

Fragmentation



Isomer production in fragmentation reaction

Zsolt Podolyák University of Surrey









A/q

Isomers:

-Very sensitive (decays): info about exotic nuclei -Isomeric beams (in storage rings, in reactions)





Isomeric decay spectroscopy:

- decay correlated with the fragment
- very sensitive





Past: **RISING**

Future: **DESPEC** (DEGAS array)



Isomers are special



W.-D. Schmidt-Ott et al., Z. Phys. A 350 (1994) 215.

Highest spin from fragmentation: I=(55/2) isomer in ²¹³Rn



Fig. 1. Gamma-ray energy spectrum obtained in coincidence with ²¹³Rn ions using a time gate of width 1.4 µs starting ~50 ns after the prompt flash. The transitions used to obtain the isomeric ratios for the $(55/2)^+$, $43/2^-$, $31/2^-$ and $25/2^+$ levels are denoted # * % and @ respectively.

A.M. Denis Bacelar et al., Phys. Lett. B 723, 302 (2012)

Isomeric ratios from ²⁰⁸Pb and ²³⁸U fragmentation



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

Isomeric ratio vs spin



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

if A_{projectile}-A_{fragment}~large Statistical abrasion-ablasion model (ABRABLA code) Excitation energy Angular momentum

- ~27 MeV/abrated nucleon=
 - =2 x single particle (holes) energy

from single particle

states only

Is this good enough?

Ablated nuclei/abraded nuclei ~2 Good cross sections

M. De Jong, A.V. Ignatyuk and K.-H. Schmidt, Nucl. Phys. A 613 (1997) 435



M. De Jong, A.V. Ignatyuk and K.-H. Schmidt, Nucl. Phys. A 613 (1997) 435



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)



¹⁸⁶W(¹⁶O,6n) at 110 MeV; ¹⁷⁰Er(³⁰Si,4n) at 144 MeV

fusion-evaporation reaction! $\varphi = I_{isomer} / (I_{parallel} + I_{isomer}) = I_{isomer} / I_{total}$ $\rho_{exp} = R_{exp} / \varphi$

 ρ_{exp} - the probability of populating states with higher spin than the isomer – can be compared with theory!

Without structure considerations



With structure considerations



Zs. P., Acta Phys. Pol. B36 (2005) 1269



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

Isomeric ratios following fragmentation

 208 Pb \rightarrow 206 Pb

at E/A=1 GeV



N. Lalović et al., to be published

Fragments are slower than projectile: momentum shift (friction)



(collective) *I* perpendicular to the beam

We need to couple: single particle holes *I* (any direction in 3D) collective *I* (2D)

single particle only (Analytical)

single particle + collective





A.M. Denis Bacelar et al., Phys. Lett. B 723, 302 (2012)

Comparison with theory (sharp cut-off approx.)



Simplified theory (analytical formula)



J.-J. Gaimard and K.-H. Schmidt, Nucl. Phys. A 531 (1991) 709

M. De Jong, A.V. Ignatyuk and K.-H. Schmidt, Nucl. Phys. A 613 (1997) 435



FIG. 8. (Color online) Isomeric ratios determined in the current study (see Table I) compared with the theoretical population predicted by the analytical formula only [Eq. (3)] plotted as a function of angular momentum of the isomeric state. The spin-cutoff parameter in Eq. (3) was multiplied by a factor of 2.
M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

Population of isomers by *two-proton knockout* reaction in ²⁰⁶Hg



E.Simpson et al., Phys. Rev. C 80 (2009) 064608.

Isomeric ratio as function of longitudinal momentum





FIRST OBSERVATION OF THE Δ RESONANCE IN RELATIVISTIC HEAVY-ION CHARGE-EXCHANGE REACTIONS



Role of nucleonic resonances in reactions

(but not for individual excited states)



do/dE(µb/MeV)



