

# Heavy-ion induced transfer reactions and the role of pairing

NUSPRASEN Workshop on Nuclear Reactions (Theory and Experiment)



Heavy Ion Laboratory, Warsaw 22-24 January 2018

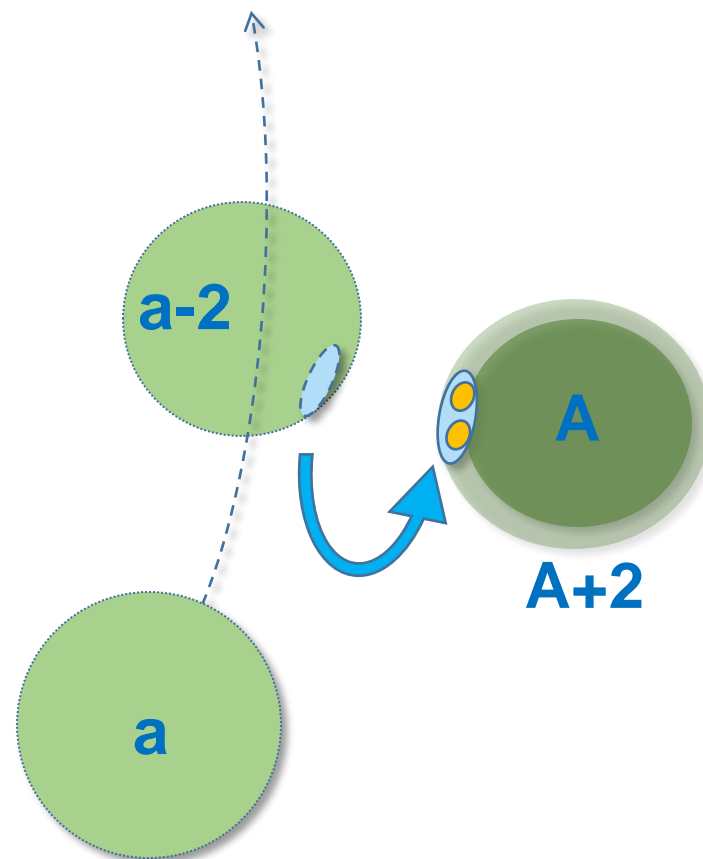
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# Direct transfer reactions

- ❖ Select specific **degrees of freedom** in the complex many-body nuclear system
- ❖ Exploration of the **nuclear structure**
  - ❖ Relation between 1n transfer cross sections and **single-particle configurations**
  - ❖  $\alpha$  transfer and **clustering**
  - ❖ Connection between 2n transfer probabilities and **pairing correlations** in nuclei



The extraction of structure information from  $2n$  transfer cross-sections is not straightforward

## Heavy ions



### Experimental difficulties

- ❖ Particle identification capability
- ❖ Resolution (energy and angle)
- ❖ Absolute cross-section measurement

The techniques to extract the optical potential from fits of elastic scattering data fail

- ❖ Coupling with inelastic excitations (CC corrections)
- ❖ Recoil effects
- ❖ Finite range f.f.
- ❖ Sequential transfer
- ❖ Only the product of projectile and target S.F. is accessible

**Arbitrary scaling factors**  
***"unhappiness" ( $\gg 1$ )***  
**to reproduce the exp.**  
**angular distributions**



# Our study:

## The ( $^{18}\text{O}, ^{16}\text{O}$ ) two-neutron transfer

The ( $^{18}\text{O}, ^{16}\text{O}$ ) reactions are good candidates to show the role of **pairing interaction** thanks to

- The presence of a **correlated pair** of neutrons in the  $^{18}\text{O}_{\text{g.s.}}$  w.f.
- The very low polarizability of the  **$^{16}\text{O}$  core**

### Different target systems explored

$^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$   
 $^{13}\text{C}(^{18}\text{O}, ^{16}\text{O})^{15}\text{C}$   
 $^{16}\text{O}(^{18}\text{O}, ^{16}\text{O})^{18}\text{O}$   
 $^{28}\text{Si}(^{18}\text{O}, ^{16}\text{O})^{30}\text{Si}$   
 $^{64}\text{Ni}(^{18}\text{O}, ^{16}\text{O})^{66}\text{Ni}$   
heavier...

Studies on **one-neutron transfer** ( $^{18}\text{O}, ^{17}\text{O}$ ) to ascertain the selectivity of the two processes in exciting s.p. and two-particle configurations

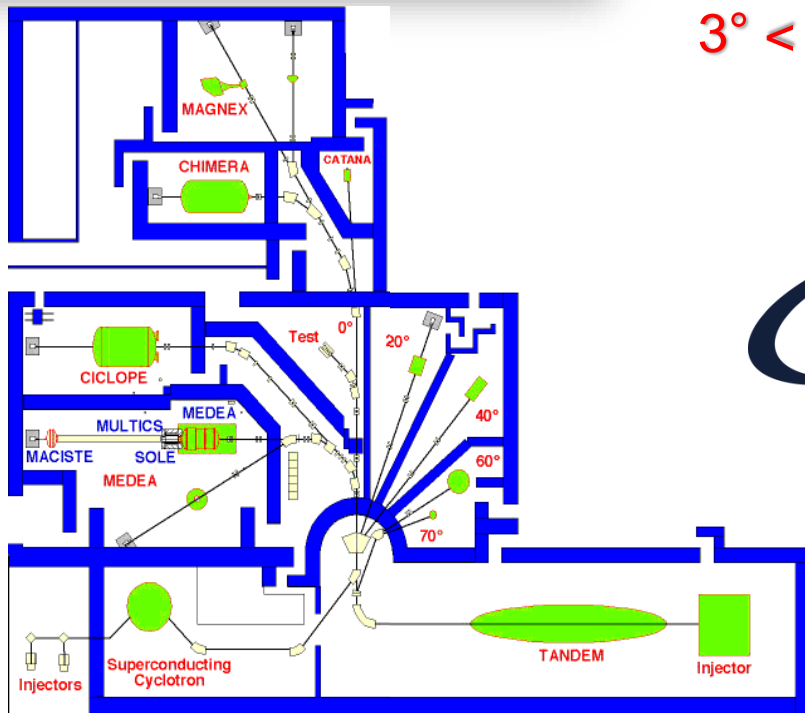
**One-proton and two-proton transfer** channels measured, under analysis

