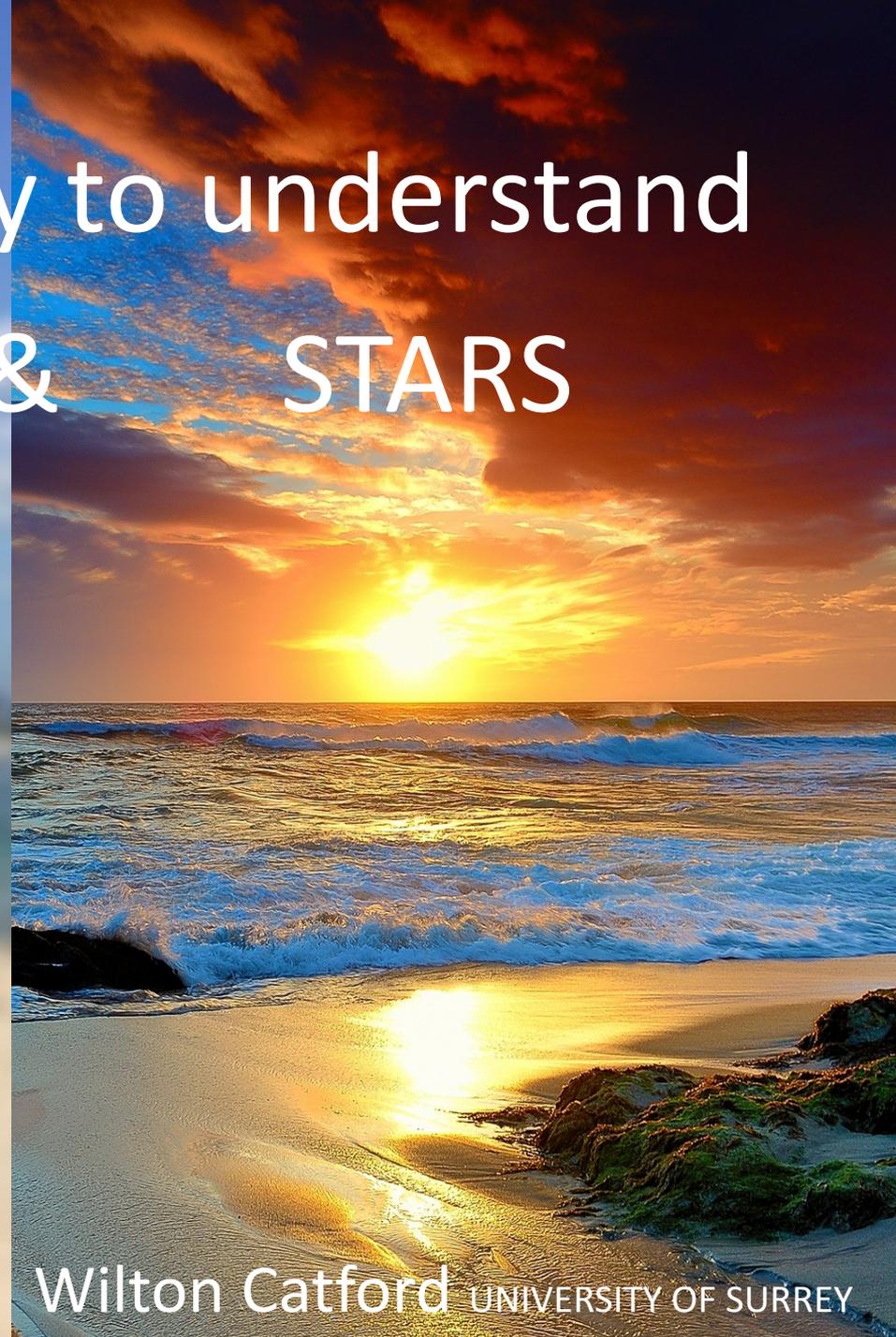


transfer as a way to understand SHELLS & STARS



COLLABORATORS FOR THIS WORK

In Surrey:

Gavin Lotay, Dan Doherty, Mhd Moukaddam,
Adrien Matta (LPC Caen), Ryan Wilkinson, Sam Hallam,
Gemma Wilson, Andy Knapton, Ilker Can Celik

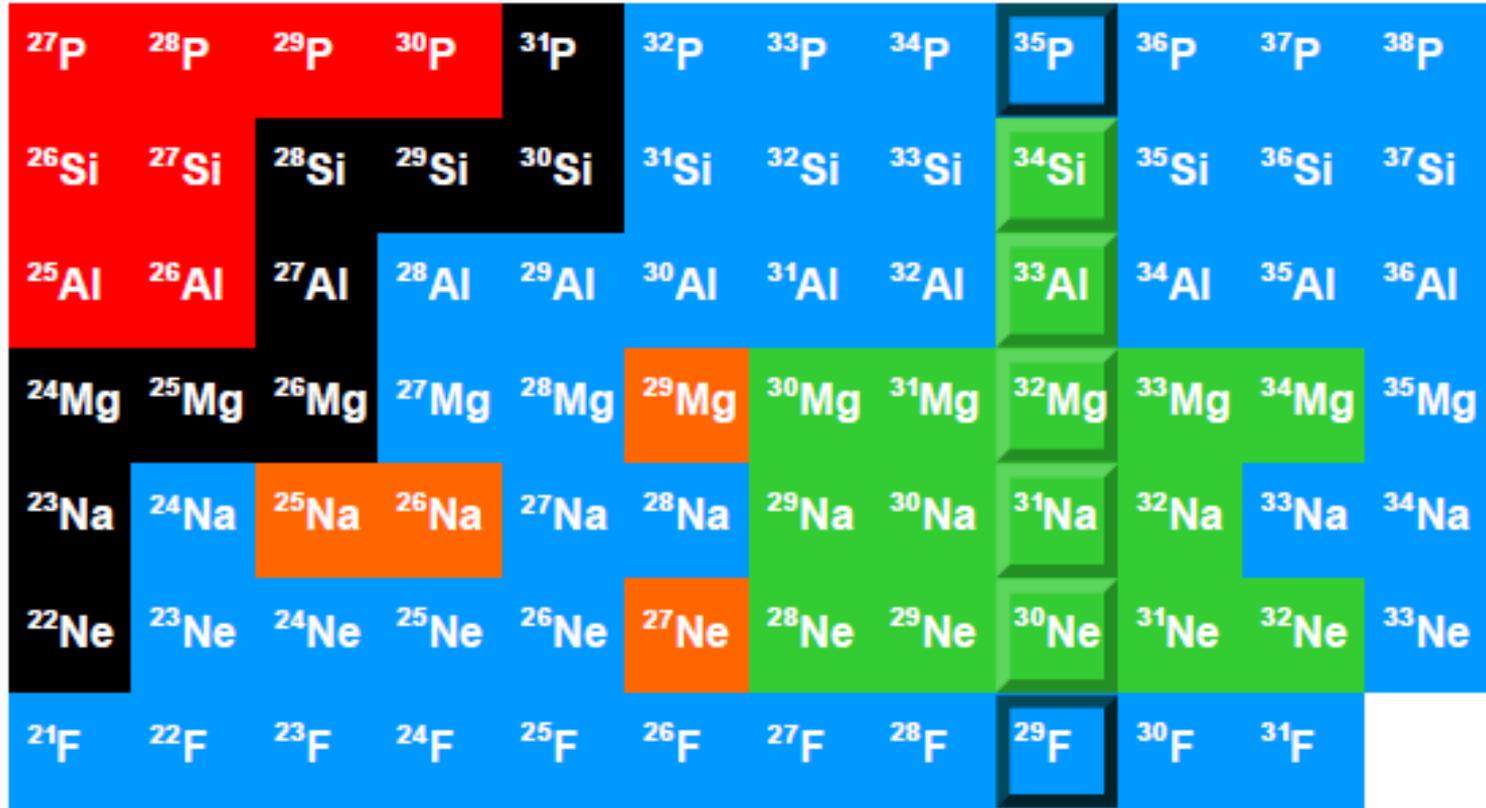
In TRIUMF:

Nigel Orr (LPC Caen), Greg Hackman, Jack Henderson,
Panu Ruotsalainen, Peter Bender, Carl Unsworth, Christian Aa. Diget,
Franck Delaunay (LPC Caen) and many more...

In Texas:

Greg Christian, Antii Saastamoinen, Shuya Ota, Eames Bennett

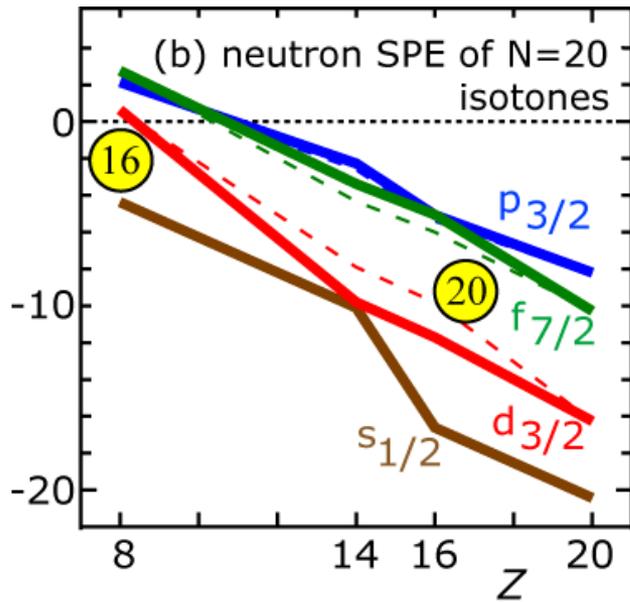
Region of Interest – Approaching the Island of Inversion



orange – nuclei studied
by us, using (d,p)

green – (a) N=20,
(b) island of inversion
(intruder structure dominates
ground state structure)

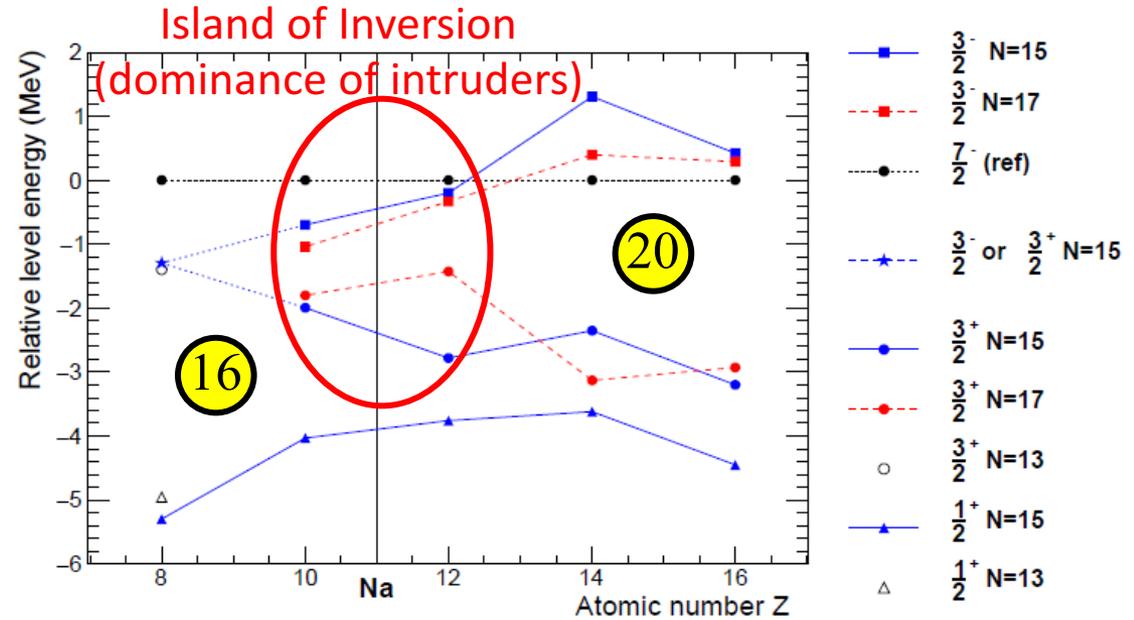
Theory: effective spe's



PRL 104, 012501 (2010)

Otsuka et al.

Experiment: energies of just the lowest levels



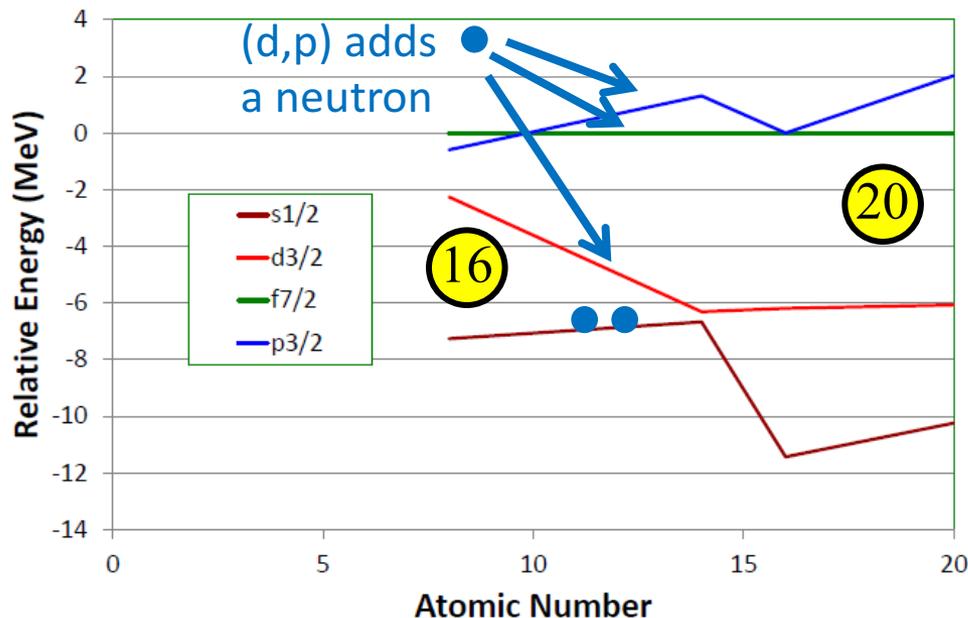
PLB (2016)

N=15 and 17 isotones

<http://dx.doi.org/10.1016/j.physletb.2016.05.093>

G.L. Wilson et al.

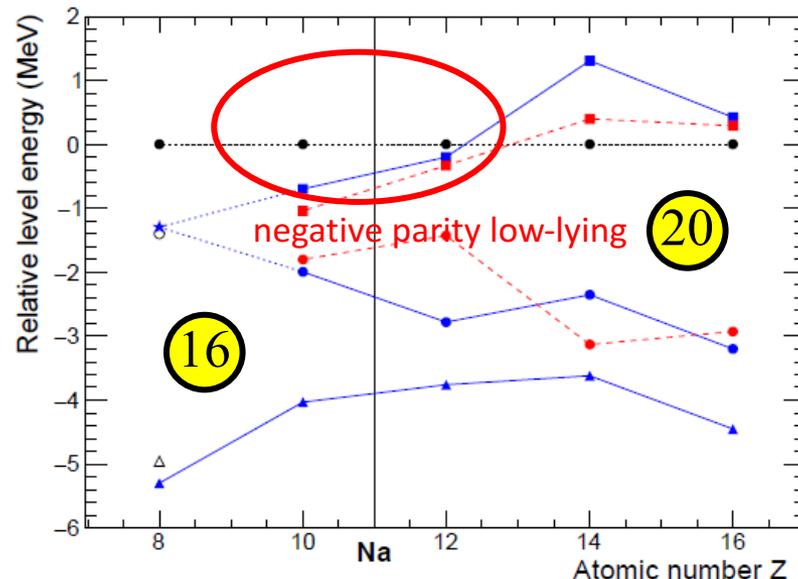
Theory: effective spe's



PRL 104, 012501 (2010)

Otsuka et al.

Experiment: energies of just the lowest levels



PLB (2016)

N=15 and 17 isotones

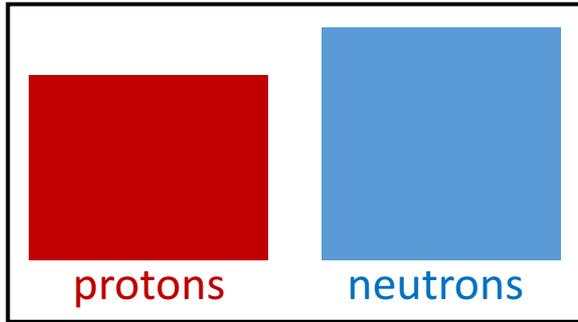
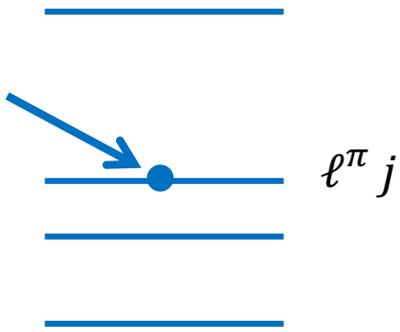
<http://dx.doi.org/10.1016/j.physletb.2016.05.093>

G.L. Wilson et al.

