



DESCRIPTION OF ENHANCEMENT OF TOTAL CROSS SECTIONS OF REACTIONS WITH ⁶HE AND ⁹LI NUCLEI

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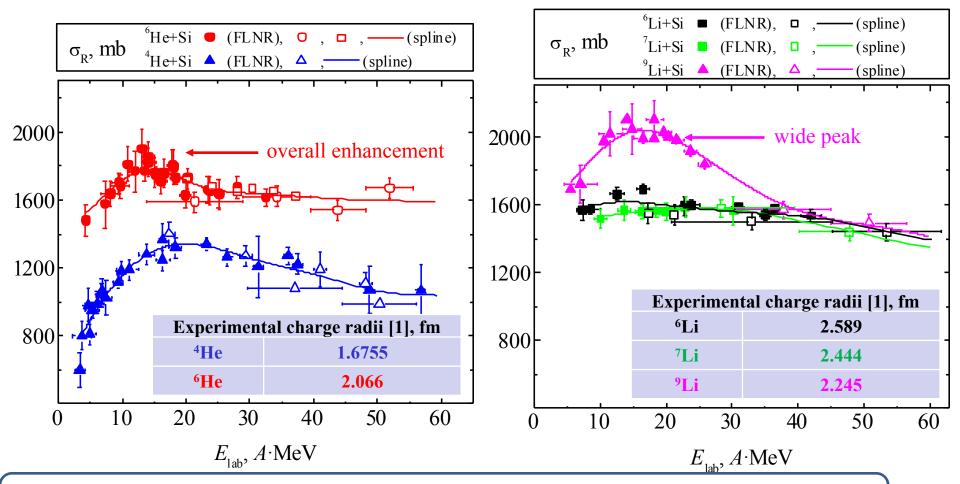


Peculiarities of total reaction cross sections for

⁶He + ²⁸Si and ⁹Li + ²⁸Si compared with



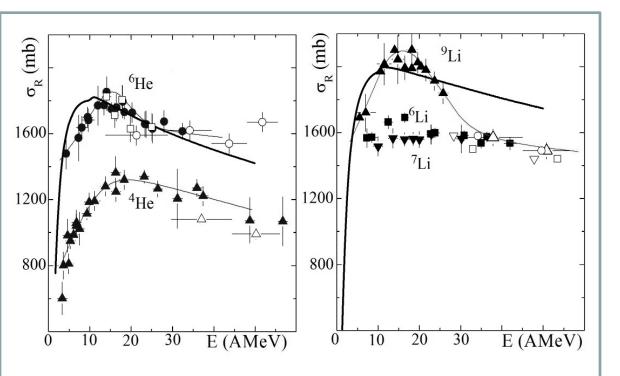
 $^{4}\text{He} + ^{28}\text{Si}$ and $^{6,7}\text{Li} + ^{28}\text{Si}$

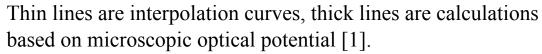


⁶He + ²⁸Si: enhancement in whole energy range: geometric effect;

 9 Li + 28 Si: wide peak in energy range 10 – 30 $A\cdot$ MeV: structural & dynamical effect.

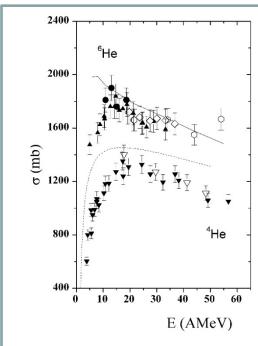
Previous attempts of theoretical description





[1] K.V. Lukyanov et al., Bull. Rus. Acad. Sci. Phys. **72**, 356 (2008).

