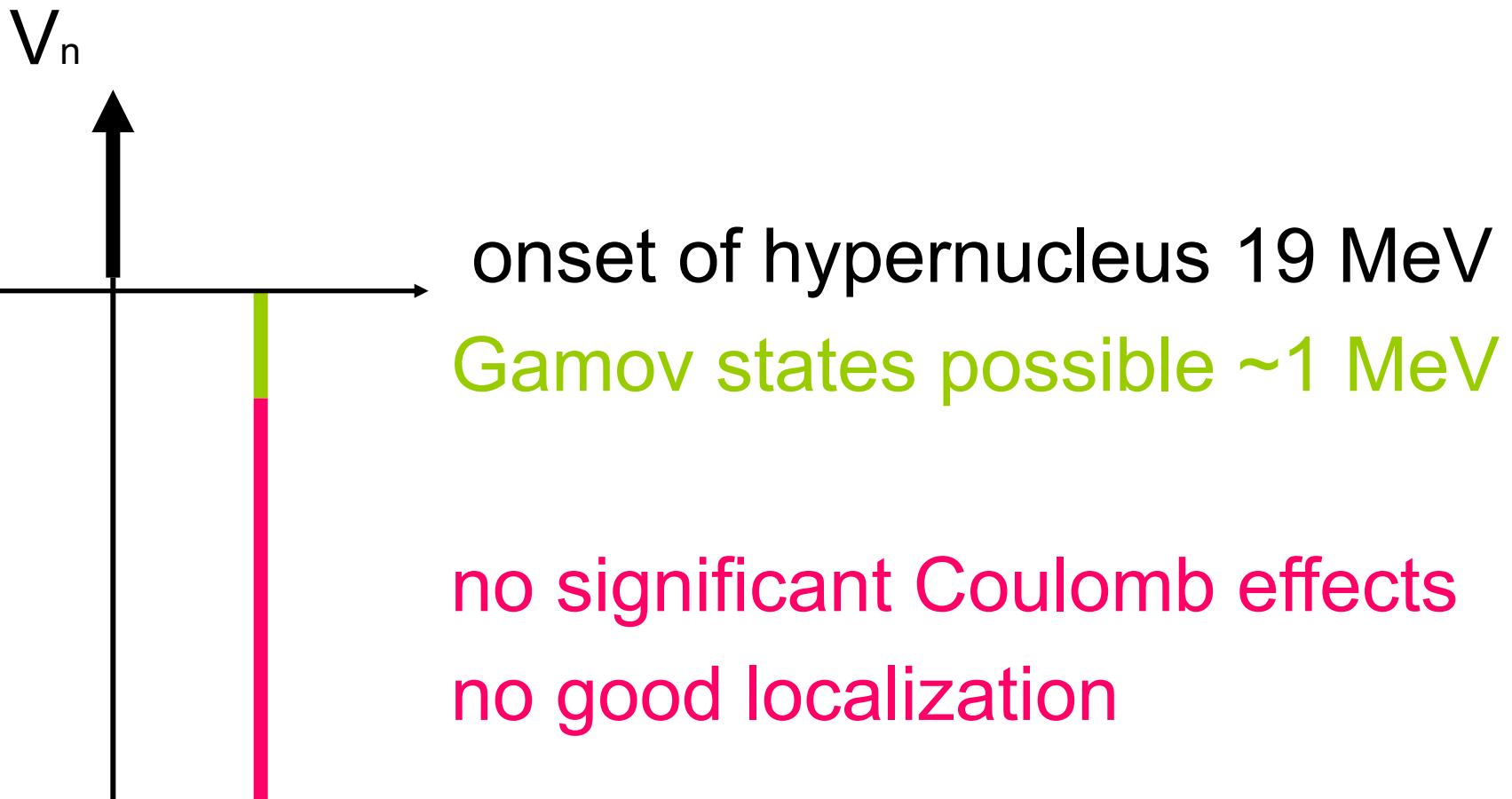
# Thank you

## References:

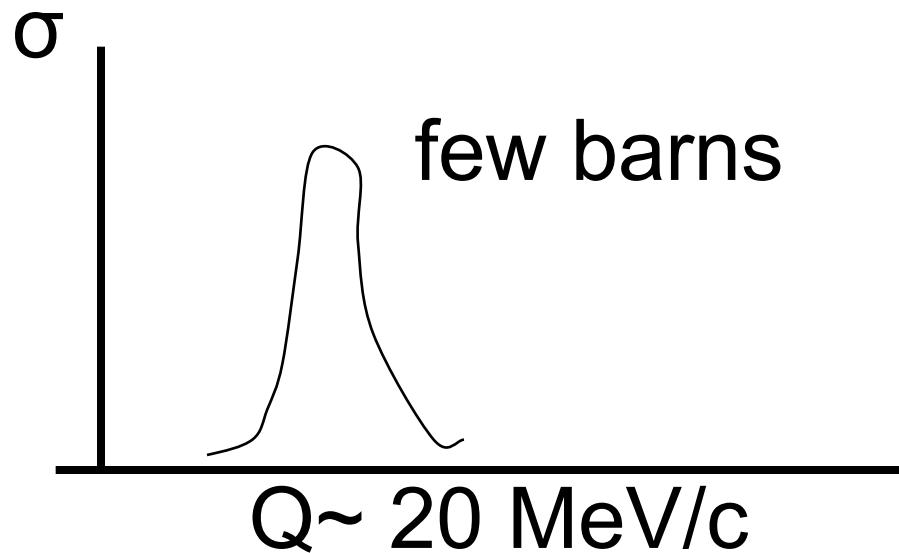
- |  |   |
|--|---|
| M. Agnello et al., Phys. Lett. B704 (2011) 474,      | FINUDA                                      |
| K. Piscicchia et al., EPJ Web Conf. 137 (2017) 09005 | AMADEUS –preliminary                        |
| T.Nagae et.al. Phys.Rev. Lett.80(1998)1605           | He- $\Sigma$ hypernucleus                   |
| S. Bart, et al., Phys. Rev. Lett. 83 (1999) 5238.    | no heavier $\Sigma$ (-) hypernuclei         |
| P.K. Saha, et al., Phys. Rev. C 70 (2004) 044613     | no $\Sigma$ (+) hypernuclei for A<16        |
| K. Piscicchia , S. W. Acta Phys Pol. 48( 2017)1869   | description of the $\Sigma$ (+) Gamov state |
| T.Harada et al. Phys. Lett. B 740 (2015) 312–316     | $\Sigma$ He P wave expected                 |