- Our aim is to identify single-particle-like levels and determine their spin/parity
- We use the selective nature of (d,p) neutron transfer (with radioactive beams)
- We aim to track the evolution of these levels and compare to the shell model

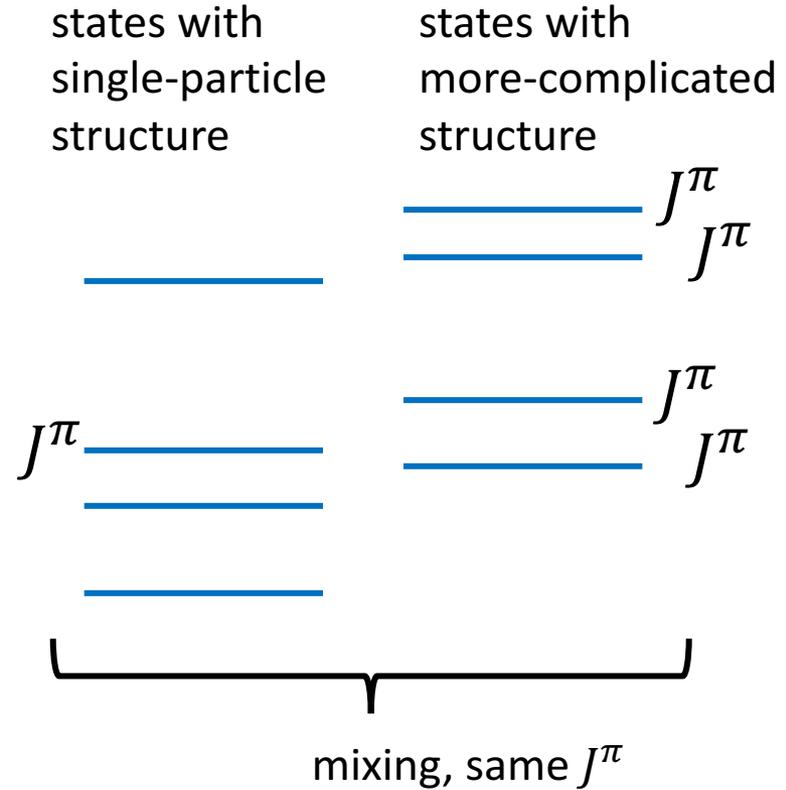
(d,p) adds a neutron

J^π



single-particle state,
unperturbed core
(idealized situation)

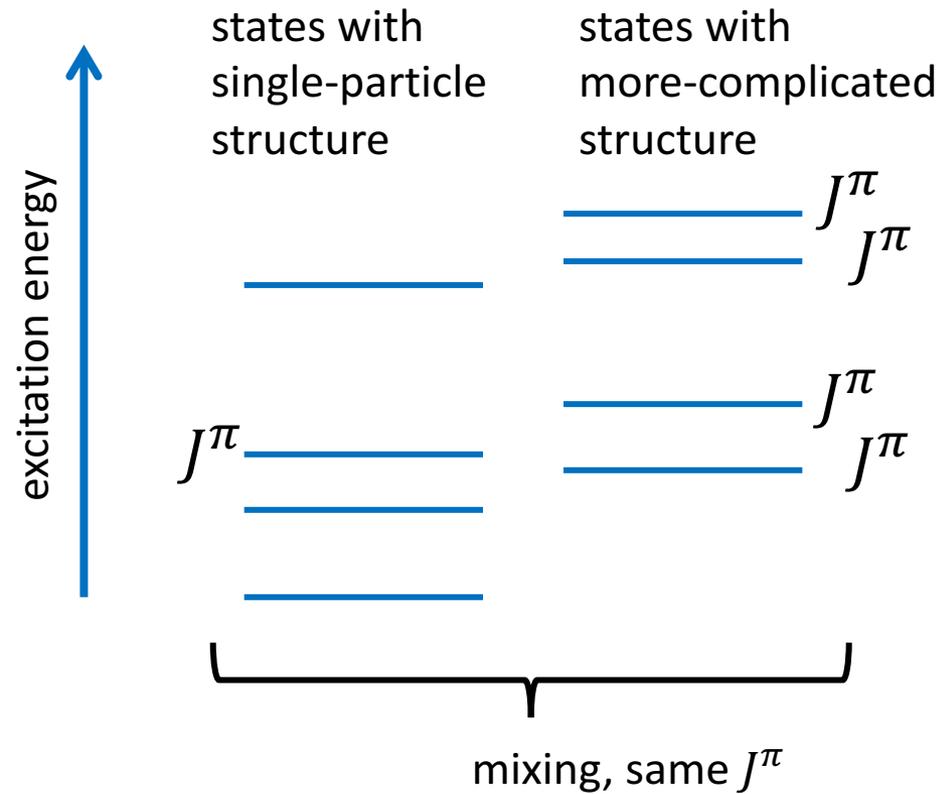
excitation energy



$$| J_i^\pi \rangle = \sqrt{S} | J_{SP}^\pi \rangle + \sum_k \alpha_k | J_k^\pi \rangle$$

$$S = | \langle J_{SP}^\pi | J_i^\pi \rangle |^2$$

spectroscopic factor
= overlap with pure SP state

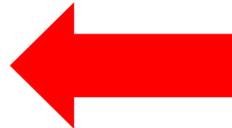


$$|J_i^\pi\rangle = \sqrt{S} |J_{SP}^\pi\rangle + \sum_k \alpha_k |J_k^\pi\rangle$$

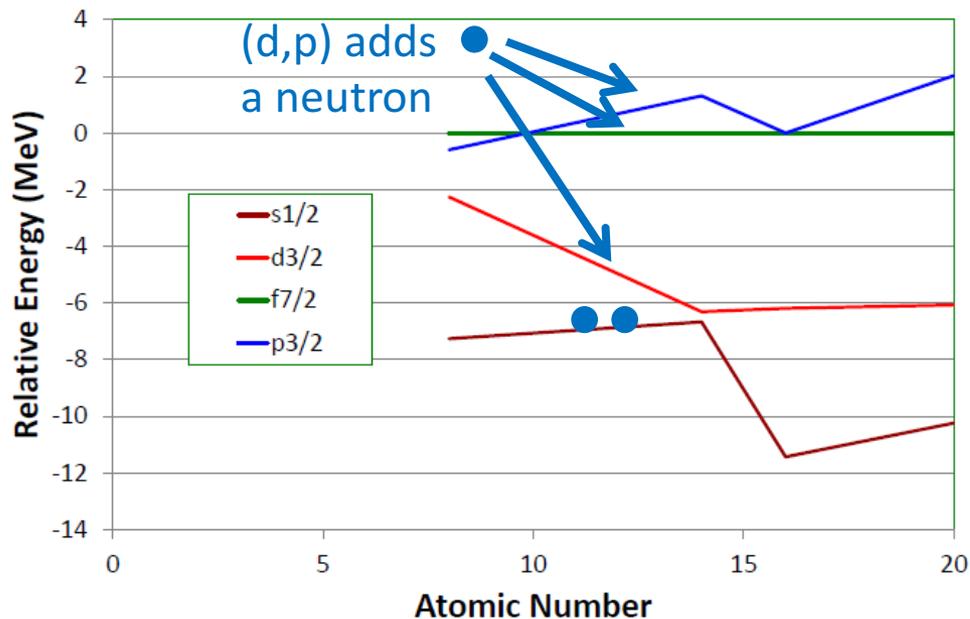
$$S = |\langle J_{SP}^\pi | J_i^\pi \rangle|^2$$

spectroscopic factor
= overlap with pure SP state

- we measure transferred ℓ_n
- we measure gamma-decays
- we aim to identify J and π
- we deduce S



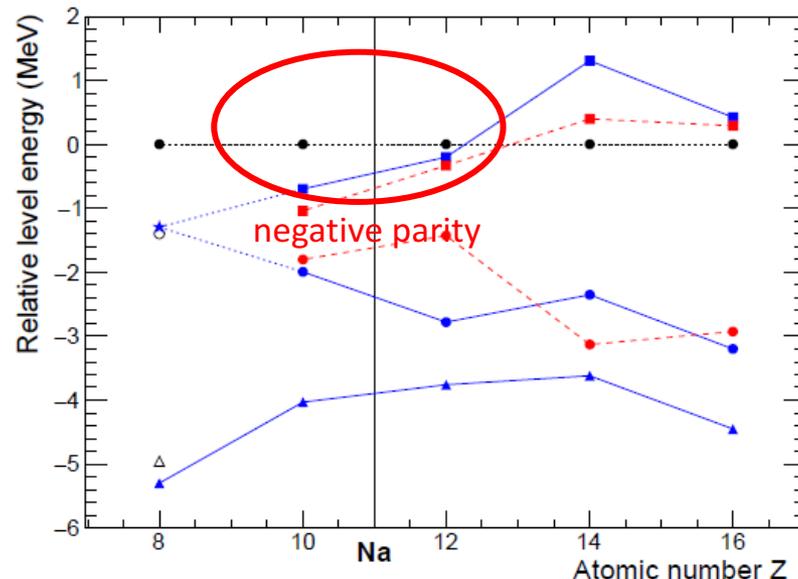
Theory: effective spe's



PRL 104, 012501 (2010)

Otsuka et al.

Experiment: energies of just the lowest levels



PLB (2016)

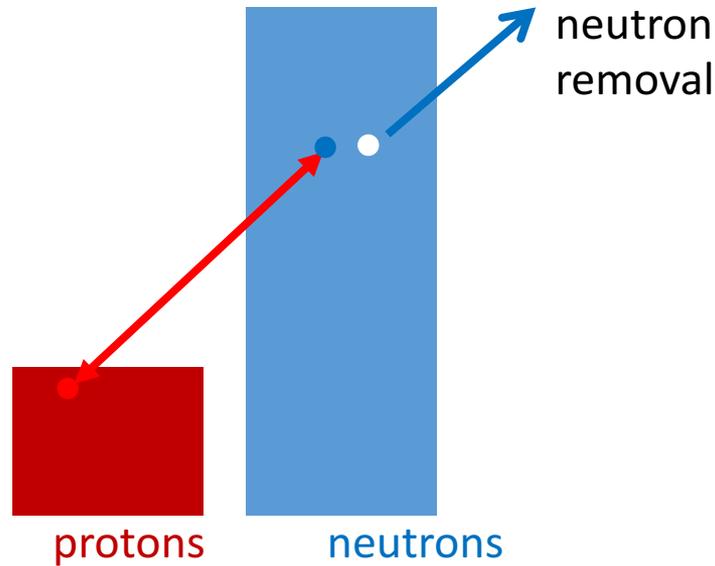
N=15 and 17 isotones

<http://dx.doi.org/10.1016/j.physletb.2016.05.093>

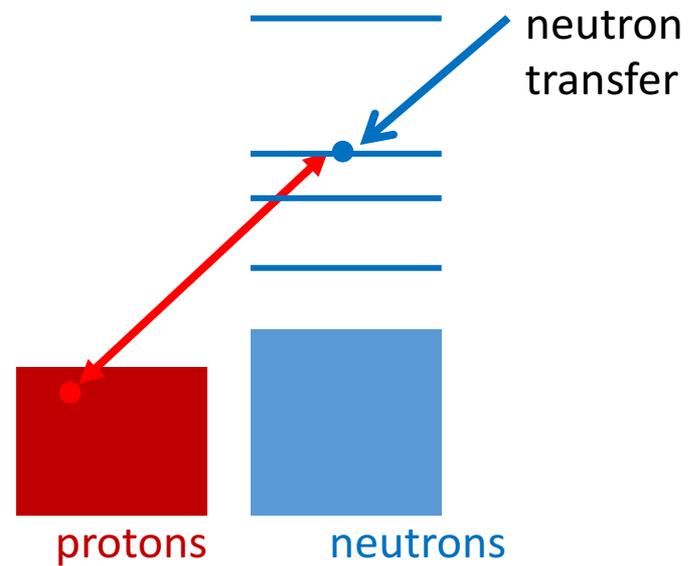
G.L. Wilson et al.

- Our aim is to identify single-particle-like levels and determine their spin/parity
- We use the selective nature of (d,p) neutron transfer (with radioactive beams)
- We aim to track the evolution of these levels and compare to the shell model
- We use the large SF for theory/experimental states to associate them with each other
- Details of the precise numerical value of the SF don't affect this process
- Results will be shown here for Z=11,12 for N=14,15,17, **probing higher orbitals**

KNOCKOUT



WHY TRANSFER IS SUCH A GOOD CHOICE

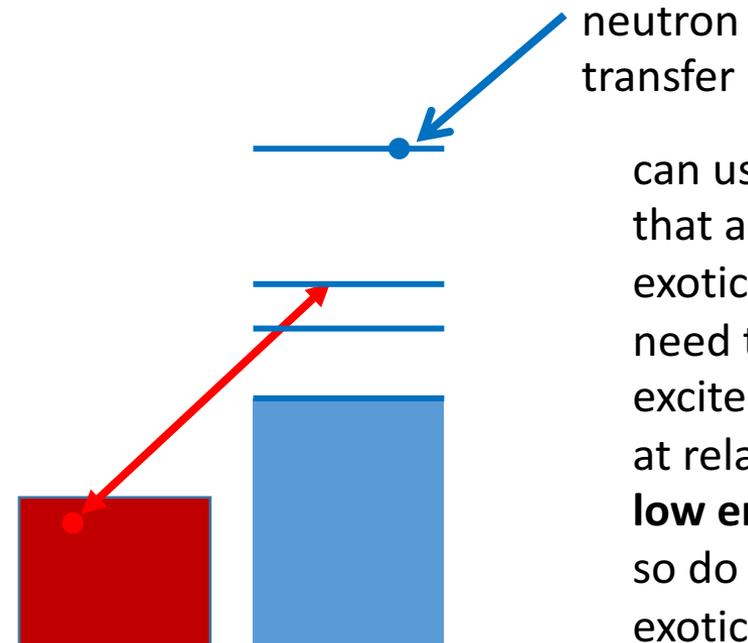


can make beams of VERY exotic nuclei
and learn properties by removing neutrons

OR

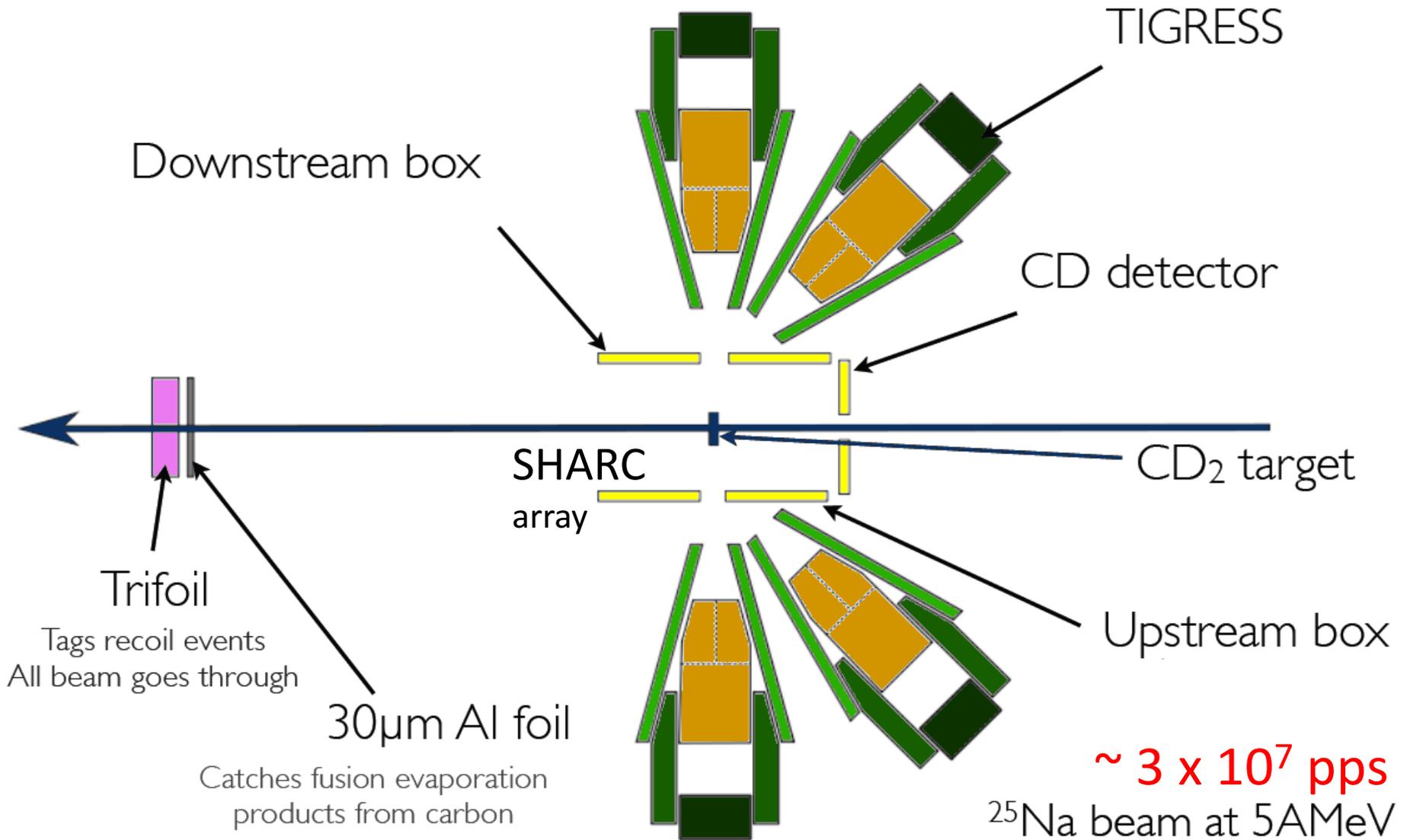
can learn the important interactions that
explain the structure by isolating p-n
interactions, using a **single nucleon** to probe
the additional orbitals one at a time

thus **transfer** is an excellent way to isolate the
separate interactions



can use beams
that are less
exotic, but do
need to keep
excited states
at relatively
low energies,
so do need
exotic beams