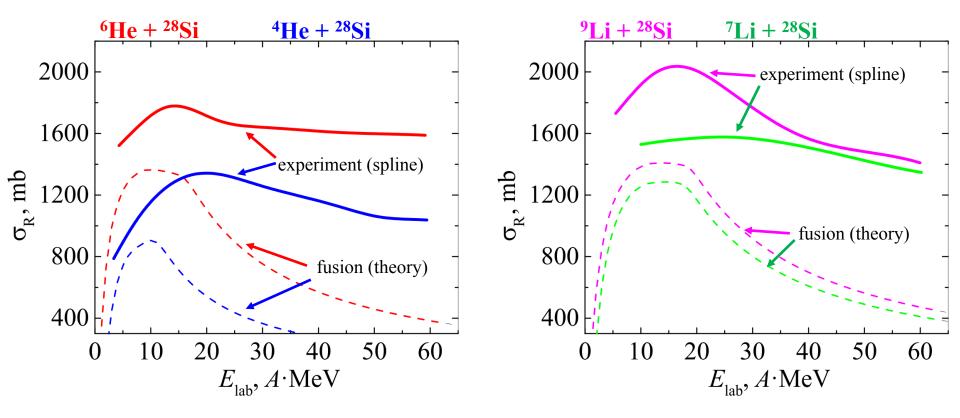
Picture from Yu.G. Sobolev et al., PEPAN 48, in press, (2017).



Dotted curve is an empirical model (Phys. Rev C 35, 1678 (1987)), solid curve is semimicroscopic optical model (Phys. Part. Nucl. 30, 870 (1999)).

Picture from G.D. Kabdrakhimova *et al.*, Phys. At. Nucl. **80**, 32 (2017).

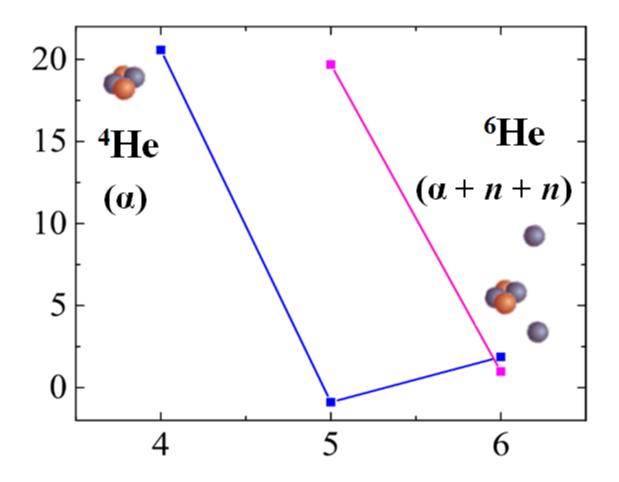
Estimation of contribution of complete fusion channel to total cross sections within one-dimensional barrier penetration model [1]



Complete/incomplete fusion is one of the main channels contributing to total reaction cross sections. Other possible channels are breakup, nucleon transfer, etc.

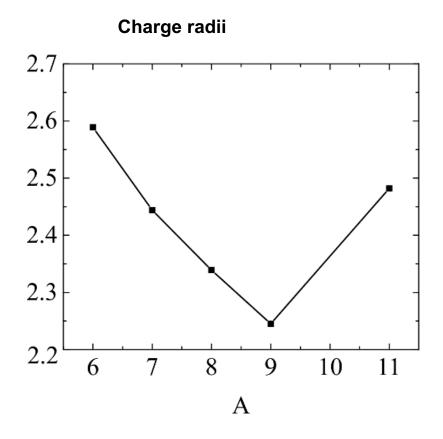
Structure of nuclei ^{4,6}He

Neutron separation energy: 1n & 2n

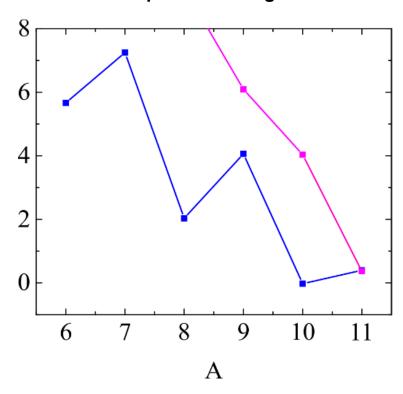


⁶He can be represented as $(\alpha + n + n)$ based on experimental data on neutron separation energies, charge radii, etc.