# The experiments



- $^{18}\text{O}$  beam from Tandem at 84 MeV (and Superconducting Cyclotron at 270 MeV)
- Several thin targets (50 -100  $\mu\text{g}/\text{cm}^2$ )
- Ejectiles detected by the MAGNEX spectrometer
- Angular settings  $\theta_{opt} = 6^\circ, 12^\circ, 18^\circ, 24^\circ$

$$3^\circ < \theta_{lab} < 31^\circ$$





### Large acceptance:

- Energy -28%, +20%
- Angle 50 msr

# MAGNEX

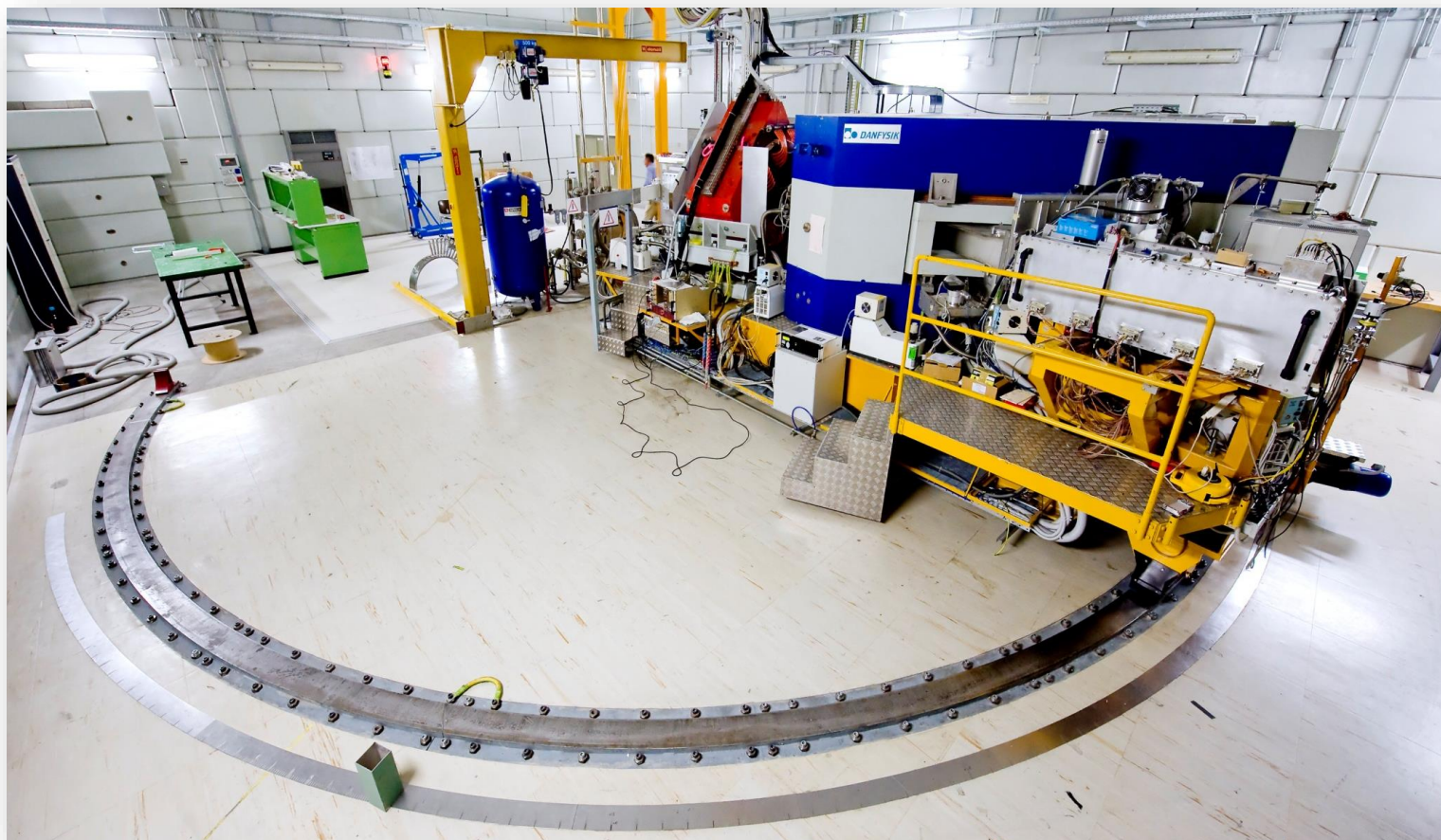
Good compensation of the aberrations

Trajectory reconstruction

### Measured resolutions:

- Energy  $\Delta E/E \sim 1/1000$
- Angle  $\Delta\theta \sim 0.3^\circ$
- Mass  $\Delta m/m \sim 1/160$

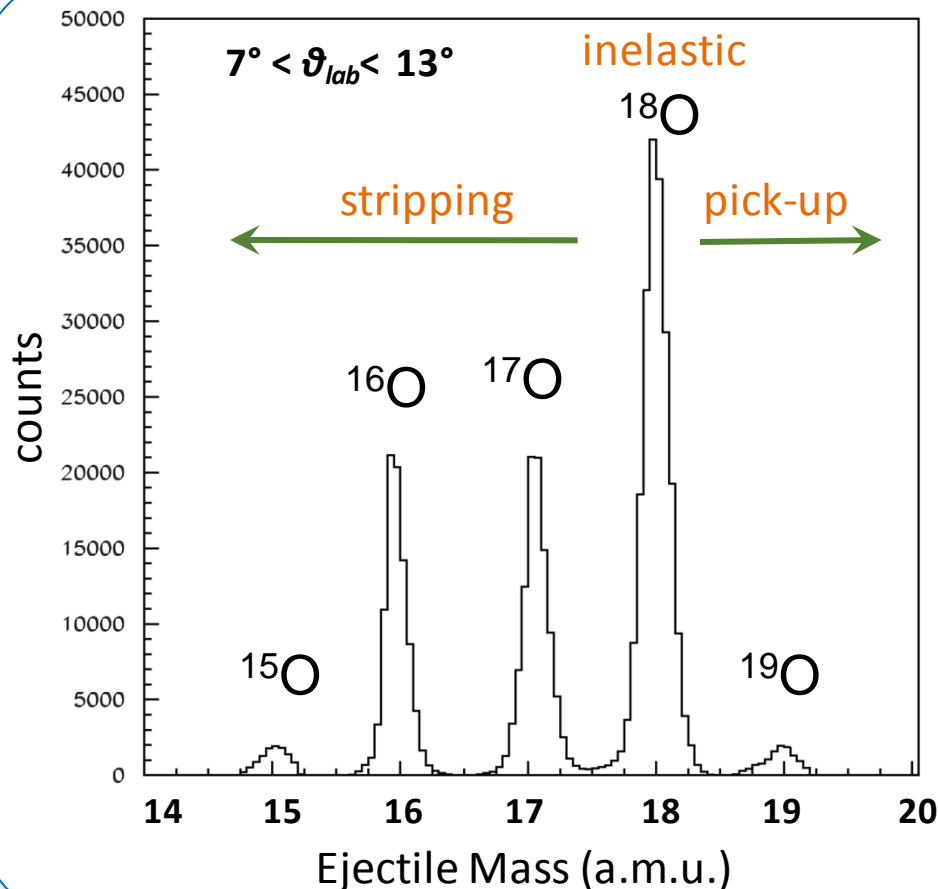
*F. Cappuzzello et al. EPJA (2016) 52 :167*