# Appendices

# Nuclear well depths in B

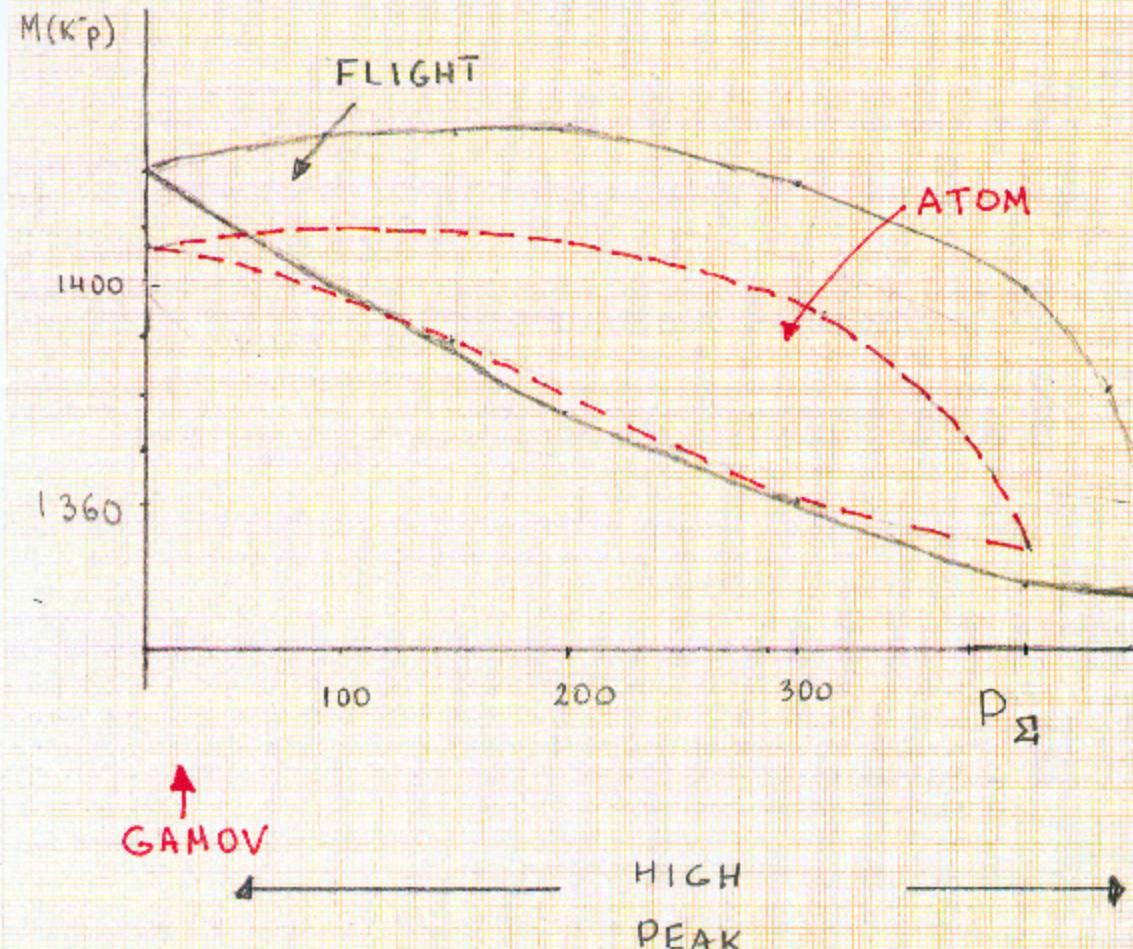


# $\Sigma^+$ nucleus scattering at low momenta



No  $\Sigma^+$  beams , only intermediate  $Kp \rightarrow \Sigma\pi$

Complicates description     $\phi(r) \rightarrow G(r,r')$



PHASE SPACE

# Gamov Peak versus Main Peak

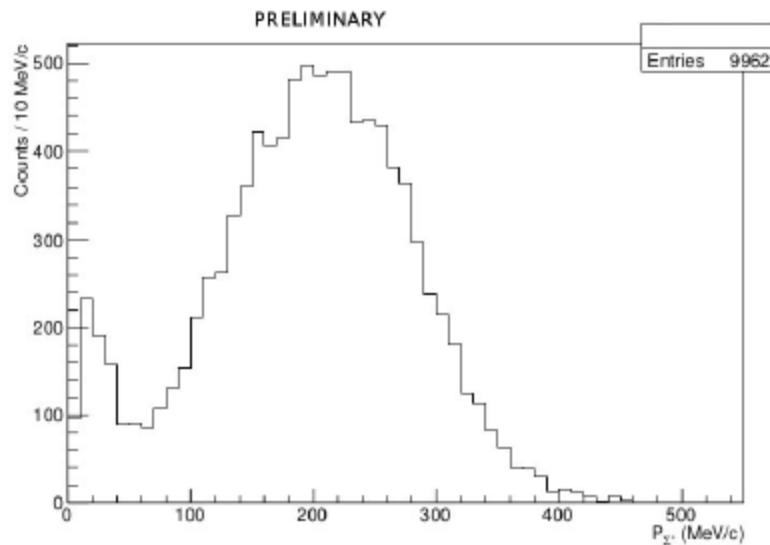


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