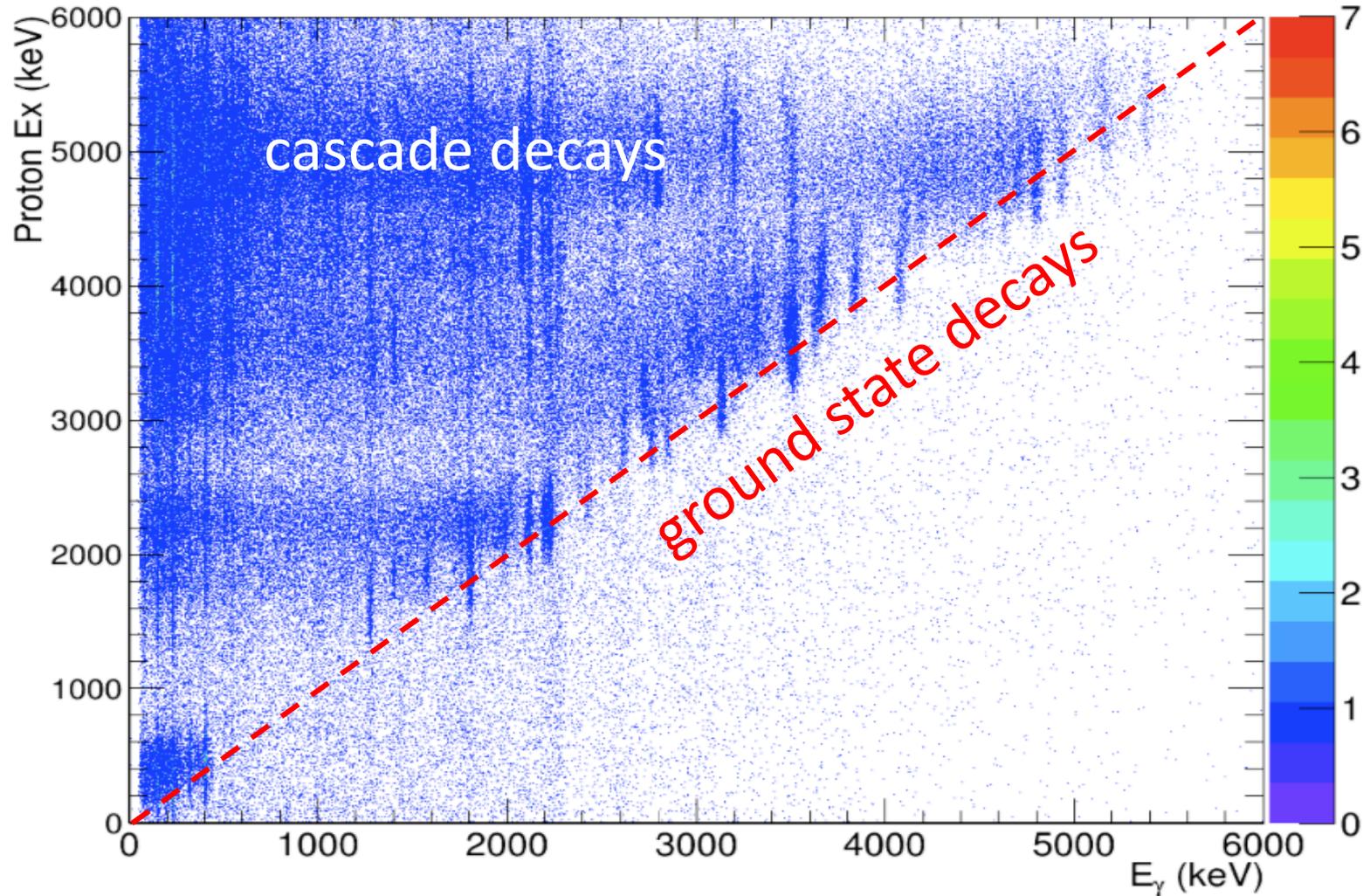
Experimental Setup to Measure $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF



Data from $d(^{25}\text{Na},p)^{26}\text{Na}$ at 5 MeV/A using SHARC at ISAC2 at TRIUMF

Gemma Wilson, Surrey

Excitation energy deduced from proton energy and angle



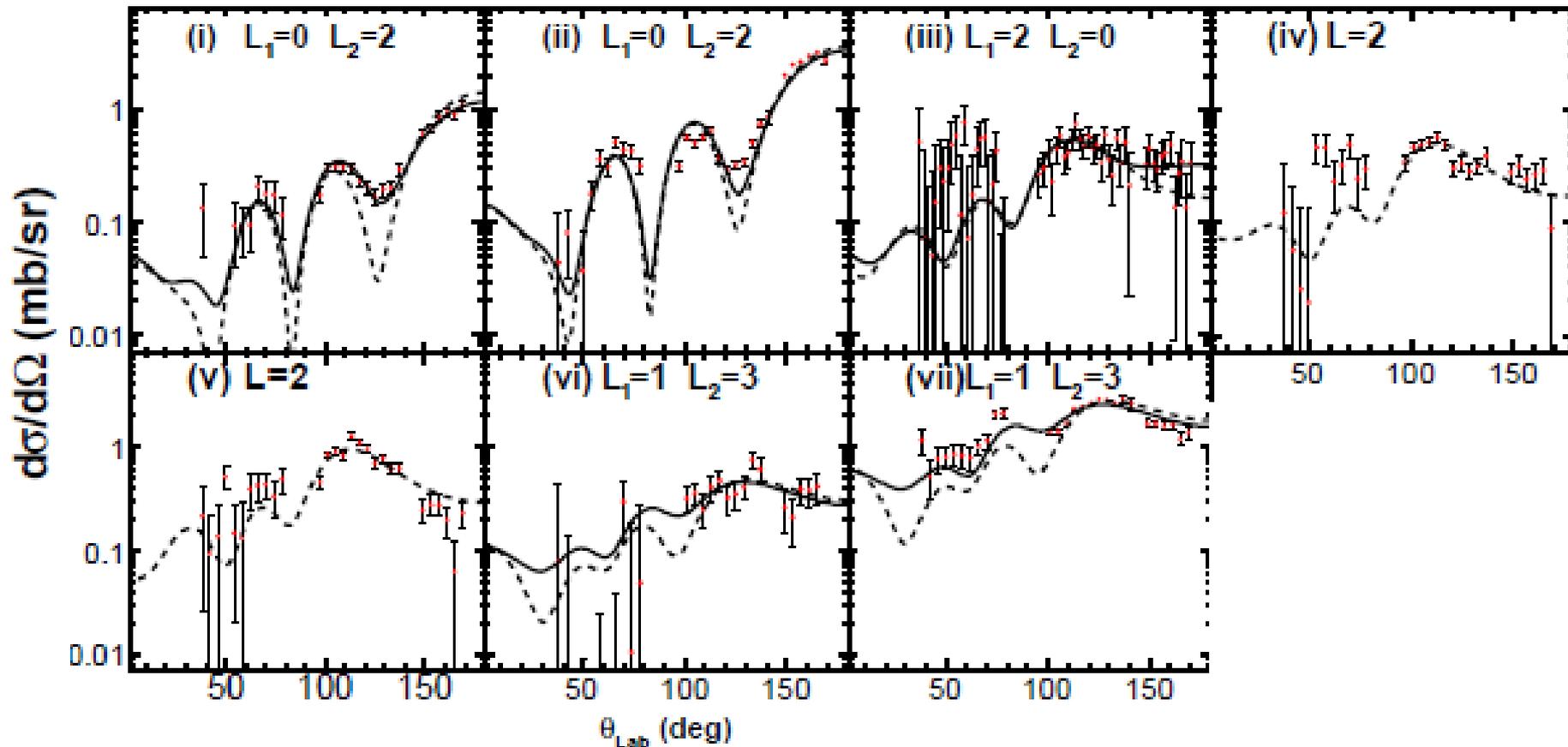
Doppler corrected ($\beta=0.10$) gamma ray energy measured in TIGRESS

Differential cross sections and spectroscopic factors

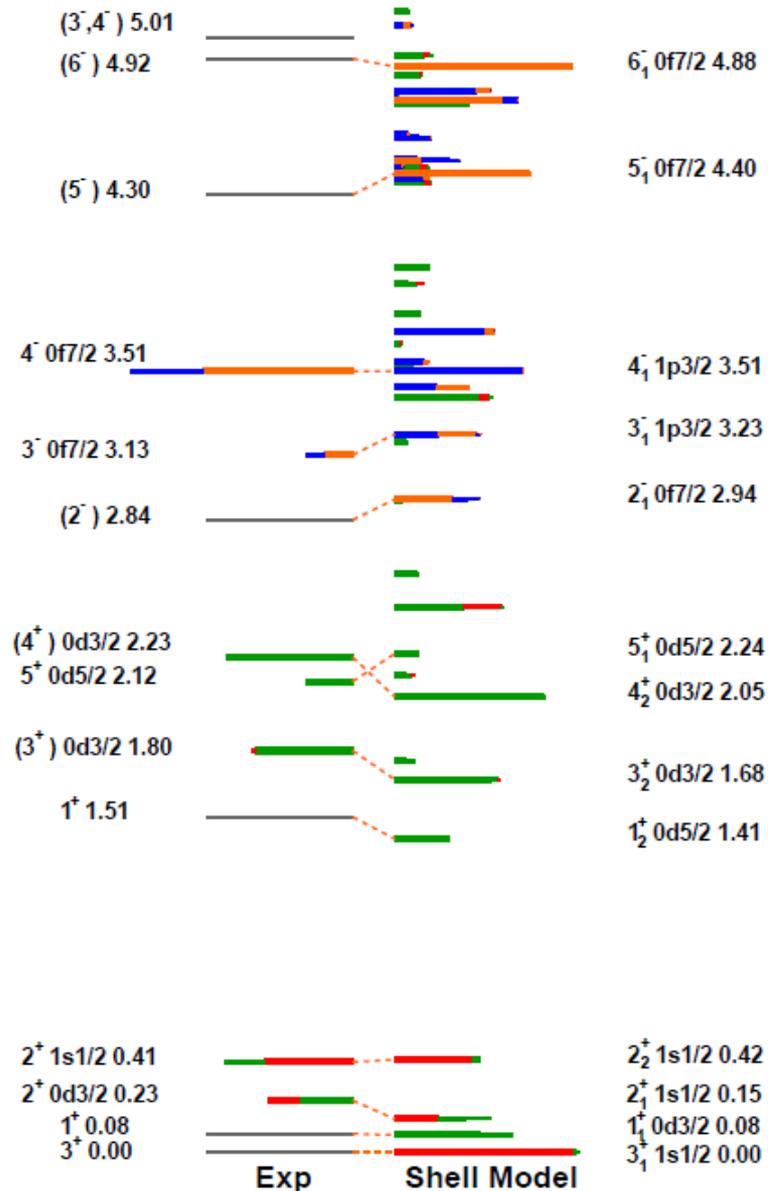
First analysis of this type:

Each of these distributions is:

- (a) gated on a gamma-ray peak
- (b) background-subtracted
- (c) corrected for gamma ray efficiency
- (d) corrected for gamma ray branching ratio



Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF



comparison between revised shell model energies and SFs

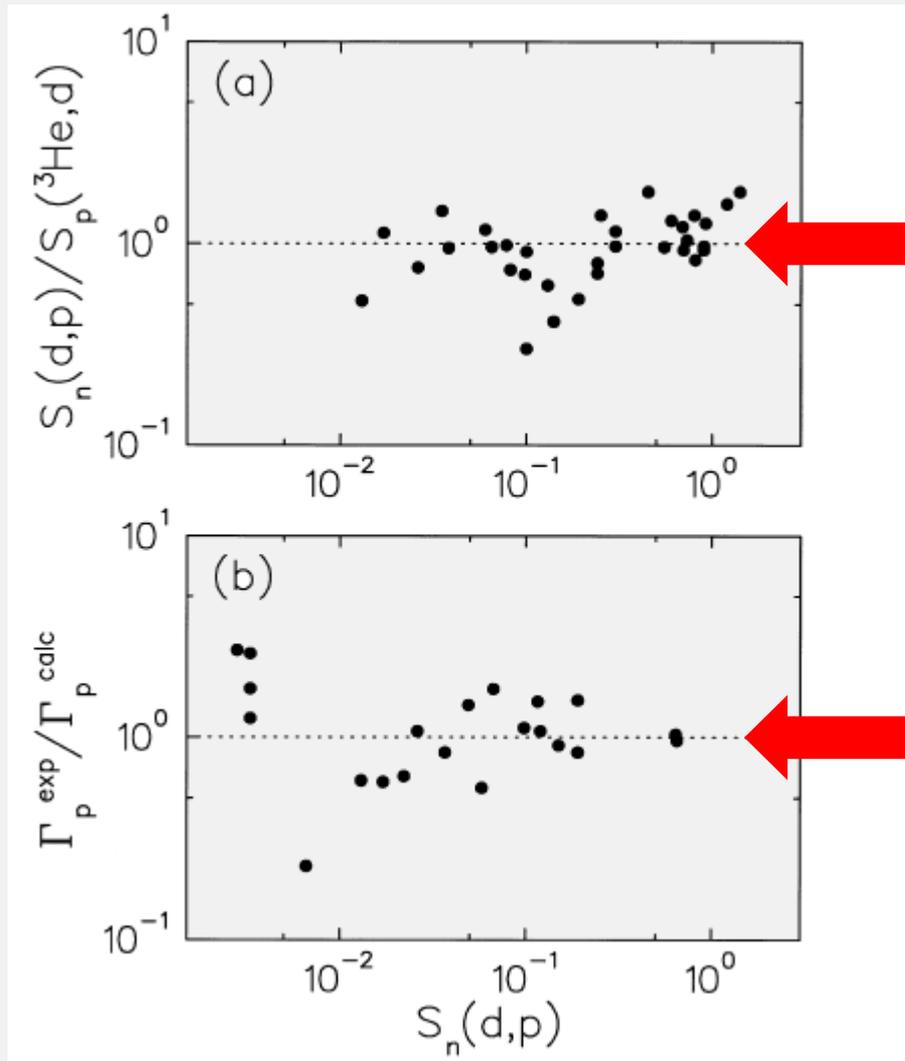
the results are somewhat subtle

evidence for stronger influence of the 1p3/2 orbital in the low-lying negative parity states, compared to the less exotic isotone ^{28}Al

this is evidence for the 1p3/2 orbital becoming lower, relative to the 0f7/2 orbital which is clear, in ^{27}Ne and ^{29}Mg

the shell model works surprisingly well
wbc spsdpf 0+1ħω

Measuring SF_n via (d,p) on n-rich conjugate $\Rightarrow \Gamma_p$ width in p-rich



strengths of states in neutron transfer
= strengths in proton transfer on mirror
within a factor of 1.5 (and a bias of 6%)

proton widths deduced from neutron
transfer strength and single-particle
decay width calculation
= actual measured proton decay width
within a factor of 1.7 (and a bias of 3%)

A=25 Isobars: ${}_{11}^{25}\text{Na}_{14}$ ${}_{14}^{25}\text{Si}_{11}$

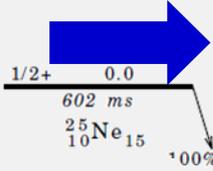
S(α) 16400¹⁴⁰⁰
S(p) 15100³⁰⁰

S(α) 9700^{SY}

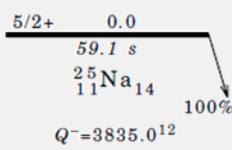
S(n) 4360¹²⁰ S(p) 16960⁸⁰



S(n) 4230³⁰ S(alpha) 11735.2²²
S(p) 10695.3¹³
S(n) 9011.0¹²



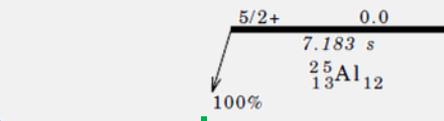
BOUND



${}^{24}\text{Na}(d,p\gamma){}^{25}\text{Na}$

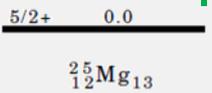
Z=11, N=14

S(p) 12063.68⁸
S(alpha) 9885.97⁵
S(n) 7330.58³



mirror

mirror



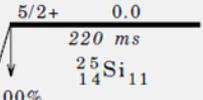
S(n) 15002²² (1/2+) 0.0
<30 ns
 ${}_{15}^{25}\text{P}_{10}$