Target

 $Z \rightarrow Z+1$ processes

$$p(n, \Delta^0)p = p(n, p\pi^-)p$$
$$p(n, \Delta^+)n = p(n, p\pi^0)n$$
$$n(n, \Delta^0)n = n(n, p\pi^-)n$$

$$\begin{split} p(n,p)\Delta^0 &= p(n,p)n\pi^0\\ p(n,p)\Delta^0 &= p(n,p)p\pi^-\\ n(n,p)\Delta^- &= n(n,p)n\pi^- \end{split}$$

p(n,p)n

Only the Δ resonance shown





Decay of the $I^{\pi}=10^+$ metastable state in 54 Fe



Momentum distribution of ⁵⁴Fe nuclei



Isomeric ratio of the 10⁺ isomer



=> the isomer is produced in the low momentum tail

Isomeric ratios following fragmentation



FIG. 2. <u>Calculated</u> isomeric ratios, as a function of residue momentum, in the projectile rest frame in the absence of broadening

E.C. Simpson et al., Phys. Rev. C 82, 037602 (2010)

²⁰⁸Pb -> ²⁰⁶Hg


N. Lalovic et al, to be published





${}^{56}\text{Fe} \rightarrow {}^{54}\text{Fe}$





Dominant configurations



Dominant configurations

Summary

Neutron-rich N~126 and south-east of ²⁰⁸Pb

Shell-model has high predictive power (structure calculations)

First-forbidden – allowed β -decay competition?

First-forbidden β-decay calculations?

10⁺ populated in ⁵⁴Fe from ⁵⁶Fe at E/A=500 MeV

Which states are populated in high-energy charge-exchange (Δ) reactions?

Conclusions

Production of ²³⁸U fragments hindered by fission

Fission probability described considering the level density

At high-spins the angular momentum from abraded nuclei are not enough: contributions from evaporation, friction, excitations

High-spin states are produced with higher probability

than expected (isomeric beams)

Can this be related to:

the spin distribution of level density?
level density through spin dependence of fission?

Thanks!

Conclusions

Reasonable predictability for isomer production

-factor of two *if* structure is known (I<15hbar)

High-spin states are produced with higher probability

than expected (isomeric beams)

At high-spins the angular momentum from abraded nuclei are not enough: contributions from evaporation, friction, excitations

Isomeric ratios from (one or) two-particle removal understood

Importance of nucleonic excitation (⁵⁴Fe 10⁺ isomer)

Thanks!

Collaborators

PHYSICAL REVIEW C 88, 024611 (2013)

Population of high-spin isomeric states following fragmentation of ²³⁸U

M. Bowry,¹ Zs. Podolyák,¹ S. Pietri,² J. Kurcewicz,² M. Bunce,¹ P. H. Regan,¹ F. Farinon,² H. Geissel,^{2,3} C. Nociforo,² A. Prochazka,² H. Weick,² N. Al-Dahan,¹ N. Alkhomashi,¹ P. R. P. Allegro,⁴ J. Benlliure,⁵ G. Benzoni,⁶ P. Boutachkov,² A. M. Bruce,⁷ A. M. Denis Bacelar,⁷ G. F. Farrelly,¹ J. Gerl,² M. Górska,² A. Gottardo,⁸ J. Grębosz,⁹ N. Gregor,² R. Janik,¹⁰ R. Knöbel,² I. Kojouharov,² T. Kubo,¹¹ N. Kurz,² Yu. A. Litvinov,² E. Merchan,² I. Mukha,² F. Naqvi,¹² B. Pfeiffer,^{2,3} M. Pfützner,¹³ W. Plaß,³ M. Pomorski,¹³ B. Riese,² M. V. Ricciardi,² K.-H. Schmidt,² H. Schaffner,² C. Scheidenberger,^{2,3} E. C. Simpson,¹ B. Sitar,¹⁰ P. Spiller,² J. Stadlmann,² P. Strmen,¹⁰ B. Sun,^{2,14} I. Tanihata,¹⁵ S. Terashima,¹⁴ J. J. Valiente Dobón,⁸ J. S. Winfield,² H.-J. Wollersheim,² and P. J. Woods¹⁶ ¹Department of Physics, University of Surrey, Guildford GU2 7XH, United Kingdom ²GSI, Planckstrasse 1, D-64291 Darmstadt, Germany ³IInd Physical Institute, Justus-Liebig University Giessen, D-35392 Giessen, Germany ⁴University of São Paulo, São Paulo 05508-900, Brazil ⁵University Santiago de Compostela, 15706 Santiago de Compostela, Spain ⁶INFN Sezione di Milano, Dipartimento di Fisica, Via Celoria 16, 20133 Milano, Italy ⁷School of Computing Engineering and Mathematics, University of Brighton, Brighton BN2 4GJ, United Kingdom ⁸INFN, Laboratori Nazionali di Legnaro, Legnaro (Padova), Italy ⁹The Henryk Niewodniczański Institute of Nuclear Physics, PL-31-342 Kraków, Poland ¹⁰Department of Nuclear Physics and Biophysics, Comenius University, Mlynská dolina, 842 48 Bratislava, Slovakia ¹¹RIKEN Nishina Center, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan ¹²Department of Physics, University of Yale, New Haven, Connecticut 06511-8499, USA ¹³Faculty of Physics, University of Warsaw, PL-00-681 Warsaw, Poland ¹⁴School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China ¹⁵Research Center for Nuclear Physics, 10-1 Mihogaoka, Ibaraki, Osaka 567-0047, Japan ¹⁶School of Physics and Astronomy, University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom (Received 2 June 2013; published 16 August 2013)