Structure of nuclei 6,7,9Li







⁶Li
$$(\alpha + d)$$

 7 Li $(\alpha + t)$

 $^{9}\text{Li} (^{7}\text{Li} + n + n)$:

⁹Li can be represented as $(^7\text{Li} + n + n)$ based on experimental data on neutron separation energies, charge radii, etc.

Time-dependent Schrödinger equation approach

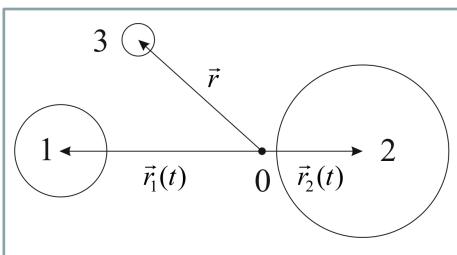
Classical motion of centers of nuclei

$$m_1 = -\nabla_{r_1} V_{12} \left(\begin{vmatrix} \mathbf{r} & \mathbf{r} \\ r_1 - r_2 \end{vmatrix} \right), \ m_2 = -\nabla_{r_2} V_{12} \left(\begin{vmatrix} \mathbf{r} & \mathbf{r} \\ r_2 - r_1 \end{vmatrix} \right).$$

• Transfer (rearrangement) of neutrons during collision is described by timedependent Schrödinger equation with spin-orbit interaction [1-4]

$$ih\frac{\partial}{\partial t}\Psi(\overset{\mathbf{r}}{r},t) = \left\{-\frac{h^2}{2m}\Delta + V_1(\overset{\mathbf{r}}{r},t) + V_2(\overset{\mathbf{r}}{r},t) + \hat{V}_{LS}^{(1)}(\overset{\mathbf{r}}{r},t) + \hat{V}_{LS}^{(2)}(\overset{\mathbf{r}}{r},t)\right\}\Psi(\overset{\mathbf{r}}{r},t).$$

• The initial wave function is determined from shell model. Parameters of shell model were chosen based on experimental data on charge radii and neutron (proton) separation energies.

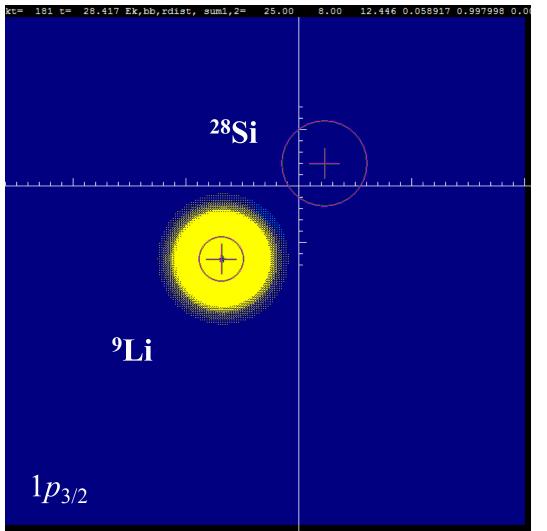


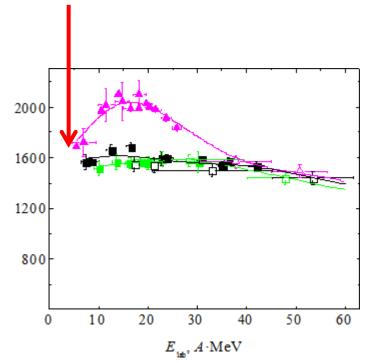
1,2 are two heavy classical particles; 3 is light quantum particle (neutron of projectile or target).