S(alpha) 9511¹⁹
Q+ = 15050^{SY}

S(n) 16931³



UNBOUND

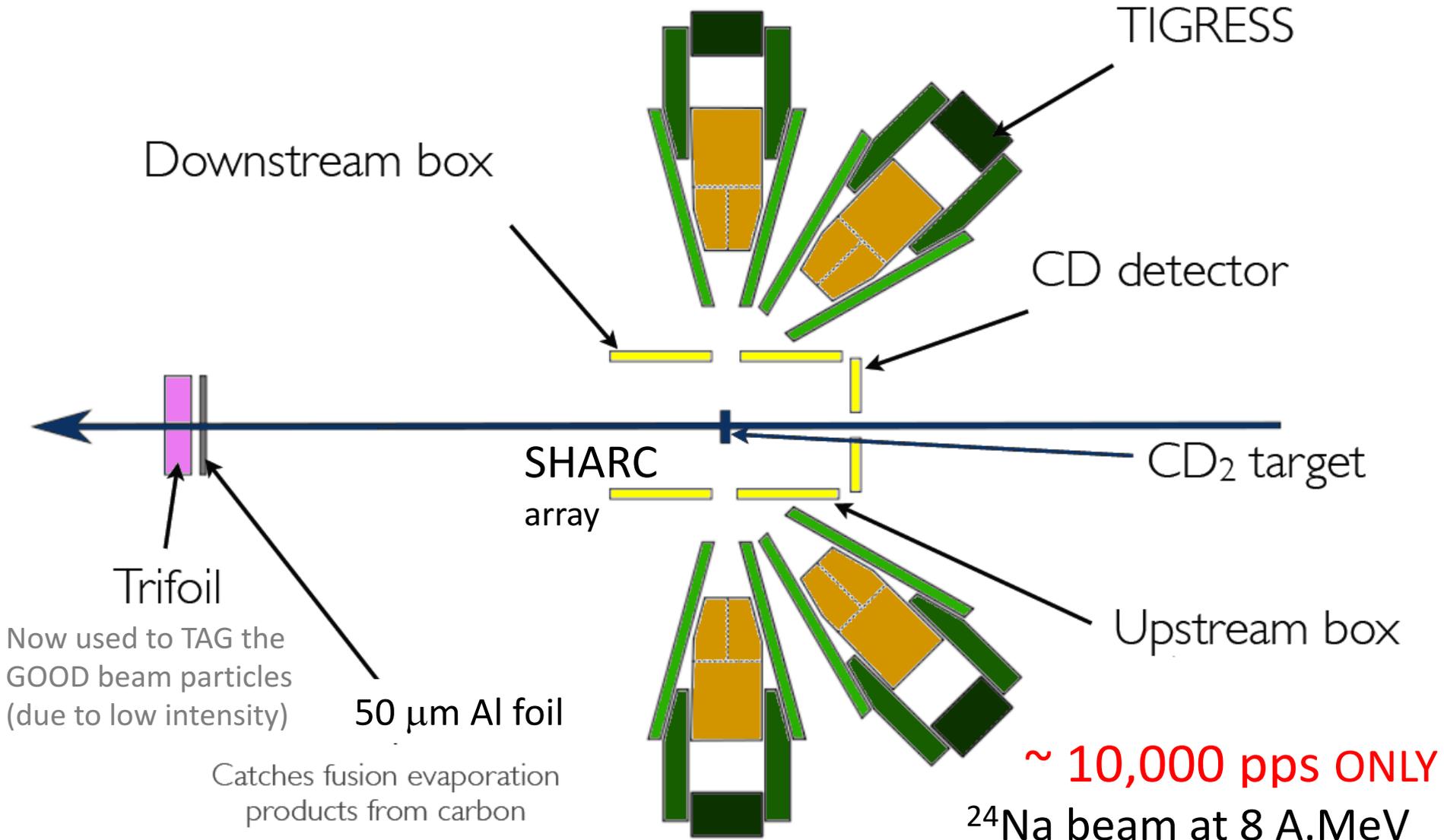


${}^{24}\text{Al}(p,\gamma){}^{25}\text{Si}$

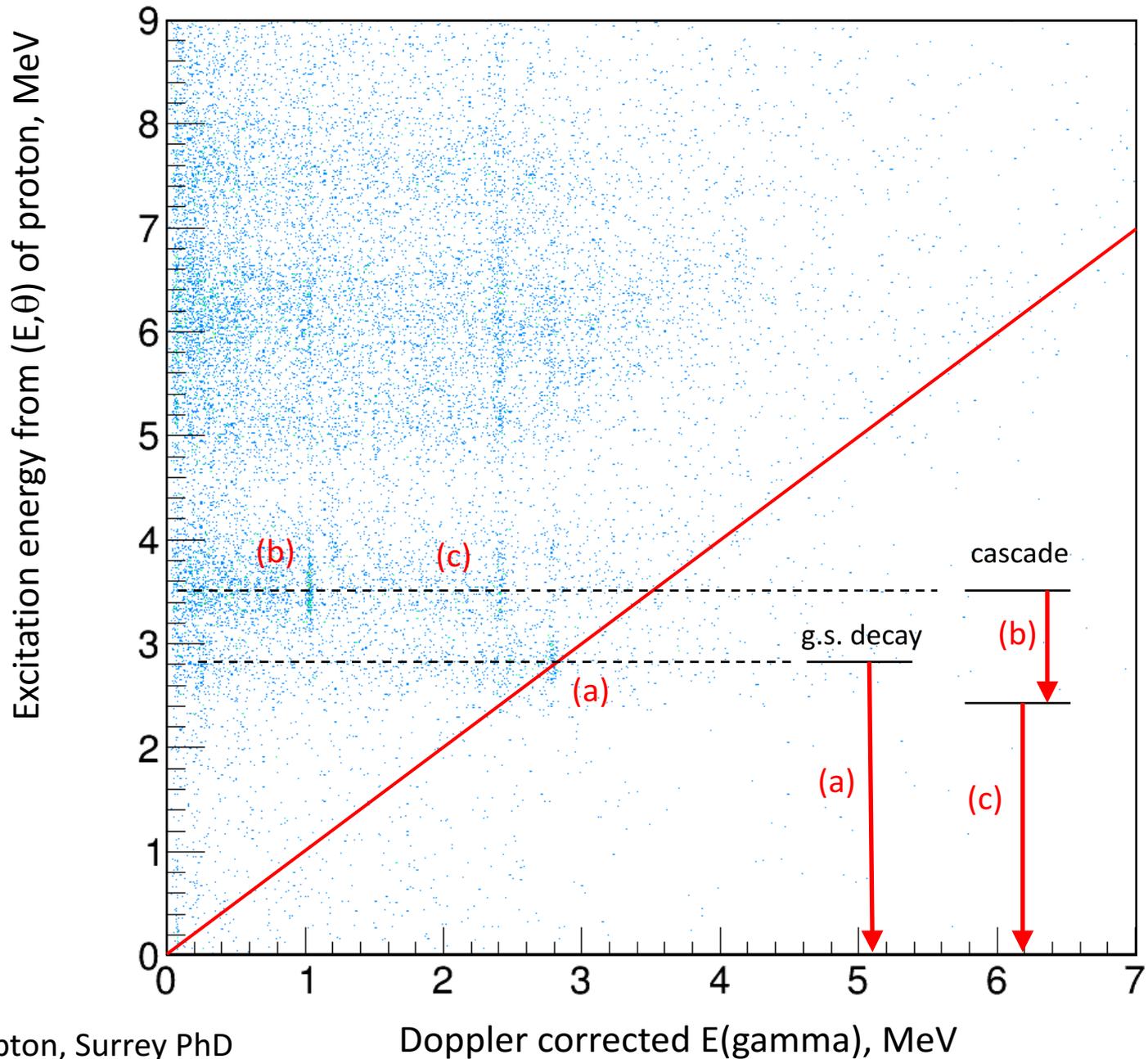
Z=14, N=11

Experimental Setup to Measure $d(^{24}\text{Na}, p)^{25}\text{Na}$ at TRIUMF

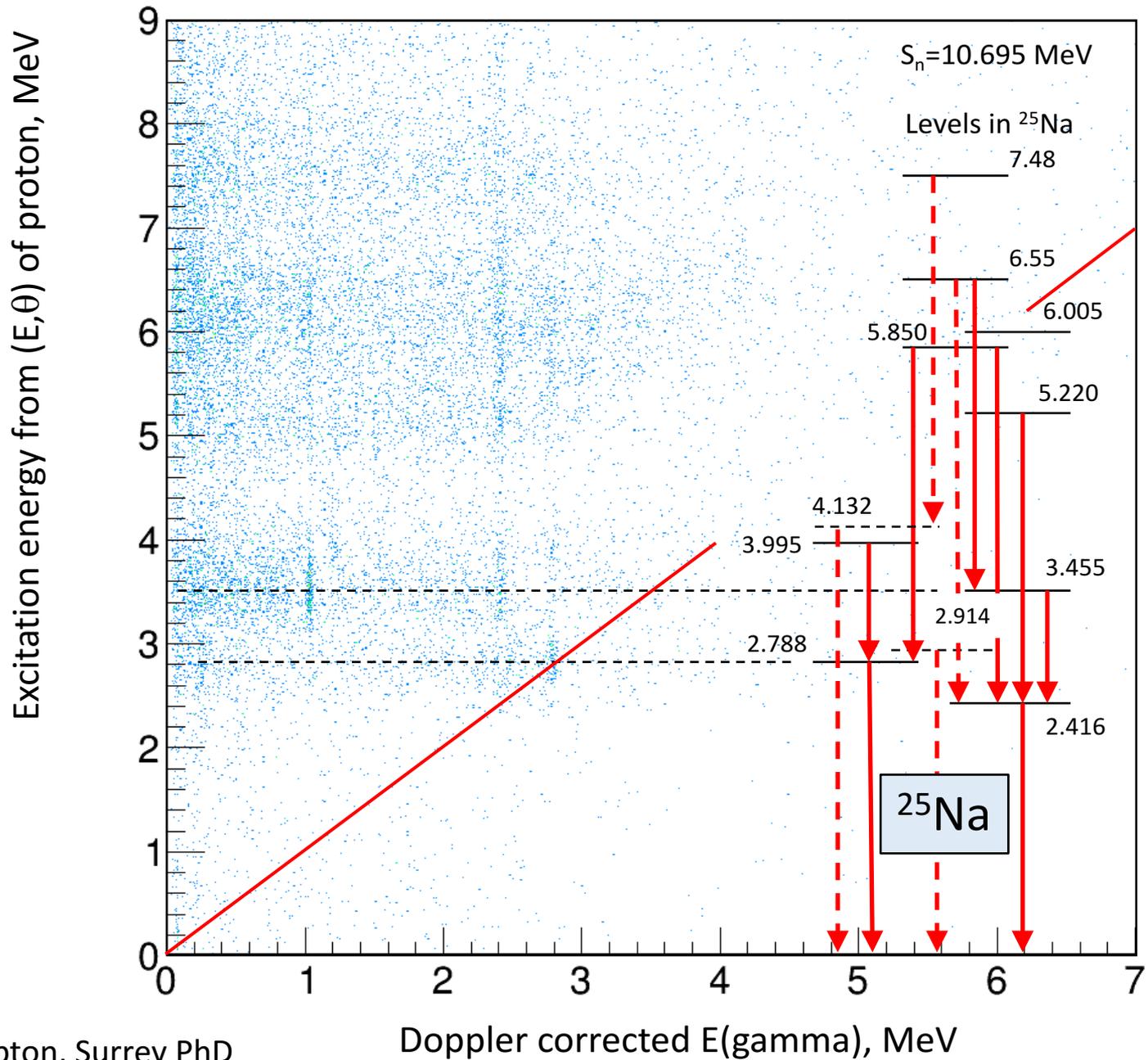
conjugate of $^{24}\text{Al}(p, \gamma)^{25}\text{Si}$



$d(^{24}\text{Na}, p)^{25}\text{Na}$ at 8.0 MeV/u with 10,000 pps

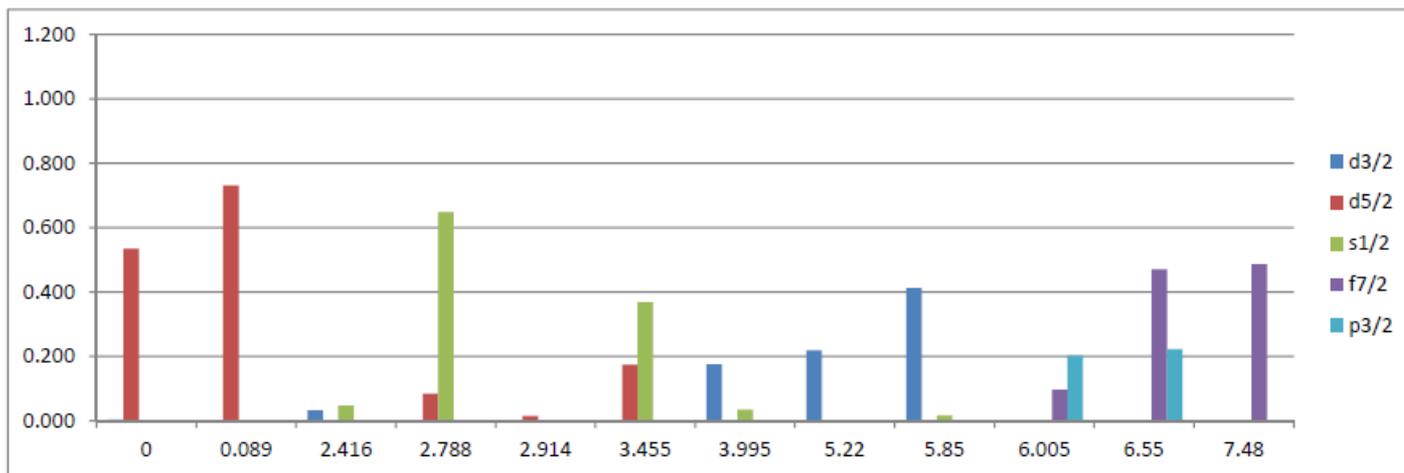


$d(^{24}\text{Na},p)^{25}\text{Na}$ at 8.0 MeV/u with 10,000 pps

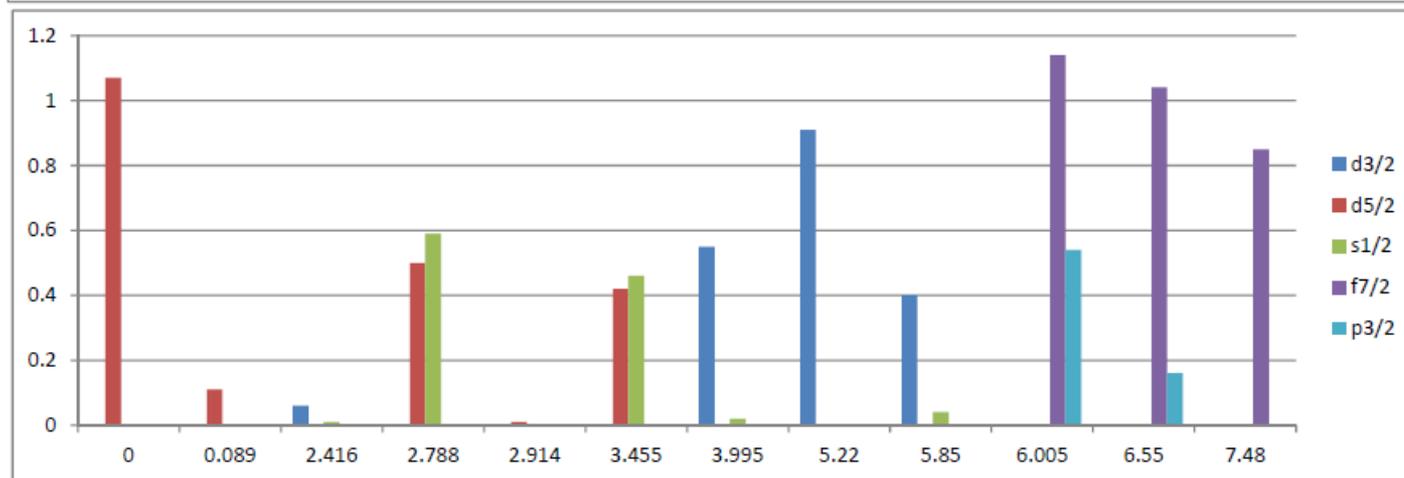


$d(^{24}\text{Na},p)^{25}\text{Na}$ – spectroscopic factors in ^{25}Na compared to theory

wbc
nushellx
(0+1) $\hbar\omega$



this work
ADWA
std geom

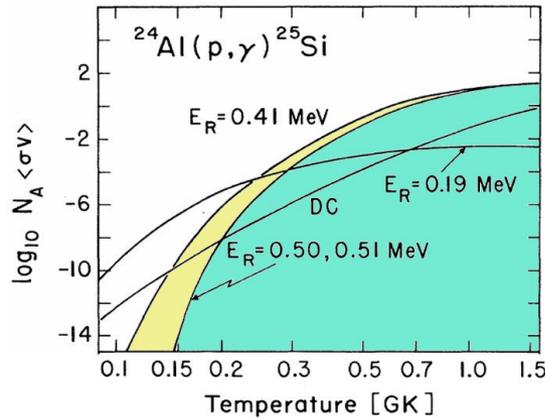


Excitation Energy in ^{25}Na (MeV)

present work	5/2+	3/2+	9/2+	7/2+	5/2+	9/2+	9/2+	11/2+	7/2+	7/2-	11/2-	13/2-
literature	5/2+	3/2+	?	3/2	5/2+	3/2+?	1/2-	?	?	(1/2, 3/2)-	?	?