Thanks!



Abrasion (incl. friction) (relativistic transport model) Abrasion+ablation (+sequential binary decay)

Ion	Ιπ	E (keV)	R_{exp} [%]	R ^{ART} [%]	R ^{SBD} _{the} [%]
²¹¹ Fr	29/2+	2423	5.7(19)	2.59	10.03
²¹² Fr	15-	2492	7.5(18)	2.24	9.15
²¹³ Fr	29/2+	2538	12(8)	2.65	10.82
²¹⁴ Ra	17-	4147	6.8(23)	0.58	3.20
²¹⁵ Ra	$43/2^{-}$	$3757 + \Delta$	3.1(6)	0.07	0.82

Better agreement

S. Pal and R. Palit, Phys. Lett. B 665 (2008) 164.

Fragmentation (spallation) reactions at relativistic energies: Ь multi-hole state abrasion ablation 87Fr 86 Rn ₈₅At 10-10 σ (mb) 10 10 10 10 10 10 23510 0 230 230 220 225 225 225 230 H. Alvarez-Pol et al., Phys. Rev. C 82, 041602(R) (2110)

To be discussed: Cross section: measures the end product Spin: info mainly about abrasion



Ablation competes with fission (238U beam)

Survival probability against fission (production cross section) depends on level density *if A_{projectile}-A_{fragment}~large (>10)* Statistical abrasion-ablasion model (ABRABLA code)

Excitation energy

- ~27 MeV/abrated nucleon~
 - =2 x single particle (holes) energy
- Ablated nuclei/abraded nuclei ~2
- Fission depends on level density

Good cross sections

A.R. Junghans, M. de Jong, H.-G. Clerc, A.V. Ignatyuk, G.A. Kudyaev, K.-H. Schmidt,

Nucl. Phys. A 629 (1998) 635





Fig. 2. Fission barriers of nuclei in the region of interest for the present investigation. Upper part: The macroscopic part [37] of the fission barrier at zero angular momentum. Lower part: The curves include the contribution of the ground-state shell effect [38].

Rotational enhancement



Collective enhancement



Collective enhancement

Damping dependent on def.

Damping independent on def.

+vibrational enhancement

A.R. Junghans et al., Nucl. Phys. A 629 (1998) 635



Conclusions from cross section measurements

- No stabilisation against fission near N=126
- Effect of shell stabilisation and collective enhancement on fissility cancels out
- Damping of the collective enhancement in the level density is independent of deformation

A.R. Junghans, M. de Jong, H.-G. Clerc, A.V. Ignatyuk, G.A. Kudyaev, K.-H. Schmidt, Nucl. Phys. A 629 (1998) 635

if A_{projectile}-A_{fragment}~large (>10) Statistical abrasion-ablasion model (ABRABLA code)

Angular momentum

from single particle states only

$$\rho_n(U,J) = \frac{2J+1}{2\sigma_n^2} \exp\left(-\frac{J(J+1)}{2\sigma_n^2}\right) \rho_n(U)$$

Spin-cutoff parameter $\sigma_n^2 = 0.234 \left(1 - \frac{U}{n\epsilon_f}\right) A_p^{2/3} \frac{n(A_p - n)}{A_p - 1}$

U-excitation energy from n holes only

Is this good enough?