References

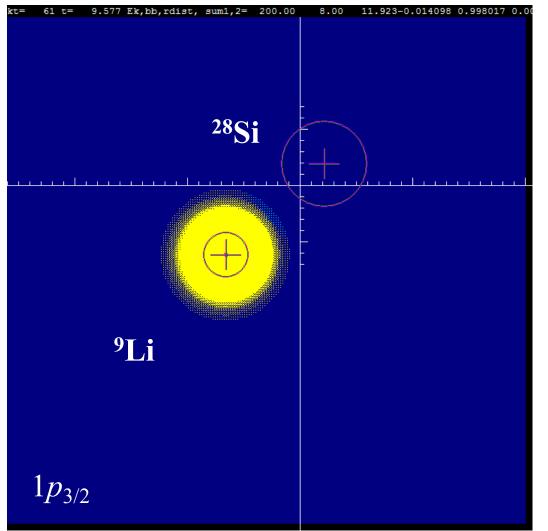
- [1] V. V. Samarin, EPJ Web Conf. 66, 03075 (2014); 86, 00040 (2015).
- [2] V. V. Samarin. Phys. At. Nucl. 78,128 (2015).
- [3] M. A. Naumenko, V. V. Samarin, Yu. E. Penionzhkevich, N. K. Skobelev. Bull. Russ. Acad. Sci. Phys. 80, 264 (2016).
- [4] M. A. Naumenko, V. V. Samarin, Yu. E. Penionzhkevich, N. K. Skobelev. Bull. Russ. Acad. Sci. Phys. 81, 710 (2017).

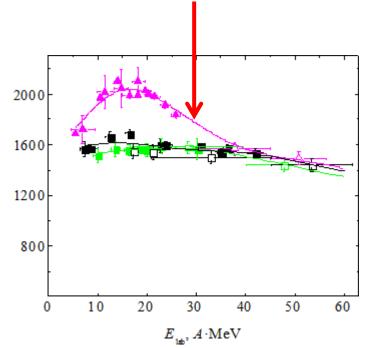
Evolution of probability density of one external neutron of ⁹Li nucleus in collision ⁹Li + ²⁸Si at 3.7 A·MeV



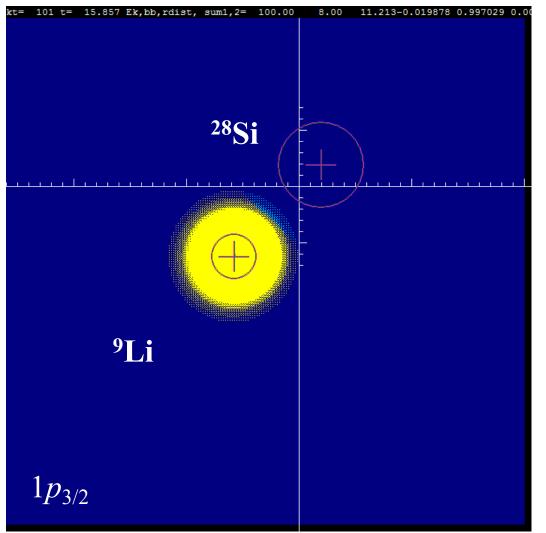


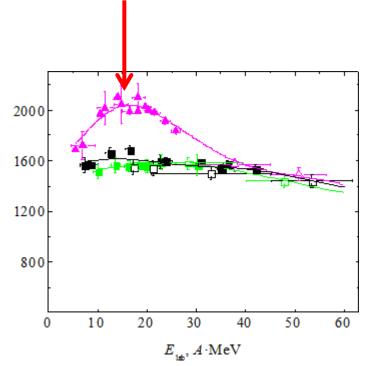
Evolution of probability density of one external neutron of ⁹Li nucleus in collision ⁹Li + ²⁸Si at 30 A·MeV