# Some experimental evidence:

## 1) Transfer Yields

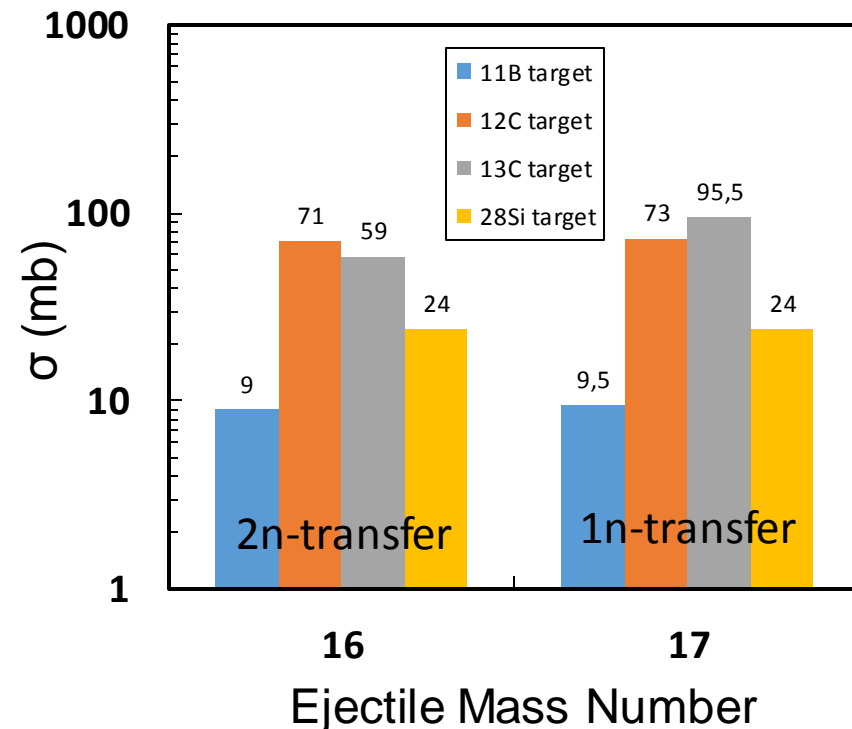
$^{18}\text{O} + ^{13}\text{C}$  @84 MeV



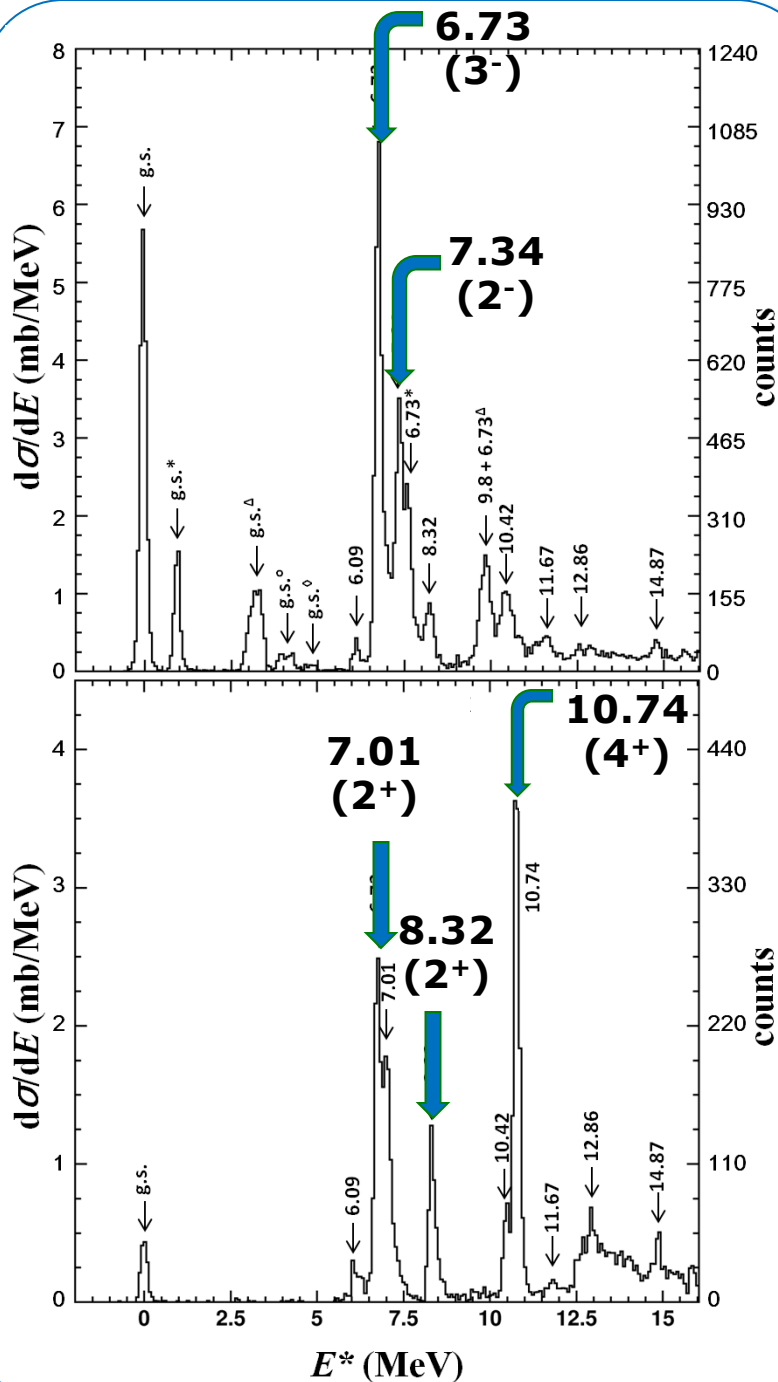
Enhancement of the two-neutron transfer channel

The 2n-transfer is not a 2<sup>nd</sup> order process

TRANSFER OF A CORRELATED PAIR



# Some experimental evidence: 2) Energy Spectra



$^{13}\text{C}(^{18}\text{O}, ^{17}\text{O})^{14}\text{C}$

$$\left[ \left( ^{13}\text{C}_{gs} \right)^{1/2^-} \otimes \left( 1d_{5/2} \right)^{5/2^+} \right]^{2^-, 3^-}$$

In the  $(^{18}\text{O}, ^{16}\text{O})$ , the **suppression of s.p. states**, which would require an uncorrelated transfer of 2n and the breaking of the initial pair in the  $^{18}\text{O}_{\text{g.s.}}$ , reveals the minor role of the **two-step dynamics**

$^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$

$$\left[ \left( ^{12}\text{C}_{gs} \right)^{0^+} \otimes \left( 1d_{5/2}, 2s_{1/2} \right)^{2^+, 4^+} \right]^{2^+, 4^+}$$

M. Cavallaro, et al., PRC 88 (2013) 054601  
F. Cappuzzello et al., Nature Comm. 6 (2015) 6743



# Microscopic quantum description of reaction mechanism and nuclear structure

## Exact Finite Range CRC

- ❖ Sao Paulo Potential (**SPP**) used in the optical model
- ❖ **Wood-Saxon form factors** used to generate single particle and cluster wave functions. Depth adjusted to fit exp. separation energies
- ❖ **Deformation parameters** for collective excitations