M. De Jong, A.V. Ignatyuk and K.-H. Schmidt, Nucl. Phys. A 613 (1997) 435







Isomeric decay spectroscopy:

- gamma decay correlated with the fragment
- very sensitive



Highest spin from fragmentation: I=(55/2) isomer in ²¹³Rn



Fig. 1. Gamma-ray energy spectrum obtained in coincidence with ²¹³Rn ions using a time gate of width 1.4 µs starting ~50 ns after the prompt flash. The transitions used to obtain the isomeric ratios for the $(55/2)^+$, $43/2^-$, $31/2^-$ and $25/2^+$ levels are denoted # * % and @ respectively.

A.M. Denis Bacelar et al., Phys. Lett. B 723, 302 (2012)



<sup>J.-J. Gaimard and K.-H. Schmidt, Nucl. Phys. A 531 (1991) 709
M. De Jong, A.V. Ignatyuk and K.-H. Schmidt, Nucl. Phys. A 613 (1997) 435</sup>

Isomeric ratios from ²⁰⁸Pb and ²³⁸U fragmentation



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

Isomeric ratio vs spin



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)



¹⁸⁶W(¹⁶O,6n) at 110 MeV; ¹⁷⁰Er(³⁰Si,4n) at 144 MeV

fusion-evaporation reaction! $\varphi = I_{isomer} / (I_{parallel} + I_{isomer}) = I_{isomer} / I_{total}$ $\rho_{exp} = R_{exp} / \varphi$

 ρ_{exp} - the probability of populating states with higher spin than the isomer – can be compared with theory!

Without structure considerations



With structure considerations



Zs. P., Acta Phys. Pol. B36 (2005) 1269



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)

Fragments are slower than projectile: momentum shift (friction)



(collective) *I* perpendicular to the beam



A.M. Denis Bacelar et al., Phys. Lett. B 723, 302 (2012)

A 4 1 1 1 1 1 1 1 1 1 1

Doubled spin-cutoff parameter



M. Bowry et al., Phys. Rev. C 88, 024611 (2013)



Decay (internal and β , α) spectroscopy:

- decay correlated with the fragment
- *very sensitive* (ion beams > 1 ion/hour)




Identification

192W setting

Future: several projects

Multinucleon transfer reactions: theory

FIG. 4. Landscape of the total cross section $d^2\sigma/dZdN$ (mb, numbers near the curves) for production of heavy fragments in collisions of ¹³⁶Xe with ²⁰⁸Pb at $E_{\rm c.m.} = 450$ MeV. Contour lines are drawn over 1 order of magnitude.

V. Zagrebaev, W. Greiner, Phys. Rev. Lett. 101, 122701 (2008)

(1) *KHH7B interaction:* The model space considered consisted of the proton orbitals $d_{5/2}$, $h_{11/2}$, $d_{3/2}$, $s_{1/2}$ below Z = 82 and the $h_{9/2}$, $f_{7/2}$, $i_{13/2}$ ones above it, and the neutron orbitals $i_{13/2}$, $p_{3/2}$, $f_{5/2}$, $p_{1/2}$ below N = 126 and $g_{9/2}$, $i_{11/2}$, $j_{15/2}$ above. The cross shell two-body interaction matrix elements (TBMEs) are based on the H7B G-matrix [18], while the neutron–proton TBMEs are based on the Kuo–Herling interaction [19] as modified in [20]. These calculations describe accurately valence particle excitations (when no core-breaking is needed). They were used extensively on nuclei below Z = 82 along the N = 126 line [21–24], as well as for both in the N > 126 [25] and N < 126 [5,24] regions.

(2) KHM3Y interaction: The model space consisted of the proton orbitals $\mathbf{g}_{7/2}$, $d_{5/2}$, $h_{11/2}$, $d_{3/2}$, $s_{1/2}$ below Z = 82 and $h_{9/2}$, $f_{7/2}$, $i_{13/2}$, $\mathbf{f}_{5/2}$, $\mathbf{p}_{3/2}$, $\mathbf{p}_{1/2}$ above it, and the neutron orbitals $i_{13/2}$, $p_{3/2}$, $f_{5/2}$, $p_{1/2}$, $\mathbf{h}_{9/2}$, $\mathbf{f}_{7/2}$ below N = 126 and $g_{9/2}$, $i_{11/2}$, $j_{15/2}$, $\mathbf{g}_{7/2}$, $\mathbf{d}_{5/2}$, $\mathbf{d}_{3/2}$, $\mathbf{s}_{1/2}$ above. The additional orbitals, compared to the KHH7B calculations, are shown in bold. The cross-shell, two-body matrix elements are based on the M3Y interaction [26], while the neutron–proton interactions are based on the Kuo–Herling interaction [19] as modified in Ref. [20]. Such calculations gave a good

END

$h_{11/2}^2$ component of the 10+ isomer?