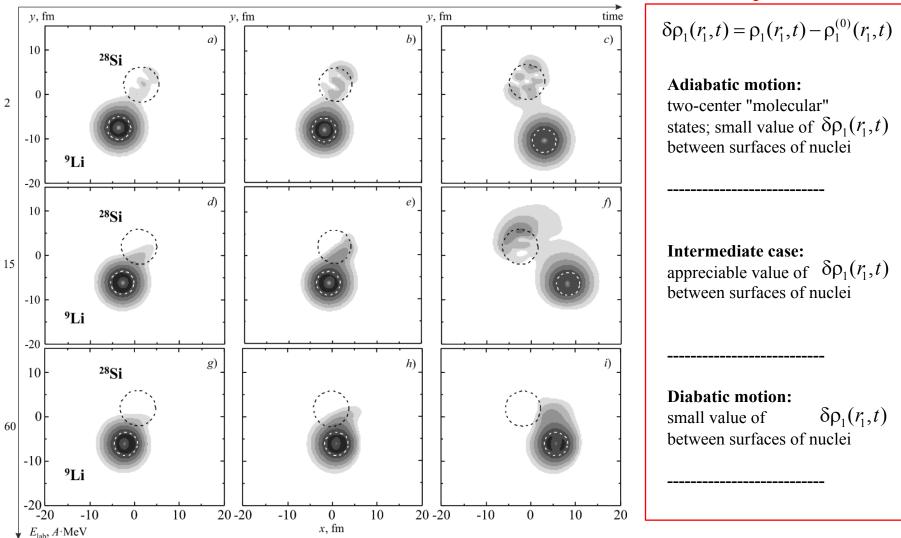


Evolution of probability density of one external neutron of ⁹Li nucleus in collision ⁹Li + ²⁸Si at 15 A·MeV



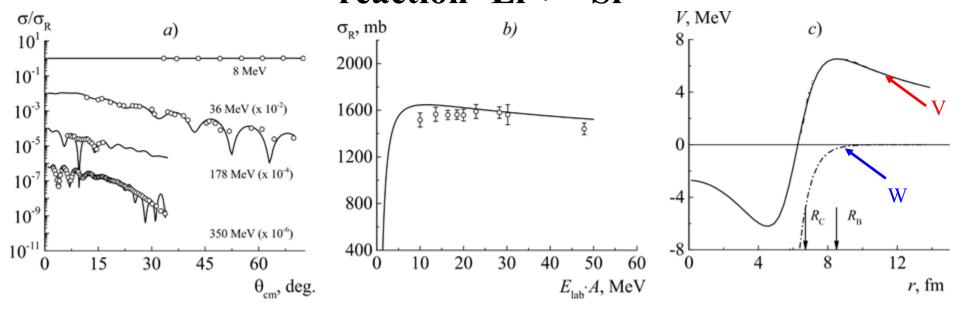


Evolution of probability density of one external neutron of ⁹Li nucleus in collision ⁹Li + ²⁸Si: summary



Rearrangement of external weakly bound neutrons of ⁶He & ⁹Li depending on energy suggests introduction of **energy-dependent corrections to nuclear part of nucleus-nucleus potential in optical model.**

Choice of parameters of optical potential for reaction ⁷Li + ²⁸Si



Energy-independent parameters of optical potential in Woods-Saxon form for the $^{6,7}\text{Li} + ^{28}\text{Si}$ reactions were chosen based on analysis of experimental data on angular distributions of elastic scattering for a number of energies in wide range: $^{6}\text{Li} + ^{28}\text{Si}$ ($E_{\text{lab}} = 7.5 \div 318 \text{ MeV}$) & $^{7}\text{Li} + ^{28}\text{Si}$ ($E_{\text{lab}} = 8 \div 350 \text{ MeV}$).

Energy-independent parameters of optical potential in the Woods-Saxon form for ${}^{9}\text{Li} + {}^{28}\text{Si}$ reaction were obtained by extrapolating the parameters for ${}^{6,7}\text{Li} + {}^{28}\text{Si}$.

Good agreement with experimental data on elastic scattering; acceptable agreement with experimental data total cross section; parameters for ⁹Li + ²⁸Si were chosen close to the parameters for ^{6,7}Li + ²⁸Si.