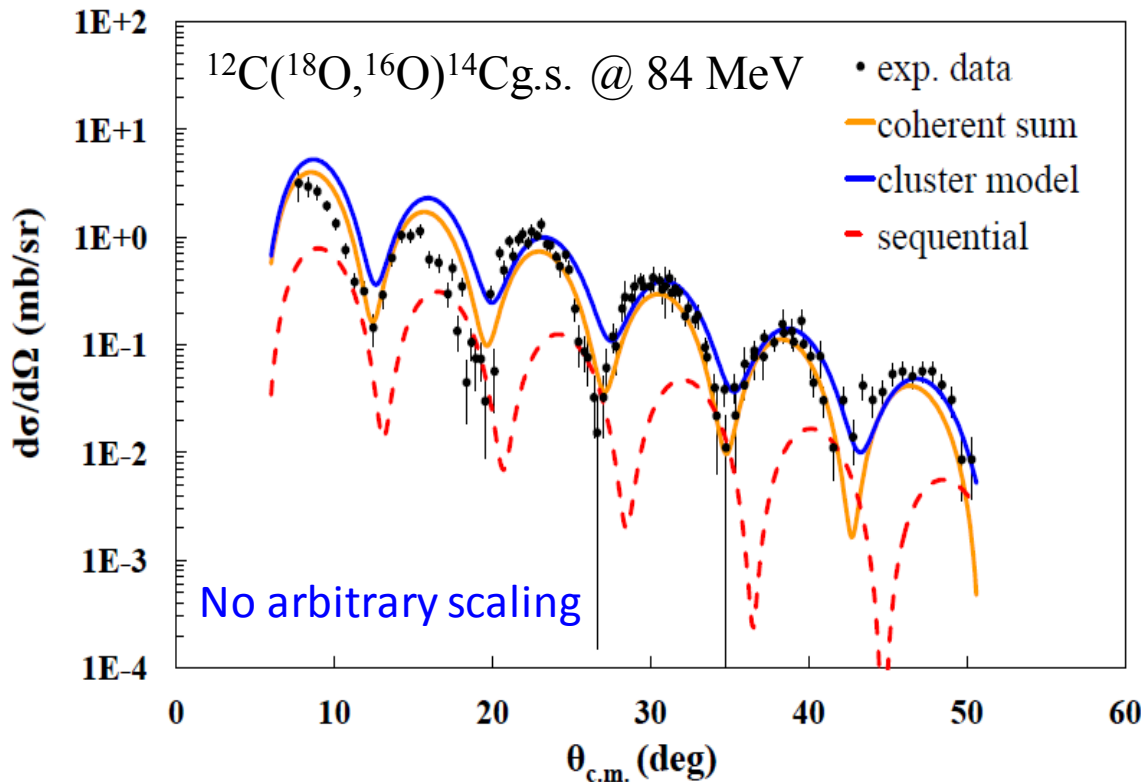
Calculations by  
J. Lubian et al. – Niteroi (Brasil)

- ❖ **Spectroscopic Amplitudes** by shell-model, IBM-2, IFBM-2

Calculations by  
A.Gargano – Napoli (Italy)  
S.M.Lenzi – Padova (Italy)  
E. Santopinto – Genova (Italy)

# The $^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$ reaction

*M. Cavallaro, et al., PRC 88 (2013) 054601*



A **0.89** amplitude is obtained by scaling to the experimental data (**0.91** S.A. predicted by shell model for the  $(p_{1/2})^2$  configuration).

## Extreme Cluster Model

(CRC)

- ❖ Relative motion of the 2n system frozen and separated by the c.m.
- ❖ Only the term with the 2n coupled to  $S = 0$  participates to the transfer

## Sequential transfer (DWBA)

Introducing the  $^{17}\text{O} + ^{13}\text{C}$  intermediate partition

## Coherent sum

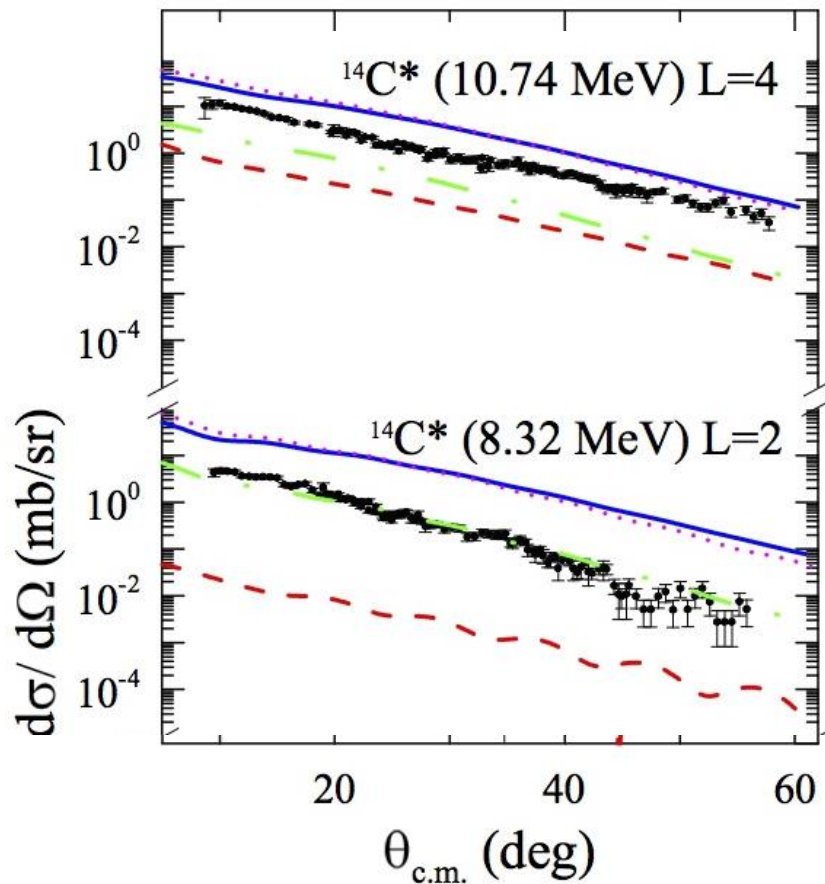
Presence of two-neutron pairing correlations in the  $^{14}\text{C}$  ground state