D. Rudolph et al., Phys. Rev. C78, 021301(R) (2008).

Isomeric ratio of the 10⁺ isomer

=> the isomer is produced in the low momentum tail

Conclusions

The 10⁺ isomer in ⁵⁴Fe populated from ⁵⁶Fe at E/A=500 MeV The 10⁺ state is a four particle state 10⁺ populated mainly at low momentum

=> It is populated via the Δ resonance

PRL 117, 222302 (2016)

PHYSICAL REVIEW LETTERS

week ending 25 NOVEMBER 2016

Thanks

Role of the Δ Resonance in the Population of a Four-Nucleon State in the ⁵⁶Fe \rightarrow ⁵⁴Fe Reaction at Relativistic Energies

Zs. Podolyák,¹ C. M. Shand,¹ N. Lalović,^{2,3} J. Gerl,³ D. Rudolph,² T. Alexander,¹ P. Boutachkov,³ M. L. Cortés,^{3,4}
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G. Rainovski,²⁶ P. Reiter,¹² M. D. Salsac,¹³ E. Sanchis,¹⁹ and J. J. Valiente Dóbon⁷

PRESPEC-AGATA campaign

Fragmentation of ⁵⁶Fe on H

C. Villagrasa-Canton et al., PRC75, 044603 (2007)

FIRST OBSERVATION OF THE Δ RESONANCE IN RELATIVISTIC HEAVY-ION CHARGE-EXCHANGE REACTIONS

Theory: intranuclear cascade model, e.g. A. Boudard et al., PRC66, 044615 (2002)

FIG. 3 (color online). Half-life systematics across the $N \sim 126$ shell closure. Results reported in this Letter are shown with red squares. For ²¹⁵Pb, the FRDM and DF3 predictions are shown with filled and empty circles, respectively. Deviations up to a factor of 2 from the experimental values are indicated with a shaded area. See text for discussion.

Fragmentation of 56Fe C. Villagrasa-Canton et al., PRC75, 044603 (2007)

FIRST OBSERVATION OF THE Δ RESONANCE IN RELATIVISTIC HEAVY-ION CHARGE-EXCHANGE REACTIONS

D. Bachelier et al., Phys. Lett. 172, 23 (1986)

208Pb+H

FIG. 12. Calculated velocity distributions of several bismuth isotopes produced in the interaction of 1*A* GeV lead with the proton (full line) and the deuteron (dashed line). The velocity distributions are normalized to the corresponding calculated production cross sections. The calculations were performed with INCL4 +ABLA. The upper x axis shows the energy transfer in the laboratory frame.