BIG IMPROVEMENTS IN LEVEL IDENTIFICATIONS

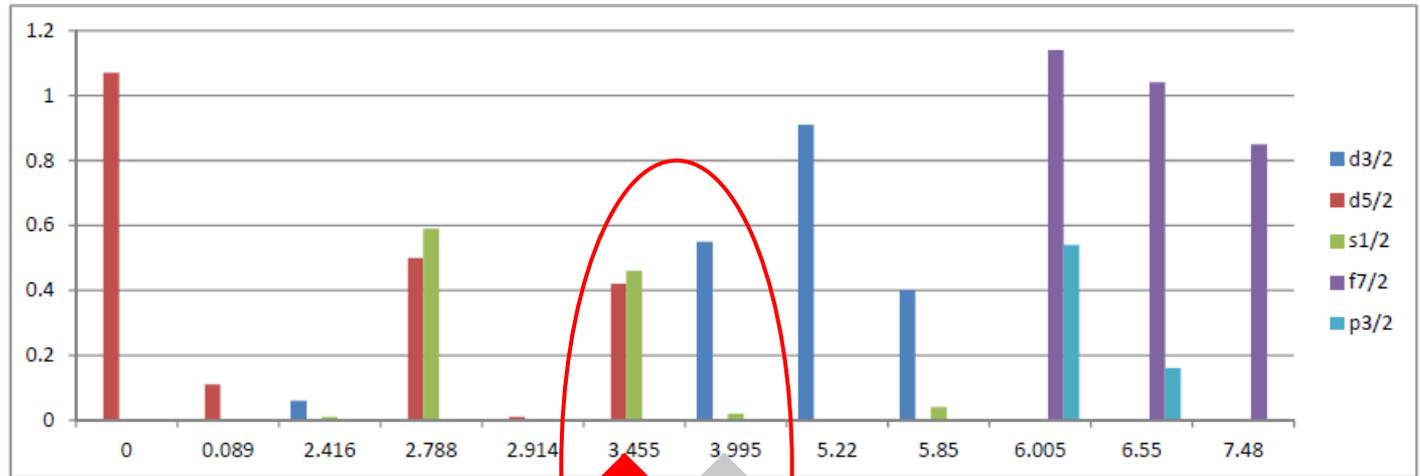
Using the ^{25}Na SFs to calculate $^{24}\text{Al}(p,\gamma)^{25}\text{Si}$ widths and $\omega\gamma$'s for novae



Wiescher, Brown PRC52, 1078 (1995)
revised the rate for $^{24}\text{Al}(p,\gamma)$ upwards $\times 100$

\longrightarrow $0.41 = 3.995$ in ^{25}Na
resonance states in ^{25}Si
 \longrightarrow $0.02 = 3.455$ in ^{25}Na
 (not considered important before,
 due to misidentification)

this work
ADWA
std geom



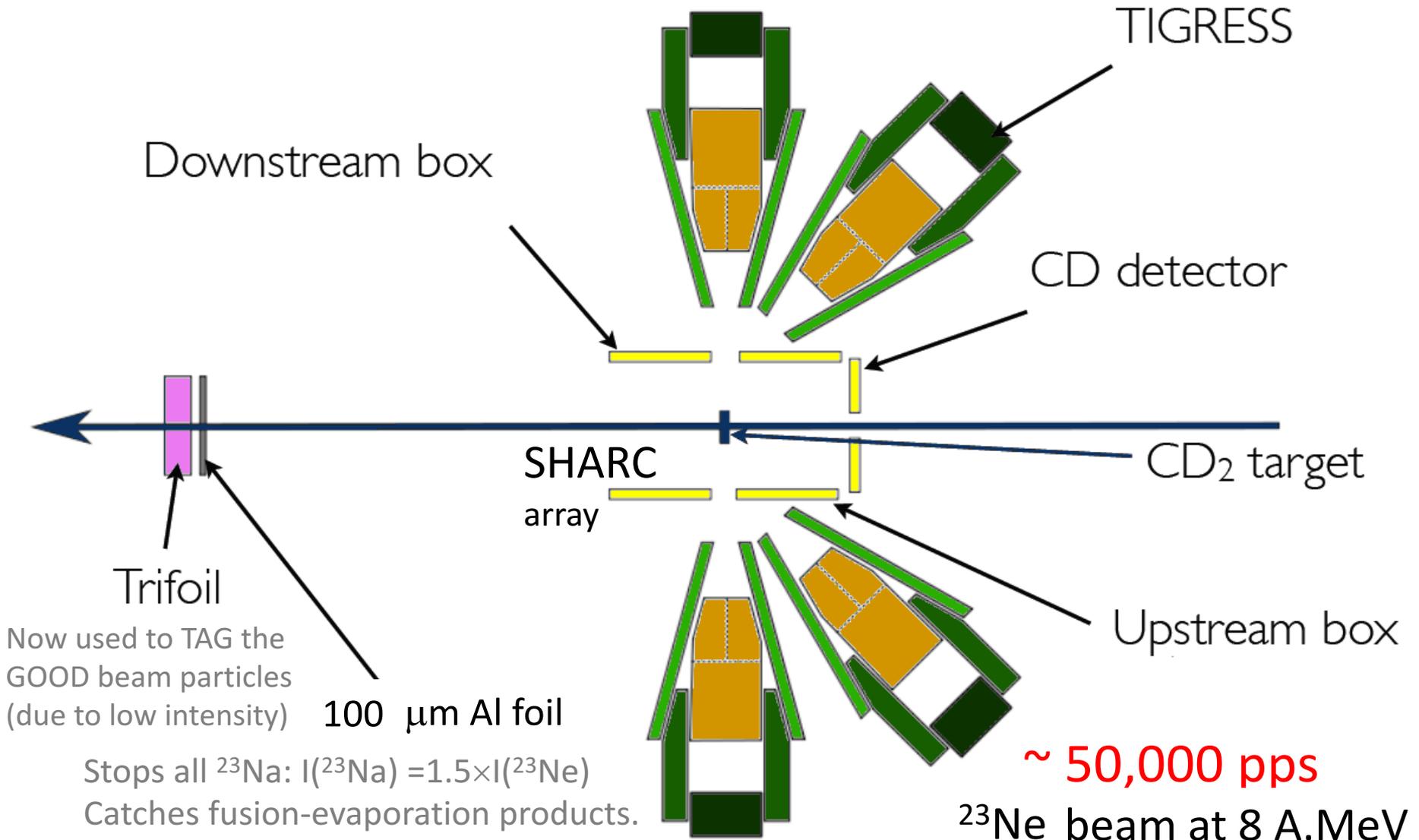
Excitation Energy in ^{25}Na (MeV)

present work	5/2+	3/2+	9/2+	7/2+	5/2+	9/2+	9/2+	11/2+	7/2+	7/2-	11/2-	13/2-
literature	5/2+	3/2+	?	3/2	5/2+	3/2+?	1/2-	?	?	(1/2, 3/2)-	?	?

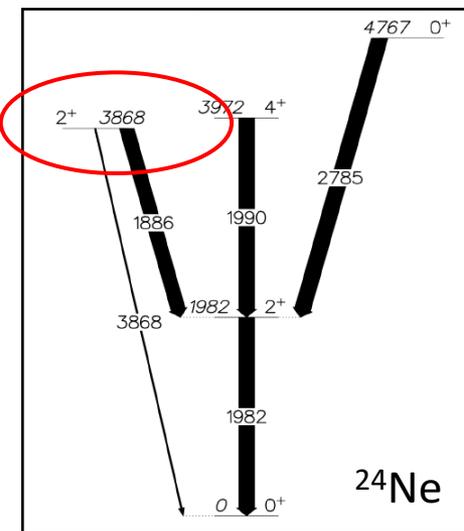
bound states in mirror ^{25}Na

Experimental Setup to Measure $d(^{23}\text{Ne}, p)^{24}\text{Ne}$ at TRIUMF

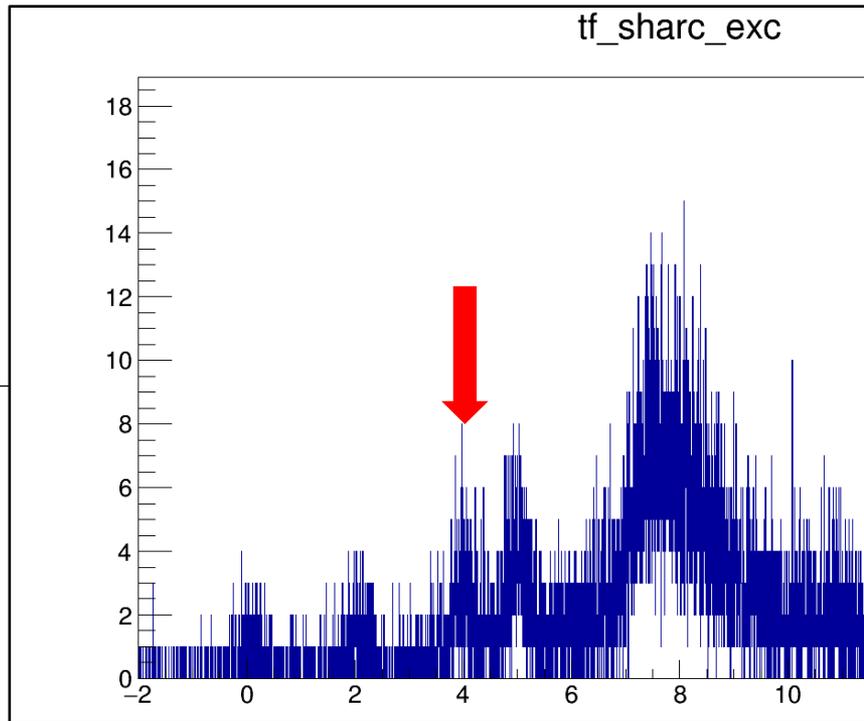
conjugate of $^{23}\text{Al}(p, \gamma)^{24}\text{Si}$



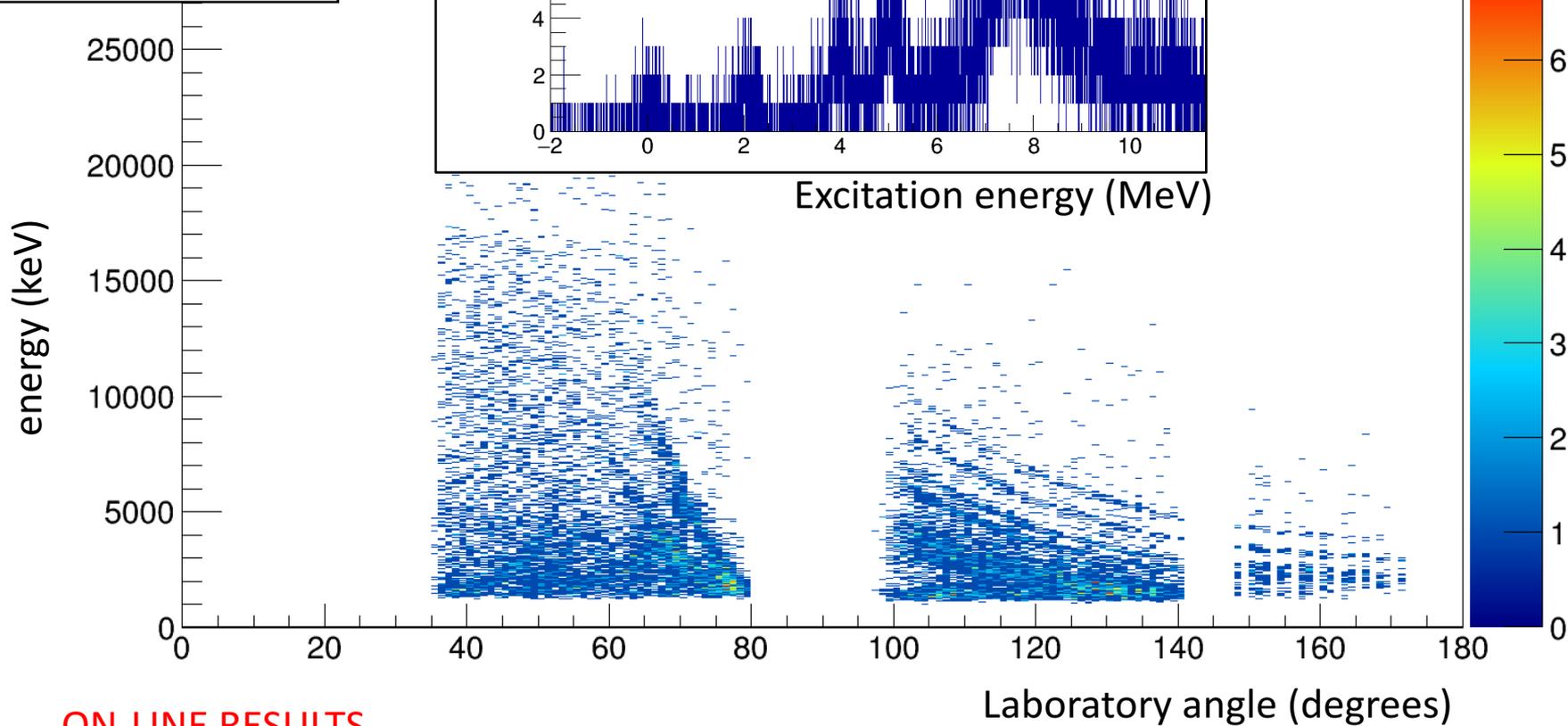
$d(^{23}\text{Ne},p)^{24}\text{Ne}$



counts



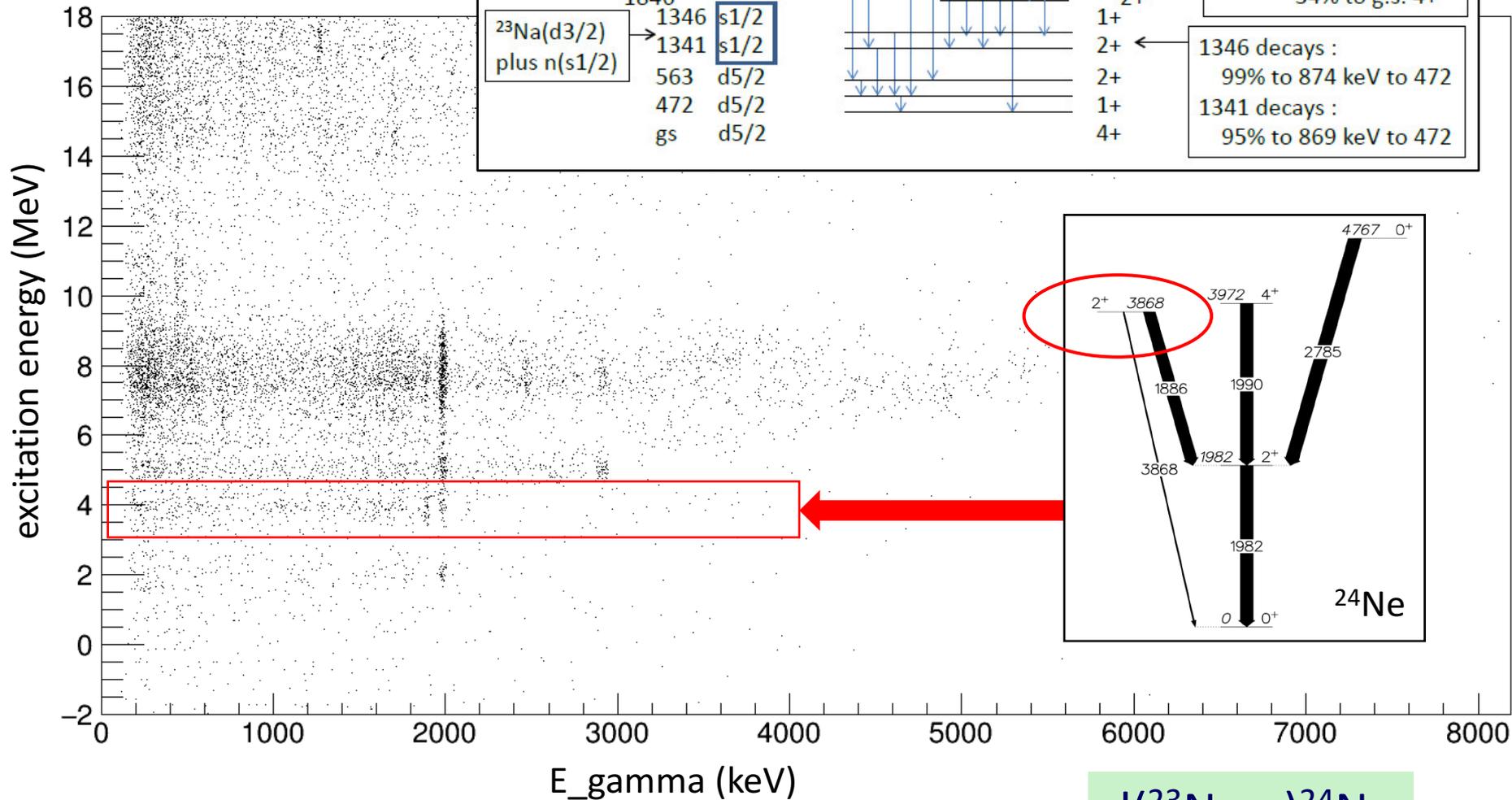
Excitation energy (MeV)



ON-LINE RESULTS

Laboratory angle (degrees)

- The ^{24}Na gamma-rays are eliminated.
- The ^{24}Ne gamma-rays indicate that ONLY the state of interest is made.