# The $^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$ reaction

$^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$  @ 84 MeV

— Cluster model  
- - Sequential transfer  
- · - Independent coordinates

No scaling



**Extreme cluster model** largely overestimates the data. A larger model space for the cluster wave function is needed.

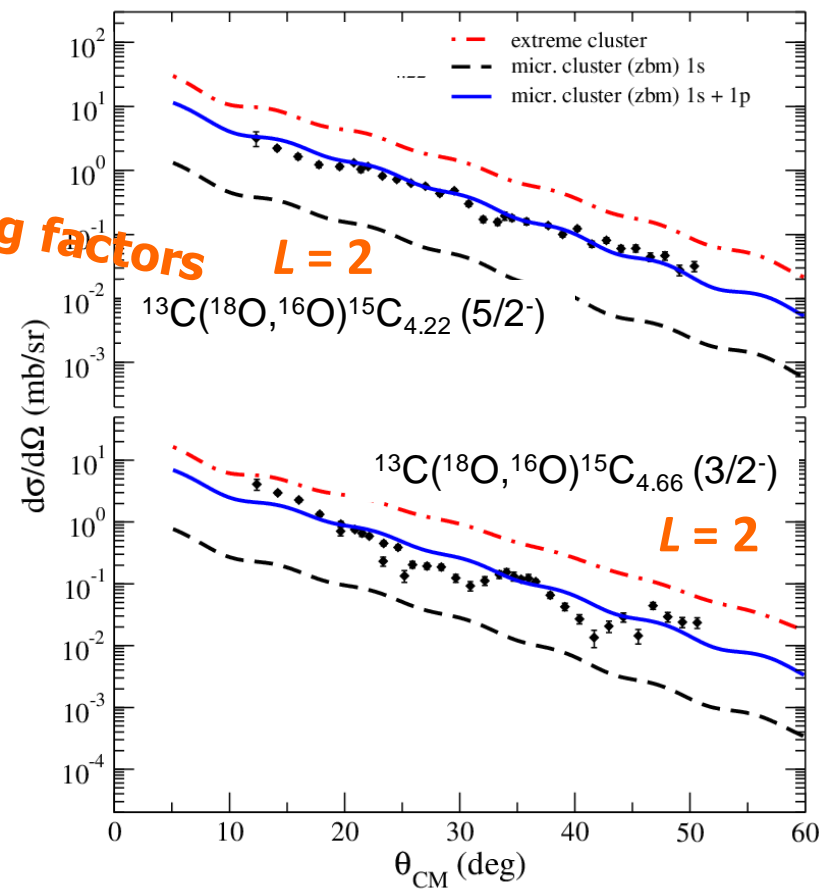
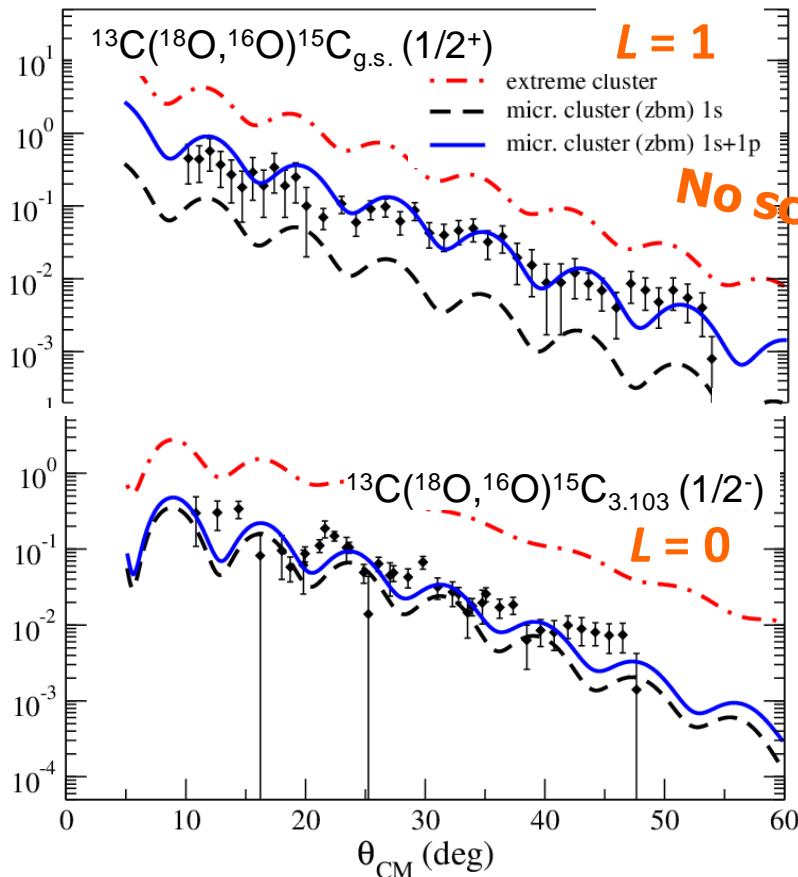
## Independent coordinates scheme

The transfer is described taking into account s.p. information obtained by shell model calculations ( $p_{1/2}s_{1/2}d_{5/2}$ )

- well reproduce L=2 data.
- underestimates the L=4 data. A larger space is required in the shell-model. Not surprising since one expects relevant ( $d_{5/2} d_{3/2}$ ) contributions in the  $4^+$  wave function, excluded in our model space

**Sequential transfer** small

# The $^{13}\text{C}(^{18}\text{O}, ^{16}\text{O})^{15}\text{C}$ reaction



----- Extreme cluster model overestimates data

The extreme cluster model assumes  $S = 0$  coupling of the two neutrons with 100% of probability



Overestimation of the cross-section

# A «less extreme» cluster model: microscopic cluster model

- Introducing both parallel and antiparallel couplings ( $S=0$  and  $S=1$ )
- Realistic spectroscopic amplitudes derived from shell-model calculations

Wave functions for two particles in terms of individual coordinates ( $j$ - $j$  coupling)



wave functions in terms of the relative and centre of mass coordinates of the two particles ( $LS$  coupling)