A. Kelic et al., Phys. Rev. C 70, 064608 (2004)

J. Benlliure et al., JPS Conf. Proc. 6, 020039 (2015)

AGATA detector layout – Status 13-3-2014

6 triplets 3 doublets

22 crystals

$Z \rightarrow Z+1$ processes

 $(^{A}Z, ^{A}(Z + 1))$ reaction

Target excitation		Projectile excitation		
$p(n, p)\Delta^{0} = p(n, p)n\pi^{0}$ $p(n, p)\Delta^{0} = p(n, p)p\pi^{-}$ $n(n, p)\Delta^{-} = n(n, p)n\pi^{-}$	[2/3] $[-\sqrt{2}/3]$ $[-\sqrt{2}]$	$\begin{split} p(n, \Delta^{0})p &= p(n, p\pi^{-})p \\ p(n, \Delta^{+})n &= p(n, p\pi^{0})n \\ n(n, \Delta^{0})n &= n(n, p\pi^{-})n \end{split}$	$[-\sqrt{2}/3]$ [-2/3] $[\sqrt{2}/3]$	
$\begin{array}{l} p(n,p)P_{11}^{0} = p(n,p)n\pi^{0} \\ p(n,p)P_{11}^{0} = p(n,p)p\pi^{-} \end{array}$	$\begin{bmatrix} -2 \\ 2\sqrt{2} \end{bmatrix}$	$p(n, P_{11}^{0})p = p(n, p\pi^{-})p$ $p(n, P_{11}^{+})n = p(n, p\pi^{0})n$ $n(n, P_{11}^{0})n = n(n, p\pi^{-})n$	$\begin{bmatrix} -\sqrt{2} \\ [2] \\ [\sqrt{2}] \end{bmatrix}$	

 $(^{A}Z, ^{A}(Z-1))$ reaction

Target excitation		Projectile excitation		
$\begin{split} p(p,n)\Delta^{++} &= p(p,n)p\pi^+\\ n(p,n)\Delta^+ &= n(p,n)n\pi^+\\ n(p,n)\Delta^+ &= n(p,n)p\pi^0 \end{split}$	$[\sqrt{2}]$ $[\sqrt{2}/3]$ [-2/3]	$\begin{split} p(p, \Delta^{+})p &= p(p, n\pi^{+})p \\ n(p, \Delta^{+})n &= n(p, n\pi^{+})n \\ n(p, \Delta^{0})p &= n(p, n\pi^{0})p \end{split}$	$[-\sqrt{2}/3]$ $[\sqrt{2}/3]$ [2/3]	
$\begin{split} n(p,n)P_{11}^+ &= n(p,n)n\pi^+ \\ n(p,n)P_{11}^+ &= n(p,n)p\pi^0 \end{split}$	$[-2\sqrt{2}]$ [2]	$ \begin{array}{ c c } p(p,P_{11}^{+})p = p(p,n\pi^{+})p \\ n(p,P_{11}^{+})n = n(p,n\pi^{+})n \\ n(p,P_{11}^{0})p = n(p,n\pi^{0})p \end{array} $	$[-\sqrt{2}]$ $[\sqrt{2}]$ [-2]	

I. Vidana et al., EPJ Web of Conferences 107, 10003 (2016)

PHYSICAL REVIEW C 70, 064608 (2004)

FIG. 8. Total charge-pickup cross section as a function of the projectile energy per nucleon: open triangles, ${}^{197}Au + {}^{1}H$ [11]; full dot, ${}^{197}Au + {}^{1}H$ [25]; full square, ${}^{208}Pb + {}^{1}H$ from the present work; and open dots, ${}^{197}Au + {}^{1}H$ [9]. The data from Refs. [9,11] were extracted from measurements performed with CH₂ and C targets.

Origins of the nuclear shell model

On the "Magic Numbers" in Nuclear Structure

OTTO HAXEL Max Planck Institut, Göttingen J. HANS D. JENSEN Institut f. theor. Physik, Heidelberg AND HANS E. SUESS Inst. f. phys. Chemie, Hamburg April 18, 1949

A SIMPLE explanation of the "magic numbers" 14, 28, 50, 82, 126 follows at once from the oscillator model of the nucleus,¹ if one assumes that the spin-orbit coupling in the Yukawa field theory of nuclear forces leads to a strong splitting of a term with angular momentum l into two distinct terms $j = l \pm \frac{1}{2}$.

If, as a first approximation, one describes the field potential of the nucleons already present, acting on the last one added, as that due to an isotropic oscillator, then the energy levels are characterized by a single quantum number $r=r_1+r_2+r_3$, where r_1 , r_2 , r_3 are the quantum numbers of the oscillator in 3 orthogonal directions. Table I, column 2 shows the multiplicity of a term with a given value of r, column 3 the sum of all multiplicities up to and including r. Isotropic anharmonicity of the potential field leads to a splitting of each r-term according to the orbital angular momenta l (l even when r is odd, and vice versa), as in Table I, column 4. Finally, spin-orbit coupling leads to the l-term splitting into $j=l\pm\frac{1}{2}$, columns 5 and 6, whose multiplicities are listed in column 7.