6306	d5/2	(2,3,4)+	
6257	f7/2	(1,2)-	
5180	f7/2	(1,2,3)-	
4187	d5/2	2+	
3977	3745	p3/2	3- 1-,2+
3628	d3/2	3+	
3371	p3/2	2-	
2978	d3/2	2+	
1885	1846	2+	
1346	s1/2	3+	
1341	s1/2	1+	
563	d5/2	2+	
472	d5/2	2+	
gs	d5/2	1+	
		4+	

decays of 5180 seem to include 5180, 2300, 1180

details of 3628 decays :
 19% to 1345 3+
 47% to 1341 2+
 34% to g.s. 4+

1346 decays :
 99% to 874 keV to 472
 1341 decays :
 95% to 869 keV to 472

ON-LINE RESULTS

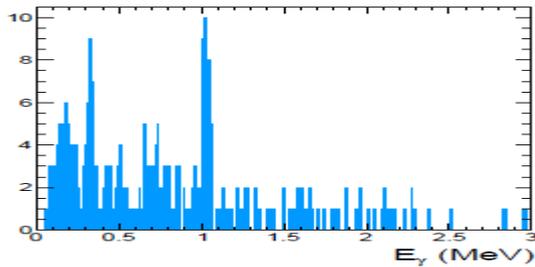
$d(^{23}\text{Ne},p)^{24}\text{Ne}$

$d(^{28}\text{Mg},p)^{25}\text{Na}$ at 8.0 MeV/u with 3,000 pps

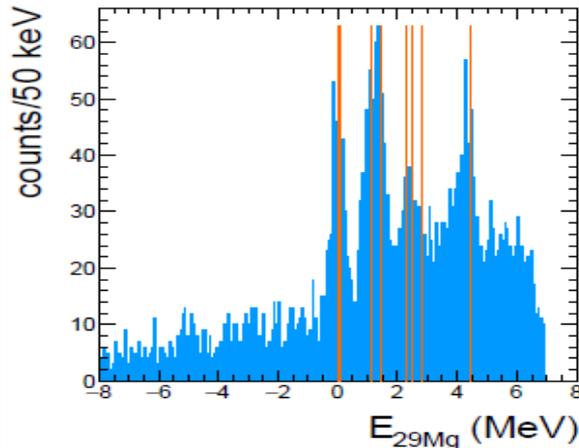
Secondary Beam

- ^{28}Mg beam 3000 pps at 8 AMeV
- With strong contamination
- ^{28}Si cont. ($3 \cdot 10^5$ pps)
- ^{28}Al cont. (300 pps)

Gated E_γ

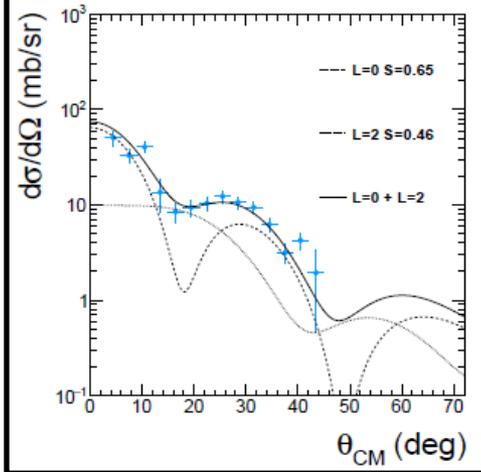


Gated Excitation Energy

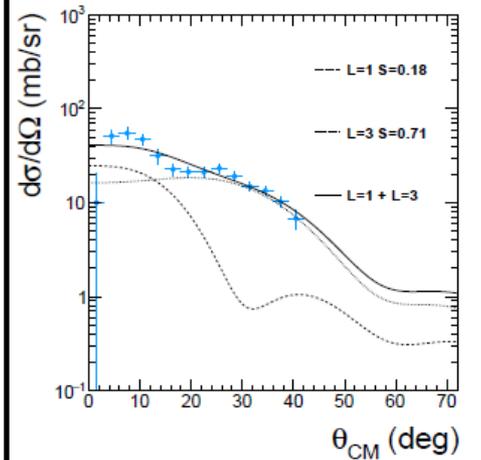


Experiment – SHARC and TIGRESS at TRIUMF

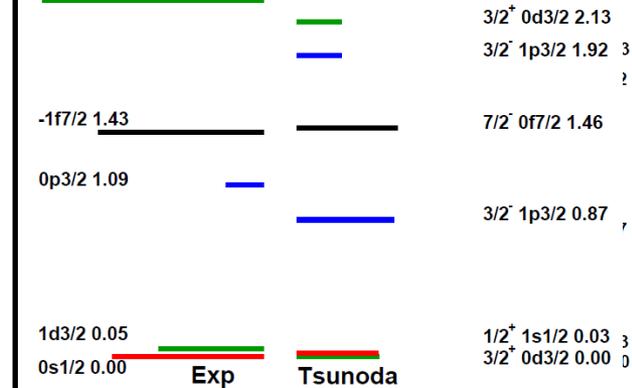
Ground State Doublet



1 MeV Doublet



Microscopic Shell Model

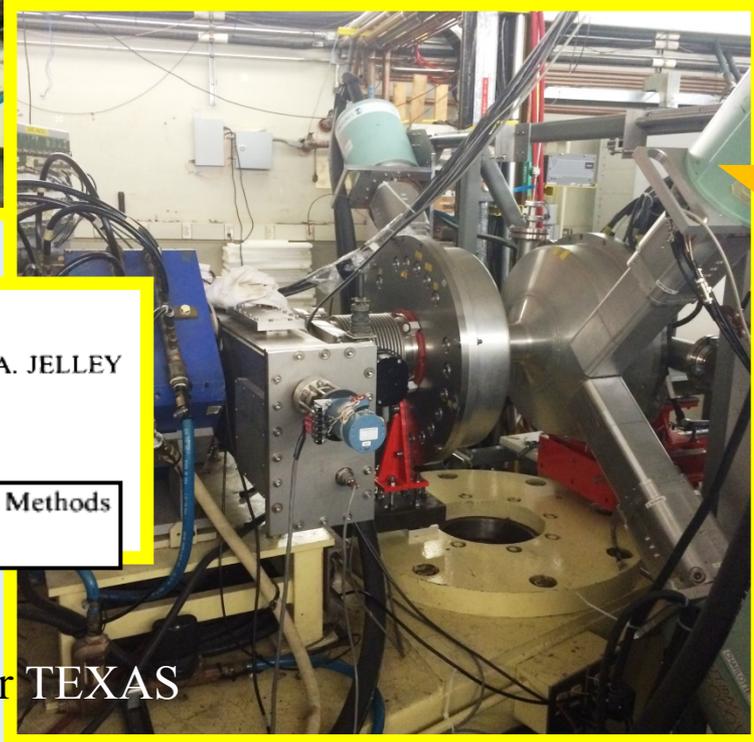
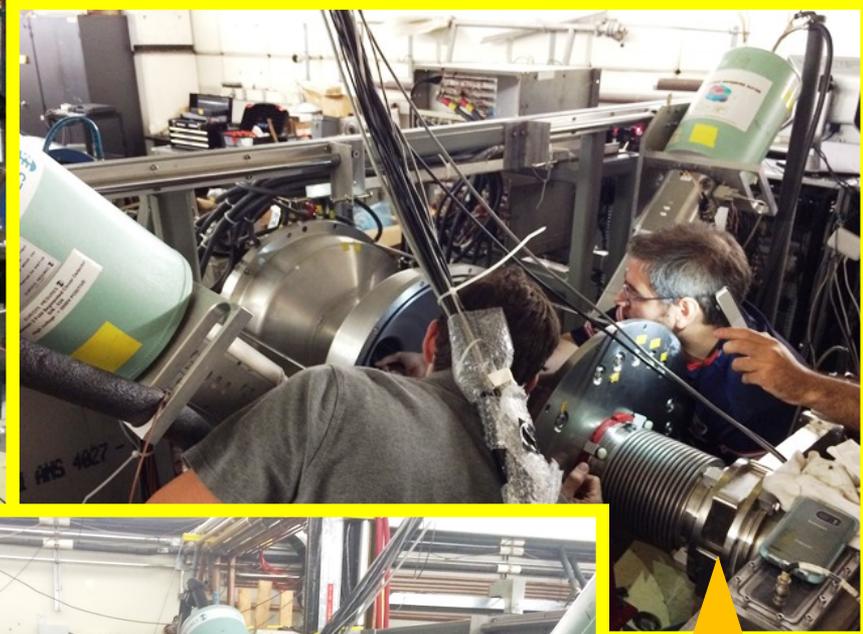
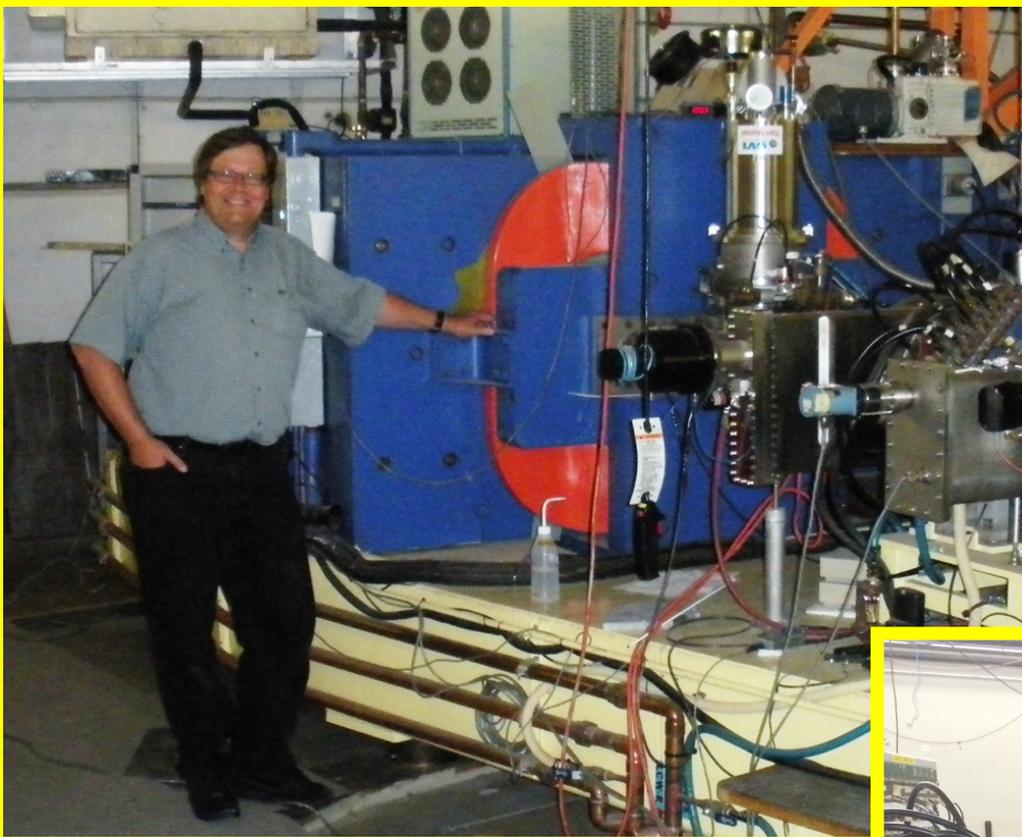


We have preliminary results from this experiment using a heavily contaminated beam.

New shell model calculations with realistic interactions and expanded sd-pf model space... Tsunoda, Otsuka EEdf1 (EKK)

Too early to judge agreement.

Texas A&M– radioactive beams using gas catcher and cyclotron reacceleration



installed,
first run
Aug 2016

zero-degree detection using Oxford MDM

THE OXFORD MDM-2 MAGNETIC SPECTROMETER

D.M. PRINGLE, W.N. CATFORD *, J.S. WINFIELD **, D.G. LEWIS, N.A. JELLEY
and K.W. ALLEN

University of Oxford, Nuclear Physics Laboratory, Keble Road, Oxford, England

J.H. COUPLAND

Rutherford Appleton Laboratory, Chilton, Didcot, England

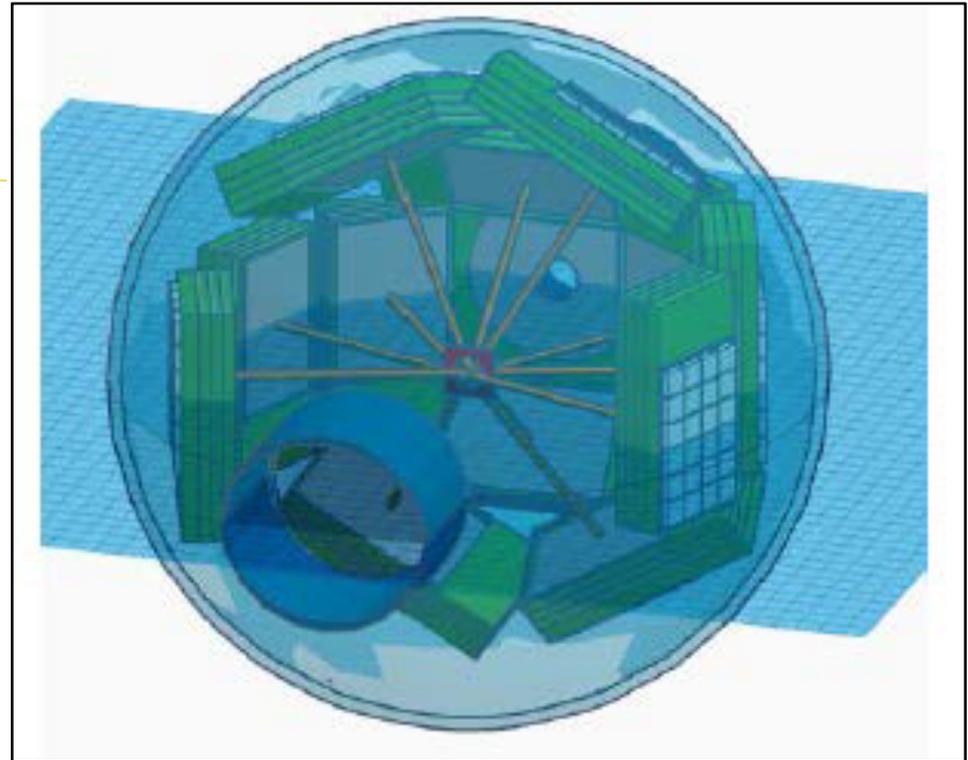
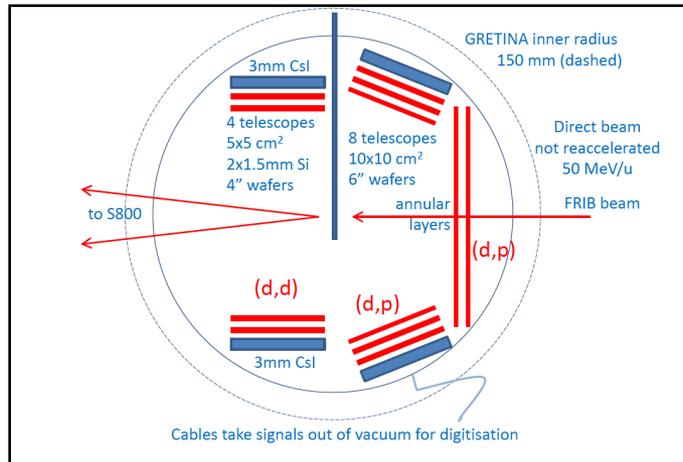
**Nuclear Instruments and Methods
A245 (1986) 230**



TIARA  for TEXAS



DIRECT REACTION ARRAY



- Propose to develop a new array consisting of silicon telescopes and annular detectors to cover light-particle emission angles, in front of the S800 spectrometer
- Detectors backed with CsI in order to provide adequate stopping for high-energy particles – exploit direct in-flight beam at 30-50 MeV/u.
- Placed inside GRETA gamma-ray tracking array
- Large number of channels (~1500) instrumented with 300 MHz digital electronics

Summary

- We found that just outside the borders of the island of inversion, the shell model that was adapted for the island (i.e. USD-A, wbc) seems to work reasonably well – we have very useful discussions with those developing the new EEdf1 interaction
- Even in some less exotic nuclei, the selectivity of (d,p) has been shown to be hugely powerful in identifying the most interesting states (for the first time) e.g. ^{25}Na , and WE STUDY THE SAME orbitals and physics as in much more exotic nuclei.
- The relatively new technique of gating on the coincident gamma rays to separate states that are not otherwise resolved has worked well
- We are edging closer towards the island of inversion to test the shell model further and improve it, and have plans to move attention to the second island of inversion
- We are preparing for new availability of beams at Texas A&M (also HIE-ISOLDE and MUGAST at GANIL and hopefully DRACULA at FRIB)

COLLABORATORS FOR THIS WORK

In Surrey:

Gavin Lotay, Dan Doherty, Mhd Moukaddam,
Adrien Matta (LPC Caen), Ryan Wilkinson, Sam Hallam,
Gemma Wilson, Andy Knapton, Ilker Can Celik

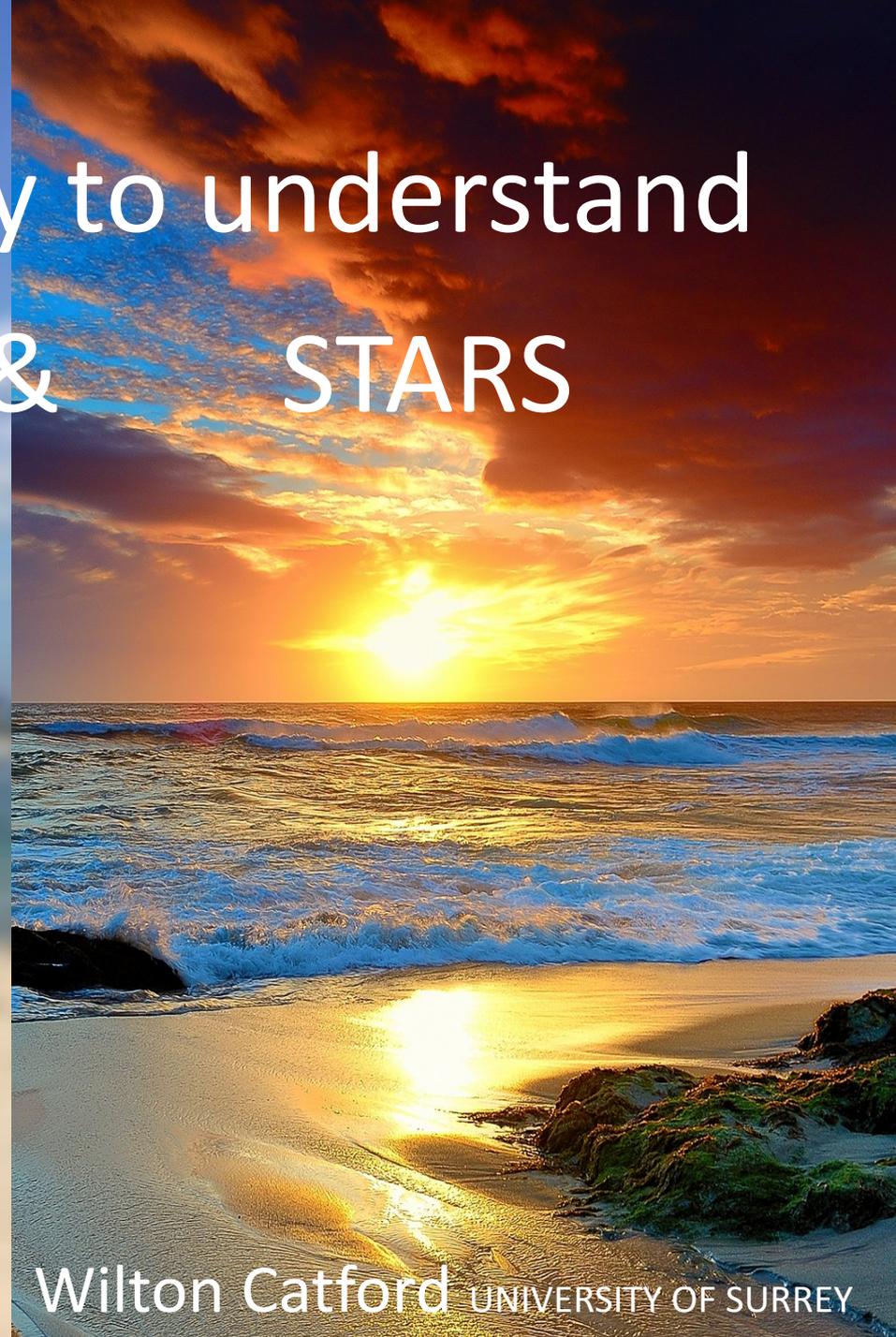
In TRIUMF:

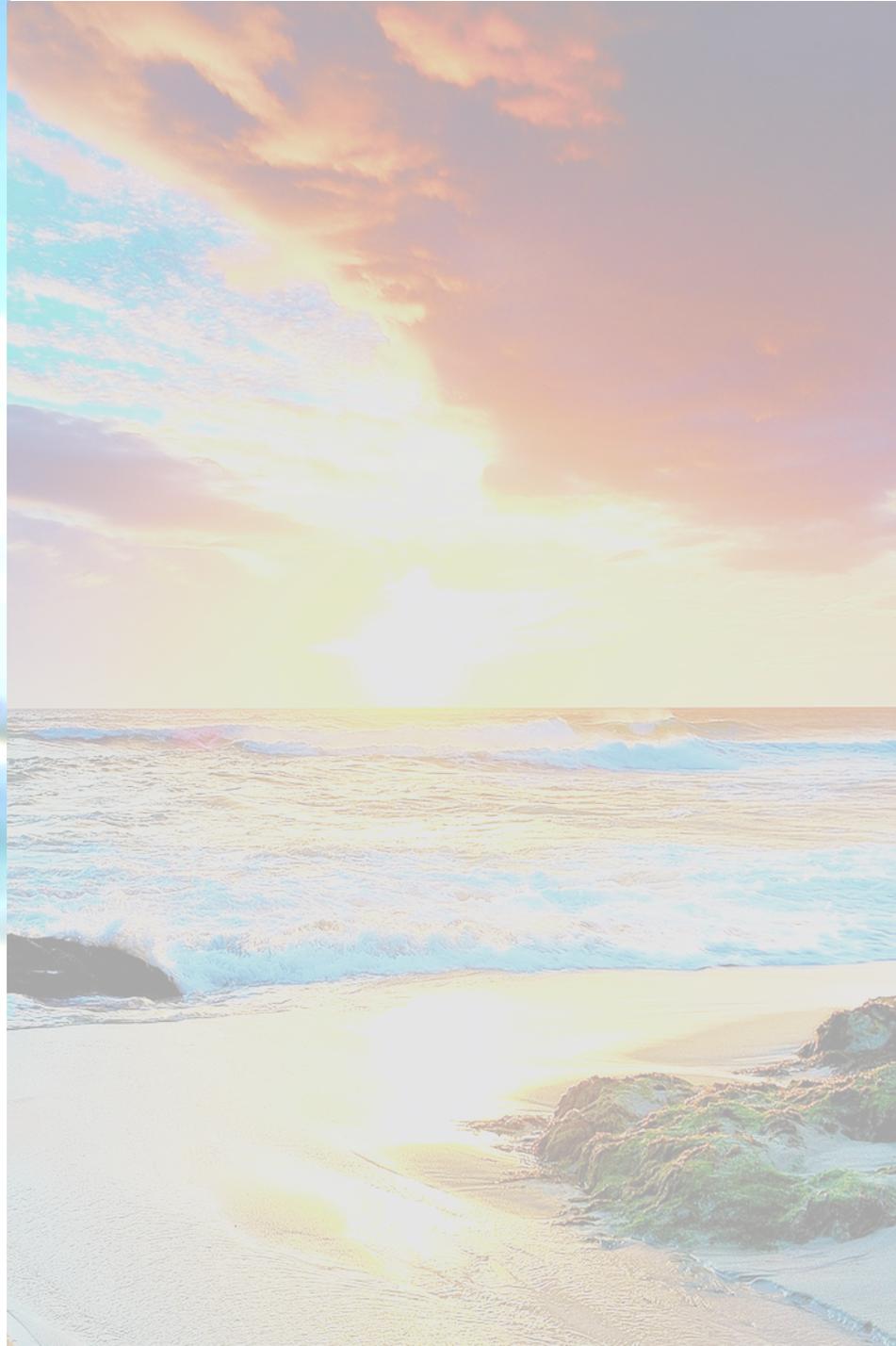
Nigel Orr (LPC Caen), Greg Hackman, Jack Henderson,
Panu Ruotsalainen, Peter Bender, Carl Unsworth, Christian Aa. Diget,
Franck Delaunay (LPC Caen) and many more...

In Texas:

Greg Christian, Antii Saastamoinen, Shuya Ota, Eames Bennett

transfer as a way to understand SHELLS & STARS





REACTION MODEL FOR (d,p) TRANSFER – the ADWA

Spectroscopic Factor

Shell Model: overlap of $|\psi(N+1)\rangle$ with $|\psi(N)\rangle_{\text{core}} \otimes n(lj)$

Reaction: the observed yield is not just proportional to this, because the **overlap integral** has a radial-dependent weighting or sampling



Hence the **observed yield** depends on the radial wave function and thus it depends on the geometry of the assumed potential well or other structure model

Many-body theory of $d + A(N, Z) \rightarrow B(N + 1, Z) + p$

overlap integral

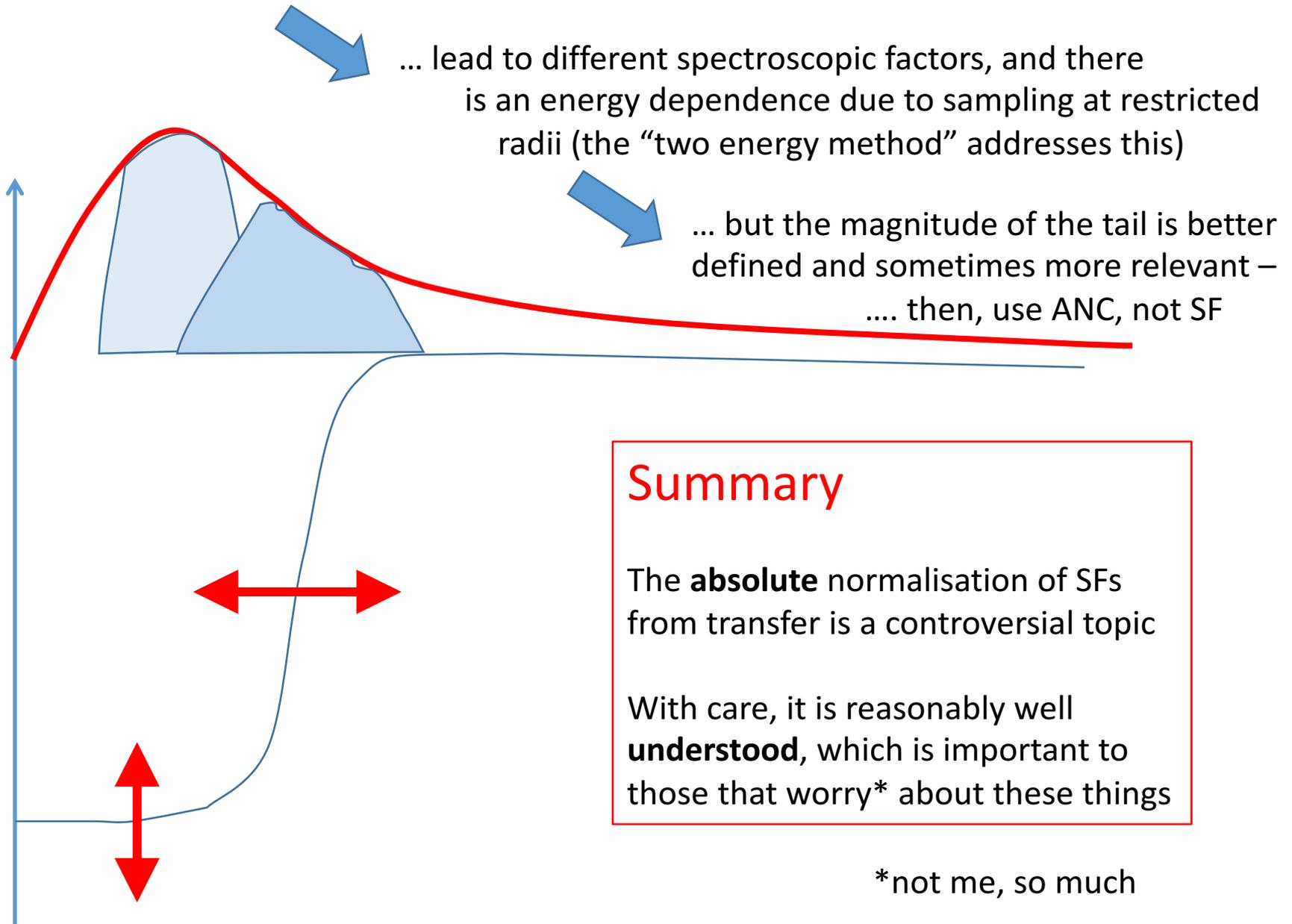
$$\phi_n^{BA}(\vec{r}_n) = \sqrt{N+1} \int d\xi_A \phi_B^*(\xi_A, \vec{r}_n) \phi_A(\xi_A)$$

spectroscopic factor

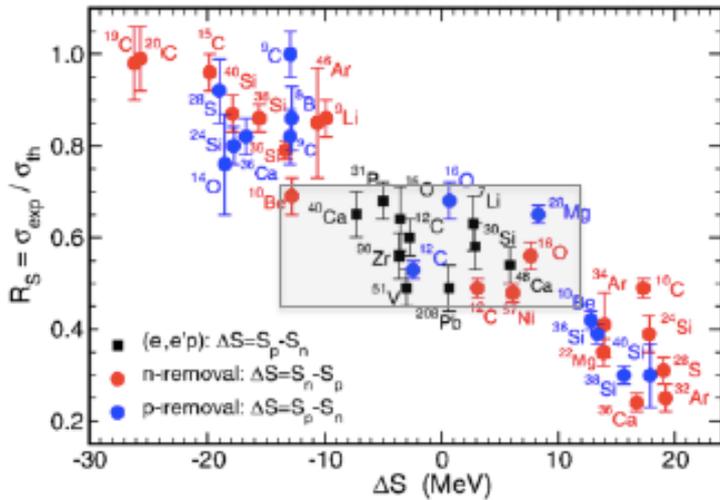
$$S^{AB} = \int d\vec{r}_n |\phi_n^{AB}(\vec{r}_n)|^2$$

$$T_{d,p} = \langle \chi_p^{(-)} | \phi_n^{BA} | V_{np} | \Psi_{\vec{K}_d} \rangle$$

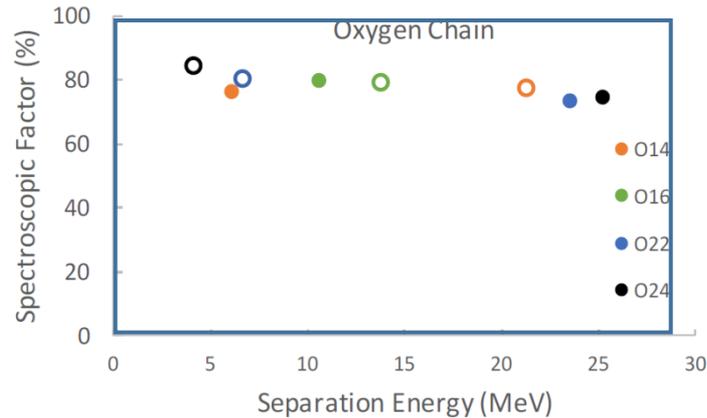
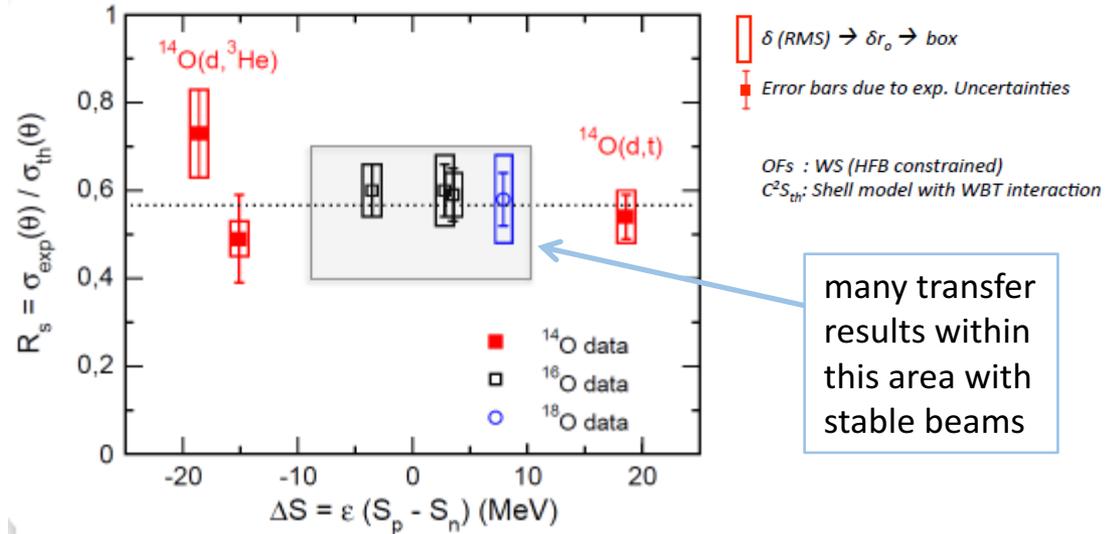
Different assumptions about the geometry of the binding for the transferred particle



J.A. Tostevin and A. Gade, Phys. Rev. C **90**, 057602 (2014)



F. Flavigny *et al.*, Phys. Rev. Lett. **110**, 122503 (2013).



(p,2p)

★ supports GANIL transfer results for ^{14}O , ^{16}O , ^{17}O , ^{21}O , ^{22}O , ^{23}O
Leila Atar, Monday

★ Ab initio structure (not reaction theory) for ^{14}O , ^{16}O , ^{22}O , ^{24}O
★
Andrea Idini, Monday

Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF

Negative parity states

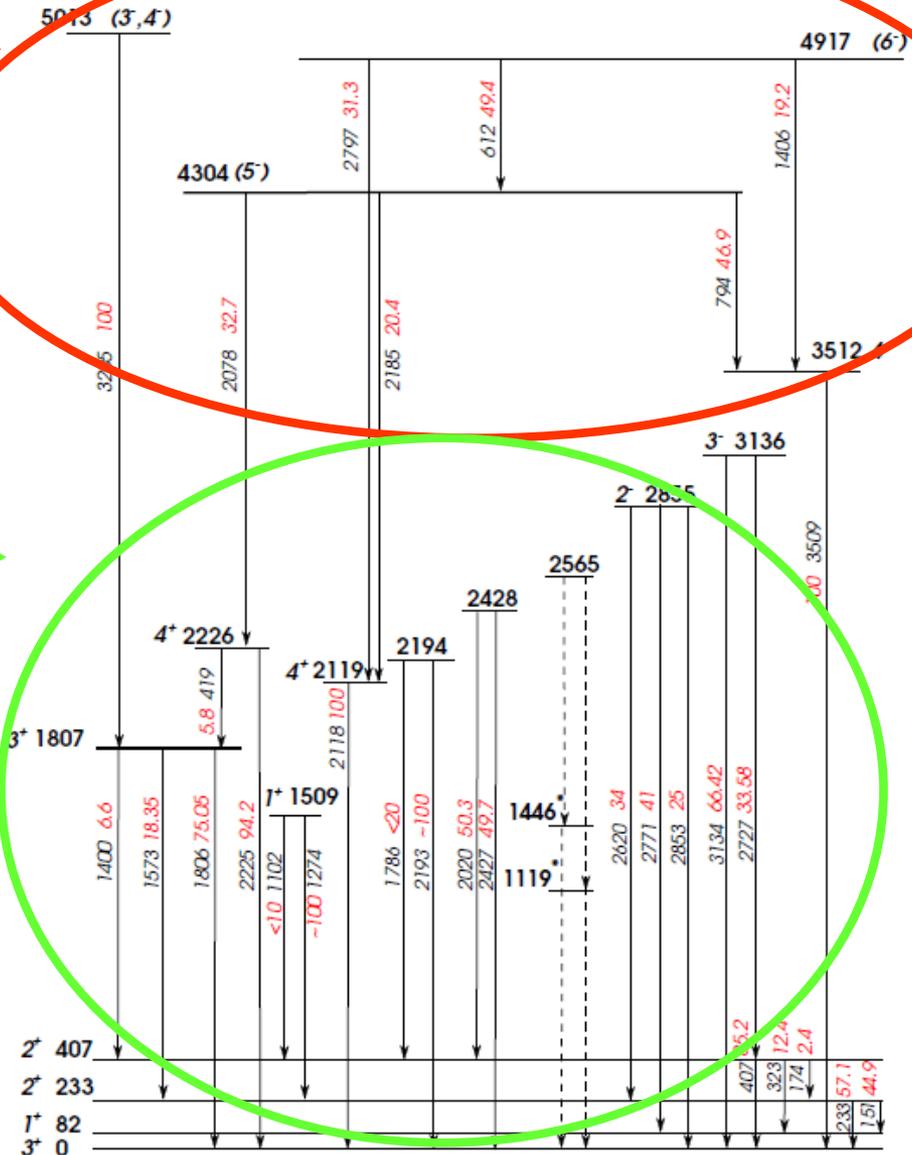
Levels never seen before,
selected by (d,p)

Gamma-ray decay scheme
Gamma-ray branching ratios

Positive parity states

GATE on the gamma rays,
take advantage of 30 keV
energy resolution

CHECK that this does not
bias the proton distribution
(*gamma angular efficiency*)



Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF

No.	E_x^a	$E_x^{SM\ b}$	$J^\pi\ c)$	J_{SM}^π	single L analysis			two L analysis (where applicable)								
					L	nlj	S	S^{SM}	L_1	$n_1l_1j_1$	S_1	S_1^{SM}	L_2	$n_2l_2j_2$	S_2	S_2^{SM}
	0	0	3^+	3_1^+	*	$1s_{1/2}$		0.61	*	$1s_{1/2}$		0.61	*	$0d_{3/2}$		0.01
														$0d_{5/2}$		0.01
	0.082 ^{d)}	0.077	1^+	1_1^+	*	$0d_{3/2}$		0.29								
						$0d_{5/2}$		0.11								
	0.232	0.149	2^+	2_1^+	0	$1s_{1/2}$	0.13	0.15	0	$1s_{1/2}$	0.10	0.15	2	$0d_{3/2}$	0.19†	0.10
														$0d_{5/2}$		0.09
	0.405	0.416	2^+	2_2^+	0	$1s_{1/2}$	0.33	0.27	0	$1s_{1/2}$	0.30	0.27	2	$0d_{5/2}$	0.13†	0.03
														$0d_{3/2}$		0.03
	1.507	1.409	1^+	1_2^+	2	$0d_{3/2}$	0.39	0.09								
						$0d_{5/2}$		0.10								
	1.805	1.676	(3^+)	3_2^+	2	$0d_{3/2}$	0.37	0.33	2	$0d_{3/2}$	0.33†	0.33	0	$1s_{1/2}$	0.01‡	0.00
						$0d_{5/2}$		0.02	2	$0d_{5/2}$		0.02				
	1.992	1.758	4^+	4_1^+	2	$0d_{3/2}$	0.07	0.07								
	2.116	2.241	5^+	5_1^+	2	$0d_{5/2}$	0.16	0.08								
	2.195	2.142	2^+	2_3^+	2	$0d_{3/2}$	0.49	0.06								
	2.225	2.048	(4^+)	4_2^+	2	$0d_{3/2}$	0.43	0.51								
						$0d_{5/2}$		0.01								
	2.423	2.452	2^+	2_4^+					0	$1s_{1/2}$	0.00	0.13	2	$0d_{3/2}$	0.14	0.23
	2.843	2.936	(2^-)	2_1^-	3	$1p_{3/2}$		0.20	3	$0f_{7/2}$	1.10	0.20	1	$1p_{3/2}$	0.10	0.05
						$0f_{5/2}$		0.00		$0f_{5/2}$		0.00		$1p_{1/2}$		0.04
	3.135	3.228	3^-	3_1^-	1	$1p_{3/2}$	0.07†	0.15	1	$1p_{3/2}$	0.06†	0.15	3	$0f_{7/2}$	0.10‡	0.13
						$1p_{1/2}$		0.02		$1p_{1/2}$		0.02		$0f_{5/2}$		0.00
	3.511	3.513	4^-	4_1^-	1	$1p_{3/2}$	0.30	0.44	1	$1p_{3/2}$	0.25	0.44	3	$0f_{7/2}$	0.51†	0.00
														$0f_{5/2}$		0.00
	4.087	3.690	2^-	2_2^-	3				1	$1p_{3/2}$	0.34	0.31	3	$0f_{7/2}$	0.78	0.03
	4.239	3.975	4^+	4_5^+	2	$0d_{3/2}$	0.12	0.12								
	4.305	4.401	(5^-)	5_1^-	3				1	$1p_{3/2}$	0.01	0.00	3	$0f_{7/2}$	0.25	0.46
	4.597	4.460	3^-	3_2^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.02	0.10	3	$0f_{7/2}$	0.76	0.10
	4.800	4.730	4^-	4_2^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.00	0.05	3	$0f_{7/2}$	0.62	0.37
	4.917	4.881	(6^-)	6_1^-	3	$0f_{7/2}$	0.51	0.61								
	4.932	4.770	3^-	3_4^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.00	0.28	3	$0f_{7/2}$	0.63	0.05
	5.009		$(3^-, 4^-)$		*											

UPDATE

8 new states

plus

4 new ℓ values

IMPROVED

background

subtraction

NEW

gamma-ray

angular

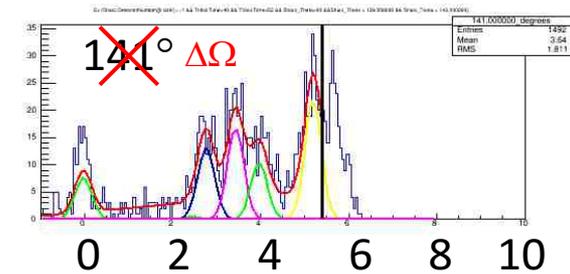
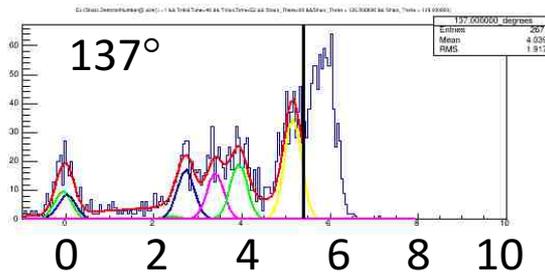
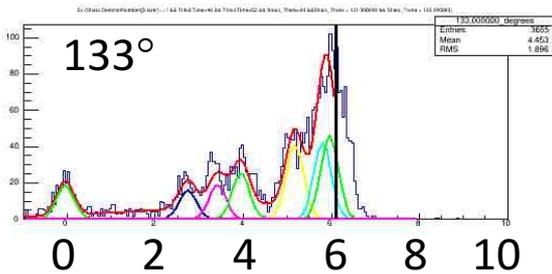
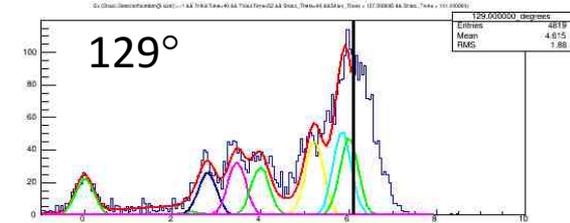
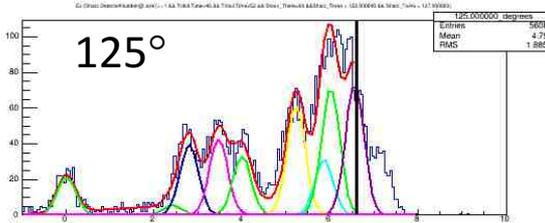
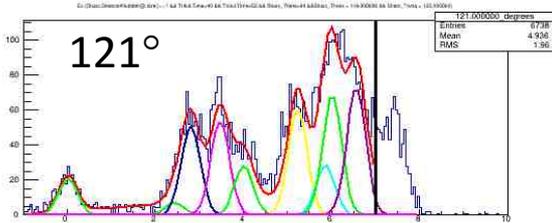
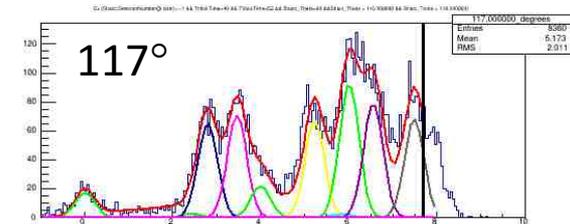
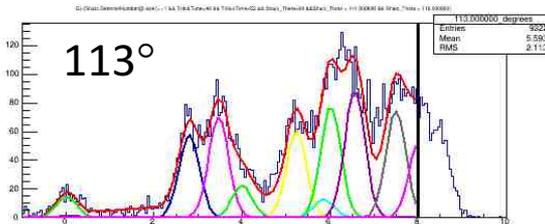
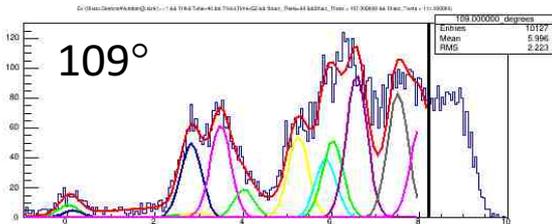
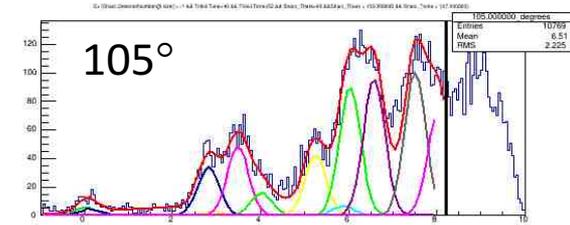
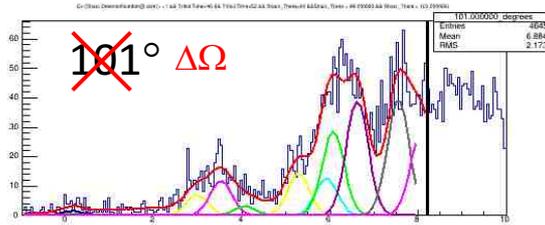
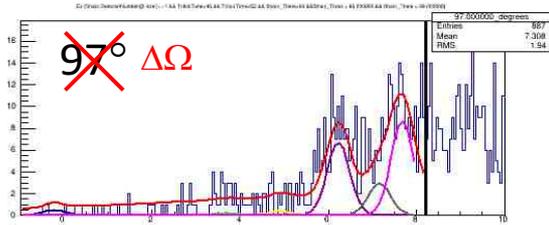
correlations

I.C. Celik

PhD thesis

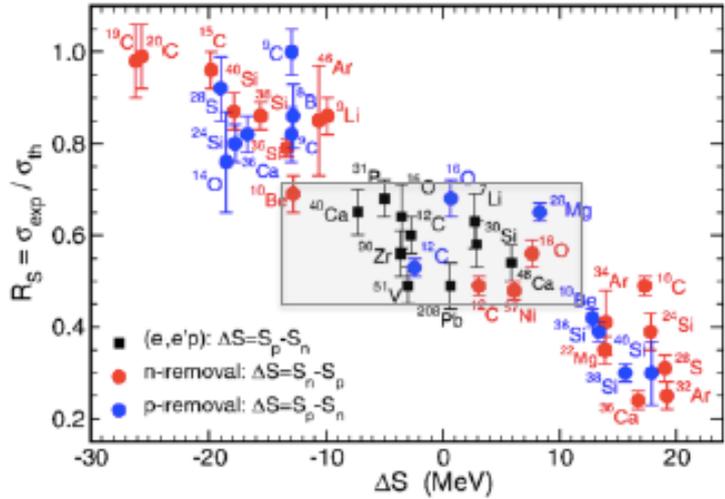
Surrey 2015

$d(^{24}\text{Na},p)^{25}\text{Na}$ – fits to excitation energy spectrum at each angle

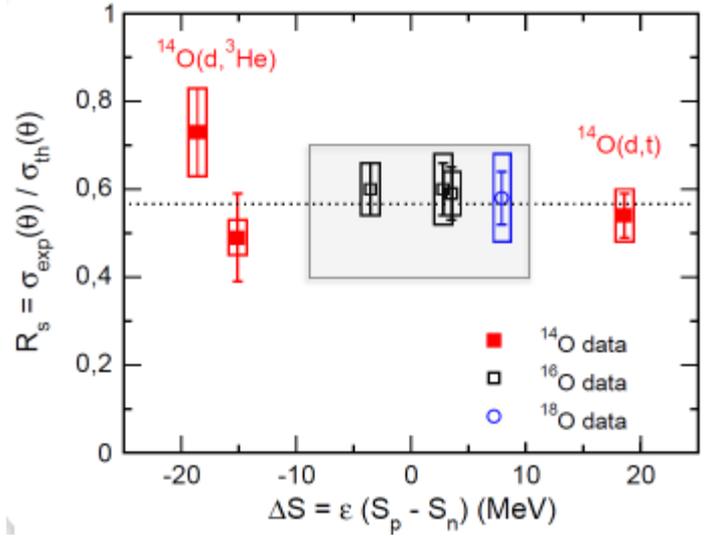


Excitation Energy in ^{25}Na (MeV)

J.A. Tostevin and A. Gade, Phys. Rev. C **90**, 057602 (2014)



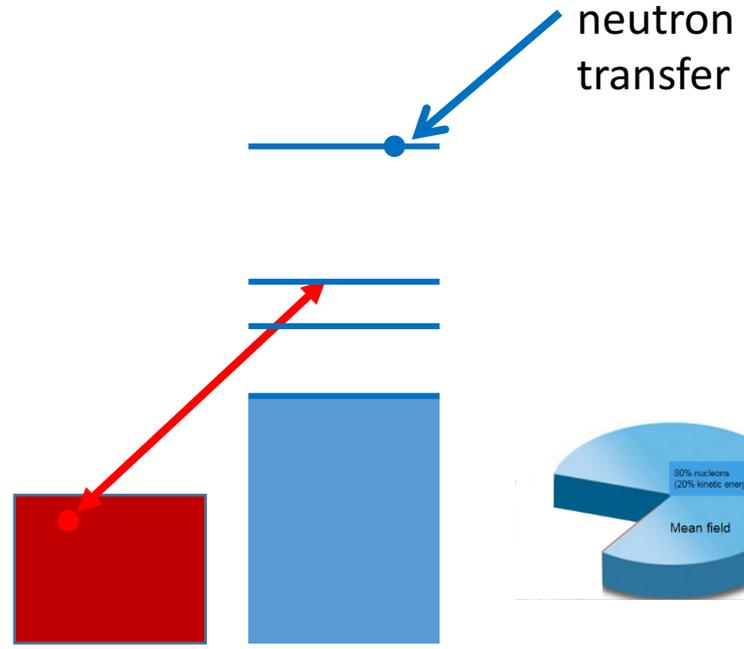
F. Flavigny *et al.*, Phys. Rev. Lett. **110**, 122503 (2013).



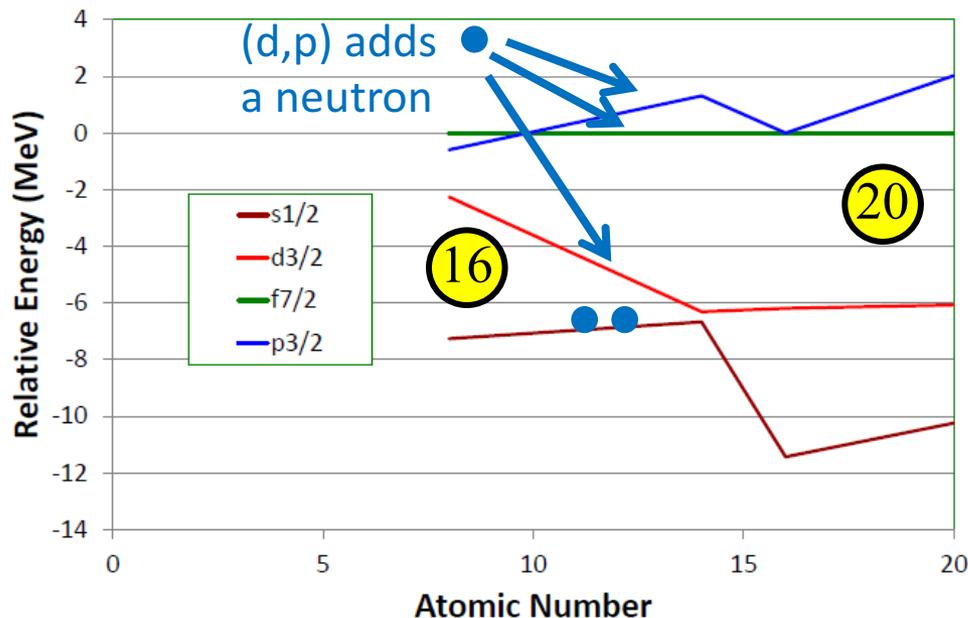
Transfer

Some “conflict” with knockout, understanding quenched SFs, possible effect of correlations...

An excellent tool to uncover and study the evolution of nuclear structure produced via the mean field and the 85% of the physics



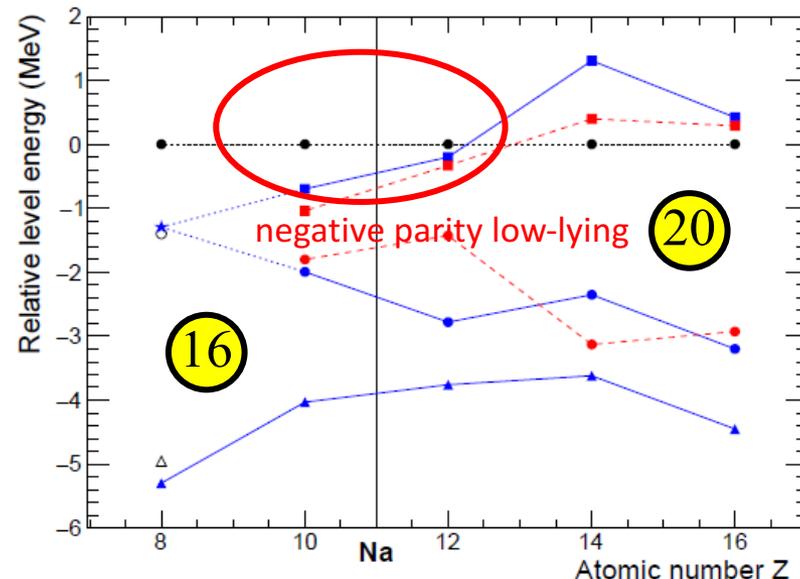
Theory: effective spe's



PRL 104, 012501 (2010)

Otsuka et al.

Experiment: energies of just the lowest levels



PLB (2016)

N=15 and 17 isotones

<http://dx.doi.org/10.1016/j.physletb.2016.05.093>

G.L. Wilson et al.

- Our aim is to identify single-particle-like levels and determine their spin/parity
- We use the selective nature of (d,p) neutron transfer (with radioactive beams)
- We aim to track the evolution of these levels and compare to the shell model

Future plans – $d(^{60}\text{Cr},p)^{61}\text{Cr}$ at 10.0 MeV/u

We have plans to move towards studying the second island of inversion e.g. via $^{60}\text{Cr}(d,p)$ at Texas A&M...