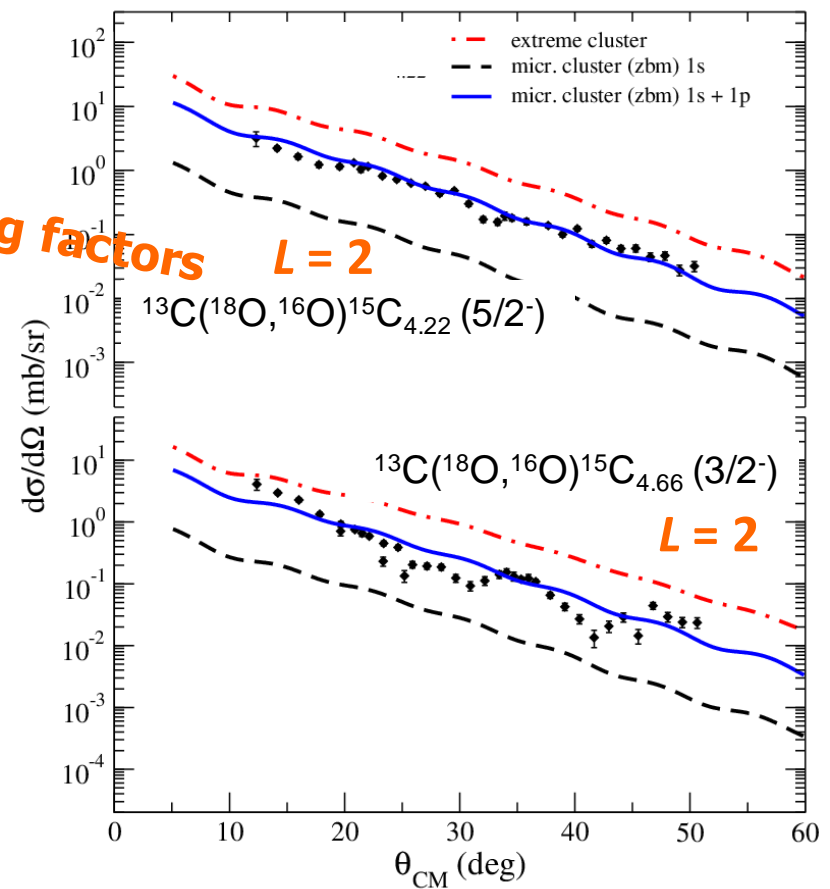
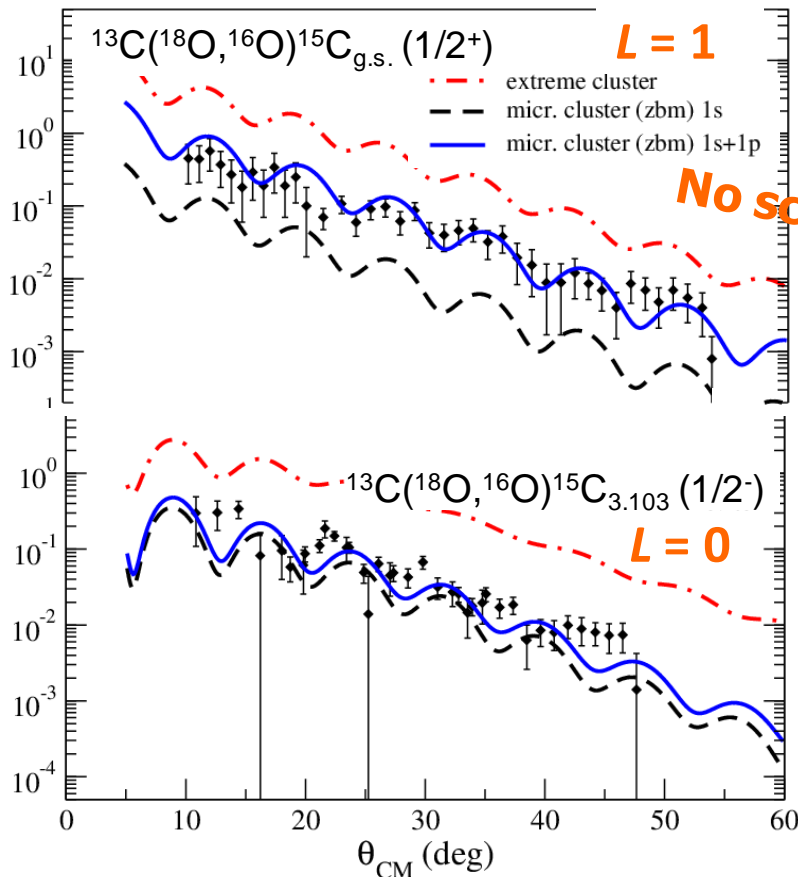
$(n,l)$  cluster internal state

$(N,L)$  cluster motion relative to the core

The use of this model can highlight the presence of cluster components in the involved wave functions



# The $^{13}\text{C}(^{18}\text{O}, ^{16}\text{O})^{15}\text{C}$ reaction



--- Extreme cluster model

- - - Microscopic cluster 1s

Taking into account configurations with  $n = 1 \quad l = 0$

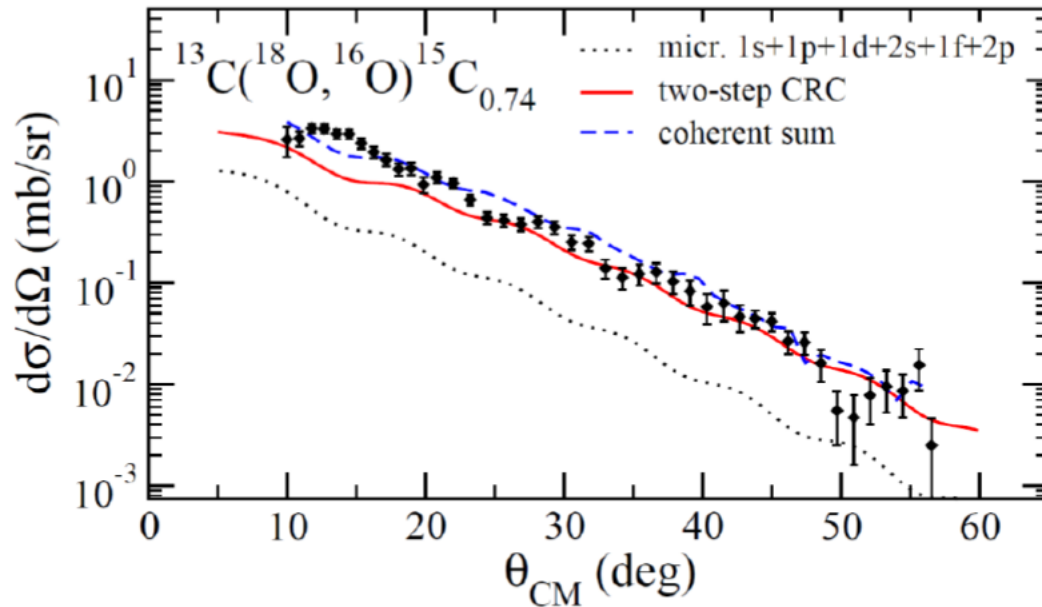
— Microscopic cluster 1s + 1p

Taking into account configuration with  $n = 1 \quad l = 0, 1$

Cross sections well reproduced by microscopic cluster with 1s + 1p waves

# The $^{13}\text{C}(^{18}\text{O}, ^{16}\text{O})^{15}\text{C}$ reaction

The 0.74 MeV state has a different behaviour



Cross sections  
**underestimated by**  
**microscopic cluster with**  
**1s+1p+2d+2s+1f+2p waves**

**Two-step CRC gives the**  
**dominant contribution**

----- **Two-step CRC**

----- **Microscopic cluster 1s+1p+2d+2s+1f+2p**

———— **Coherent sum**

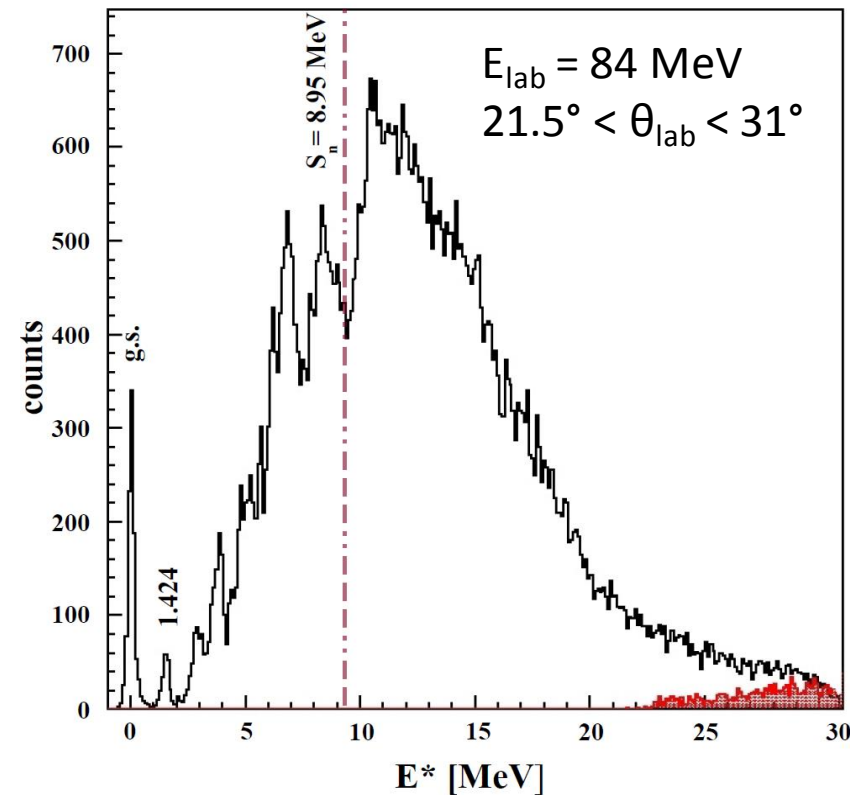
Single-particle state

$$\left| \left[ \left( ^{14}\text{C}_{gs} \right)^{0+} \otimes \left( 1d_{5/2} \right)^{5/2+} \right]^{5/2+} \right\rangle$$