Energy-dependent corrections to nuclear part of nucleusnucleus potential

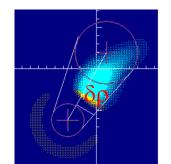
$$\operatorname{Re} \left\{ V_{\mathrm{N}}(r) \right\} \equiv V(R, E_{\mathrm{lab}}) = \overline{V}(R) + \left| \eta_{\mathrm{l}}(E_{\mathrm{lab}}) \left[\varepsilon_{\mathrm{v}}(R) - \varepsilon_{\mathrm{v}}(\infty) \right] \right| + \left| \eta_{2}(E_{\mathrm{lab}}) \delta V_{\mathrm{d}}(R, E_{\mathrm{lab}}) \right|$$

$$\eta_{\mathrm{l}}(E_{\mathrm{lab}}) + \eta_{2}(E_{\mathrm{lab}}) = 1$$
 Adiabatic correction Diabatic correction
$$\frac{\varepsilon_{\mathrm{v}}(R)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)} + \frac{\varepsilon_{\mathrm{lab}} \left(1 \right)}{1 \rho_{\mathrm{lab}} \left(1 \right)}$$

 V_1 is velocity of projectile nucleus relative to target nucleus

 $\langle \mathbf{V} \rangle$ is average velocity of external neutrons in projectile nucleus

(method of calculation) [1] V.V. Samarin, Phys. At. Nucl. 78, 128 (2015).



Energy-dependent diabatic correction to nuclear part of nucleus-nucleus potential

 $\vec{r}_1(t)$

$$\operatorname{Re}\left\{V_{N}(r)\right\} \equiv V(R, E_{\text{lab}}) = \overline{V}(R) + \underbrace{\eta_{2}(E_{\text{lab}})\delta V_{d}(R, E_{\text{lab}})}$$

Diabatic correction

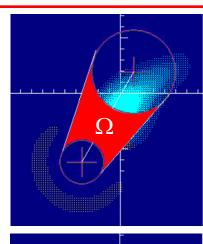
Similar to single folding

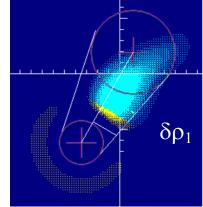
$$\delta V_{\rm d}\left(R(t), E_{\rm lab}\right) = N \int_{\Omega} d^3 r \delta \rho_1(r, t) U_{\rm T}\left(\left|\stackrel{\mathbf{r}}{r} - \stackrel{\mathbf{r}}{r_2}(t)\right|\right)$$
$$\delta \rho_1(r, t) = \rho_1(r, t) - \rho_1^{(0)}(r, t)$$

 Ω is integration region;

- $\rho_1(r,t)$ is the probability density of external neutrons of projectile taking into account their interaction with the target;
- $\rho_1^{(0)}(r,t)$ is the probability density of external neutrons of projectile without taking into account their interaction with the target;
- $U_{\rm T}(r)$ is mean field of the target nucleus for neutrons;

N = 2 is number of independent neutrons for ⁶He $(\alpha + n + n)$ & ⁹Li $(^7\text{Li} + n + n)$.





Weight of diabatic correction to nuclear part of nucleusnucleus potential

$$\text{Re}\{V_{N}(r)\} \equiv V(R, E_{\text{lab}}) = \overline{V}(R) + \overline{\eta_{2}(E_{\text{lab}})\delta V_{d}(R, E_{\text{lab}})}$$
 Diabatic correction

Weight of diabatic correction:

$$\eta_{2}(E_{\text{lab}}) = \frac{1}{1 + \exp\left[\frac{1}{\alpha}\left(\langle \varepsilon_{\text{kin}} \rangle - \left(\frac{E_{\text{lab}}}{A}\right)\right)\right]}$$

average velocity of external neutron in projectile nucleus, determined from shell model:

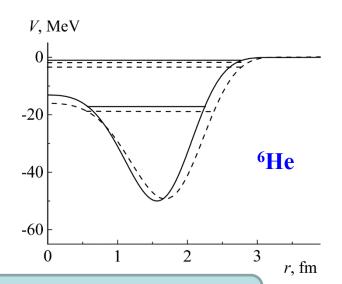
$$\langle \varepsilon_{\rm kin} \rangle \approx 10 \text{ MeV},$$

$$\alpha \sim 2 \text{ MeV}$$

R is distance between centers of nuclei.