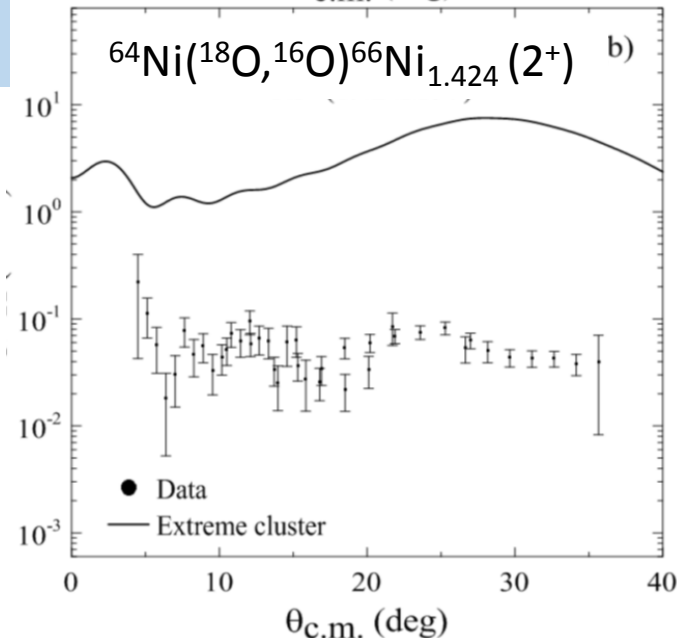
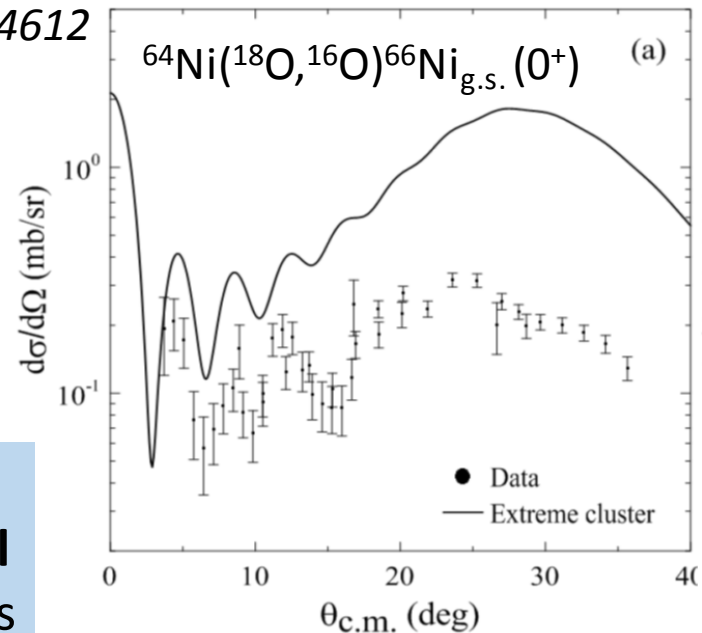
Breaking of the projectile pair  
in the transfer

# The $^{64}\text{Ni}(^{18}\text{O}, ^{16}\text{O})^{66}\text{Ni}$ reaction

*B. Paes, et al., PRC 96 (2017) 044612*



**Extreme  
cluster model  
overestimates  
data**



# The $^{64}\text{Ni}(^{18}\text{O}, ^{16}\text{O})^{66}\text{Ni}$ reaction

*B. Paes et al., PRC 96 (2017) 044612*

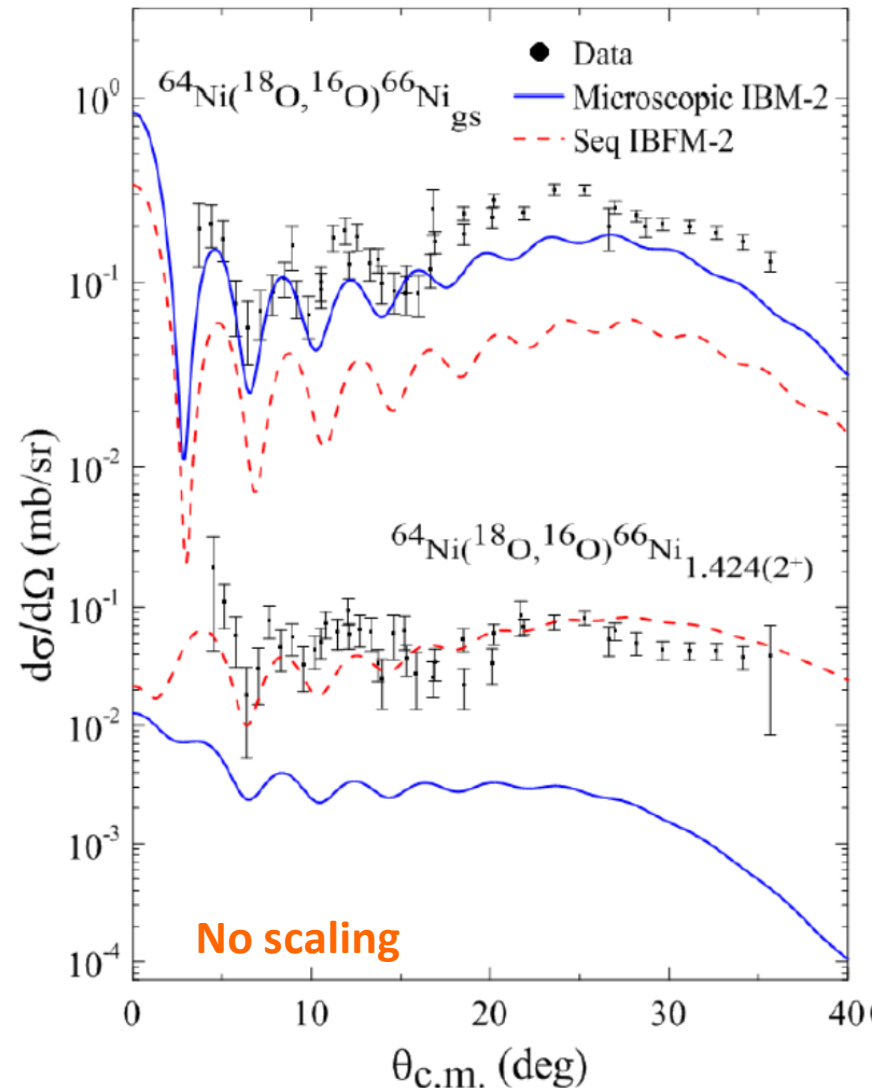
**Microscopic Interacting Boson Model**  
(IBM-2) applied for the first time to a  
2n-transfer reaction (Ni isotopes upper  
limit of confident applicability of SM)

## One-step (Ind. Coordinates)+ IBM-2

- well describes the transition to  $0^+$  g.s.
- underestimates the transition to  $2^+$

## Sequential + IBFM-2

- gives a very small contribution in the transition to  $0^+$
- well describes the transition to  $2^+$



# The $^{64}\text{Ni}(^{18}\text{O}, ^{16}\text{O})^{66}\text{Ni}$ reaction

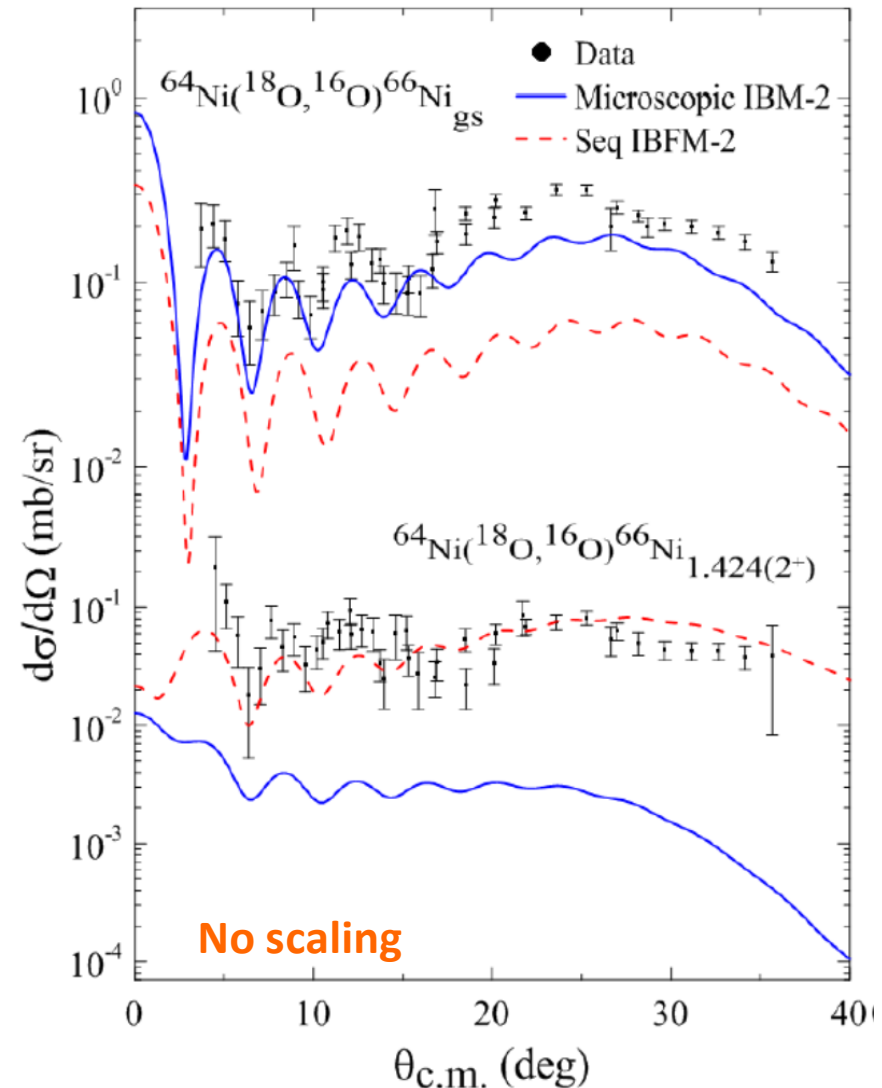
*B. Paes et al., PRC 96 (2017) 044612*

In the transfer to  $0^+$  g.s., **pairing correlations** play an important role (one-step mechanism is dominant)

In the  $2^+$  (collective) **other correlations** among nucleons are dominant over the pairing correlations (sequential mechanism is dominant)

Reduced electric quadrupole transition probabilities

Nucleus	$B(E2); 0^+ \rightarrow 2^+ (e^2 b^2)$
$^{14}\text{C}$	0.0018
$^{18}\text{O}$	0.0045
$^{28}\text{Mg}$	0.035
$^{30}\text{Si}$	0.022
$^{66}\text{Ni}$	0.060
$^{76}\text{Ge}$	0.270







# The NUMEN program and the ERC project NURE



NURE -714625

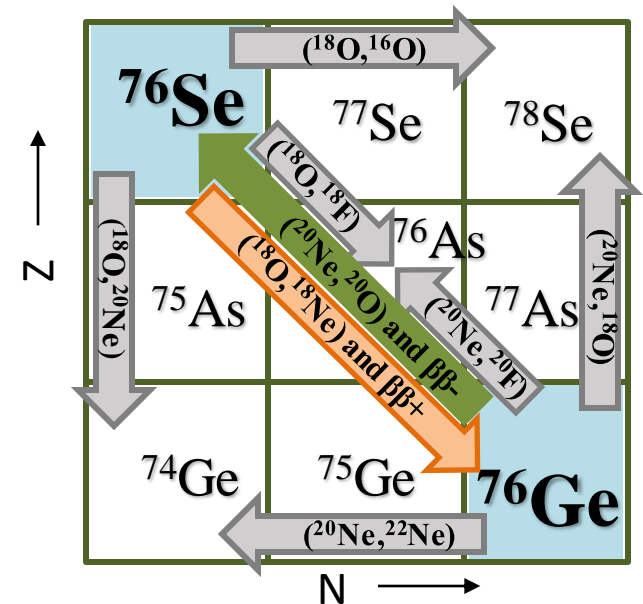
A **complete** and **reliable** description of HI induced transfer reactions is a crucial tool within the NUMEN project

Study **Double Charge Exchange (DCE) reactions** in systems candidate to  $0\nu\beta\beta$  to stimulate in the laboratory the same nuclear transition occurring in  $0\nu\beta\beta$  and get info on the NME

## Two directions:

$\beta\beta^+$  via  $(^{18}\text{O}, ^{18}\text{Ne})$  and  $\beta\beta^-$  via  $(^{20}\text{Ne}, ^{20}\text{O})$

Contribution of all the **competing channels**  
(We can measure most of them, while we need the prediction of theory for some other cases)



See poster by  
N. Nitin Deshmukh

# Conclusion

- ❖ **High resolution measurements** of energy spectra and angular distribution for **HI reactions**
- ❖ **Enhancement of the 2n stripping** in the mass spectra and strong **selectivity** in the energy spectra
- ❖ Microscopic quantum description of the experimental cross-section for heavy-ion 2n transfer reactions **without unhappiness factors**
- ❖ Role of **pairing correlations**
- ❖ The possibility to achieve a **reliable** and **predictive description** of HI transfer channels on heavy targets is crucial for the research related to  **$0\nu\beta\beta$  (NUMEN project)**

# Working group

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Thank you!