$$\eta_2(E_{\text{lab}}) \to 0, \text{ if } \frac{V_1}{\langle v \rangle} << 1$$

$$\eta_2(E_{\text{lab}}) \to 1, \text{ if } \frac{V_1}{\langle v \rangle} >> 1$$



Weight of correction is determined by the ratio of velocity of projectile nucleus relative to target nucleus to average velocity of external neutrons in projectile nucleus

Energy-dependent potential of optical model

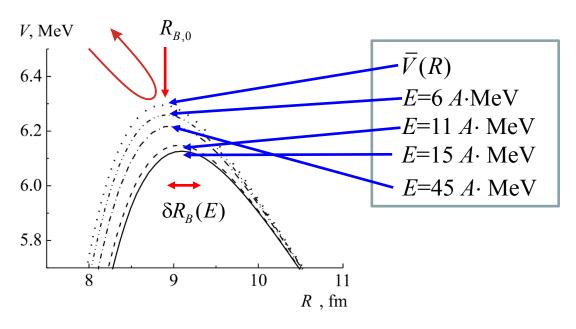
$$\operatorname{Re}\left\{V_{N}(r)\right\} \equiv V(R, E_{lab}) = \overline{V}(R) + \eta_{2}(E_{lab})\delta V_{d}(R, E_{lab})$$

Change in the radius of the imaginary part was chosen to be proportional to the change in the position of the barrier of the real part (for example, as in [1]):

$$\operatorname{Im}\left\{V_{N}(r)\right\} \equiv W(r) = \begin{cases} -W_{1}, r < R_{b} \\ W_{1} \exp\left(-\frac{r - R_{b}}{b}\right), r \ge R_{b} \end{cases}$$

$$R_B(E) = R_{B,0} + \delta R_B(E), \quad R_b(E) = R_a + k \delta R_B(E),$$

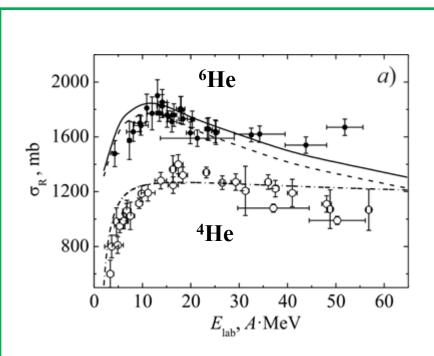
where R_a and k are parameters.



Change in the height and position of the barrier with increase of energy for ⁹Li + ²⁸Si, associated with the rearrangement of neutrons

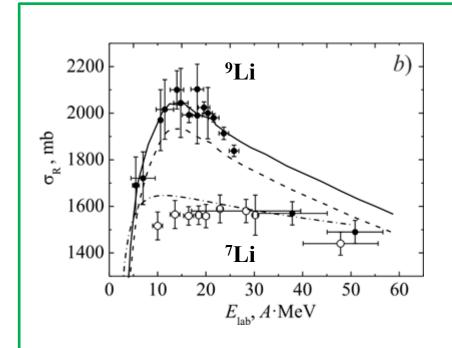
With increasing energy, the barrier first decreases and shifts to the right, and then returns to the original energy-independent one

Results of calculation of total reaction cross sections



⁶He vs. ⁴He: geometric effect prevails

⁶He + ²⁸Si: α= 1.8, W_1 = 10 MeV, b = 1 fm, k = 2, R_a = 5.0 fm (solid line) and 4.8 fm (dashed line).



⁹Li vs. ^{6,7}Li: dynamic effect prevails

 9 Li + 28 Si: α= 1.8, W_1 = 10 MeV, b = 1 fm, k = 2, R_a = 5.8 fm (solid line) and 5.6 fm (dashed line).

Conclusion

- Physical mechanism is proposed that qualitatively explains the observed features of the total cross sections for the reactions ^{4,6}He + ²⁸Si and ^{6,7,9}Li + ²⁸Si.
- Based on the solution of the time-dependent Schrödinger equation, an energy-dependent correction to the optical potential was calculated, which for the first time made it possible to obtain good agreement between the calculations and the experimental data on the total cross sections for these reactions.