The "magic numbers" (column 8) follow at once on the assumption of a particularly marked splitting of the term with the highest angular momentum, resulting in a "closed shell

Phys. Rev. 75, 1766 (1949) (also M. Goeppert-Mayer and others)

1 Orcil	2	3	4	5	6	7	8
lator- quan- tum num- ber r	Multi- plicity	Sum of all multi- plicities	Orbital momen- tum I	Total angular momen- tum j	<i>l_i-symbol</i>	Multi- plicities	Magic num- bers
1	2	2	0	1/2	\$1/2	2	
2			1	3/2	\$ 2/2	4	
	6	8		1/2	\$1/2	2	
3			2	5/2	$d_{5/2}$	6	14
				3/2	$d_{2/2}$	4	
	12	20	0	1/2	\$1/2	2	
4			3	7/2	f7/2	8	28
				5/2	∫5/2	6	
			1	3/2	\$3/2	4	
_	20	40		1/2	\$1/2	2	
5			4	9/2	89/2	10	50
				7/2	87/2	8	
			2	5/2	$d_{4/2}$	6	
		-		3/2	$d_{3/2}$	4	
	30	70	0	1/2	51/2	2	
6			5	$\frac{11}{2}$	h11/2	12	82
				2/2	129/2	10	
			3	7/2	J7/2	8	
				5/2	$J_{5/2}$	6	
	43		1	3/2	p 2/2	4	
-	42	112		1/2	\$21/2		126
1			0	13/2	\$13/2	14	126
				0/2	#11/2	12	
			*	9/2	g9/2	10	

structure" for each completed r-group, together with the highest *j*-term of the next succeeding r-group. This classification of states is in good agreement with the spins and magnetic moments of the nuclei with odd mass number, so far as they are known at present. The anharmonic oscillator model seems to us preferable to the potential well model,² since the range of the nuclear forces is not notably smaller than the nuclear radius.

A more detailed account will appear in three communications to Naturwissenschaften.³

¹See, e.g., H. A. Bethe and R. Bacher, Rev. Mod. Phys. 8, 82 (1937), pars. 32-34.

² Which anyhow does not lead to a very different term-sequence compared with that of an anharmonic oscillator, see reference 1.

³ (a) Haxel, Jensen, and Suess, Naturwiss. (in press). (b) Suess, Haxel, and Jensen, Naturwiss. (in press). (c) Jensen, Suess, and Haxel, Naturwiss. (in press).

TABLE I. Classification of nuclear states.

Example of modern shell model (Zr isotopes)

Lifetime measurements

=> For N>126 and Z<82: $t_{1/2}$ (exp) > $t_{1/2}$ (theory)

R. Caballero-Folch et al., arXiv:1511.01296

Fragmentation (spallation) reactions at relativistic energies $\overbrace{}^{\text{multi-hole state}} \circ \overbrace{}^{\text{total}} \circ \circ \overbrace{}^{\text{total}} \circ \circ \overbrace{}^{\text{total}} \circ \circ \circ \circ$

Figure 1. Quasi-elastic (a) and inelastic (b and c) elementary processes contributing to the $({}^{A}Z, {}^{A}(Z \pm 1))$ reaction considered in this nodel. The resonance *R* can be either a $\Delta(1232)$ or a $N^{*}(1440)$.

- EPJ Web of Conferences **107**, 10003 (2016)
- DOI: 10.1051/epjconf/201610710003
- © Owned by the authors, published by EDP Sciences, 2016

I. Vidana et al., EPJ Web of Conference

Excitation of Δ and N^* resonances in isobaric charge-exchange reactions of heavy nuclei

I. Vidaña^{1,a}, J. Benlliure², H. Geissel³, H. Lenske⁴, C. Scheidenberger³, and J. Vargas²

FIG. 3. Energy dependence of charge-changing cross sections of (a) 12 C and (b) 19 C on a proton target. The data are taken from Ref. [25] for open inverted triangles and from Ref. [26] for closed triangles.

FIG. 1. Total reaction (or interaction) and charge-changing cross sections of ¹²C on a ¹²C target as a function of incident energy. Calculations are performed with the HO densities that give $r_p = r_n = 2.326$ fm. Results with the zero-range profile functions are also drawn for comparison. References for the experimental data on σ_R (open circle) and σ_I (open rectangle) are quoted in Ref. [24]. The σ_{cc} data are taken from Ref. [8] for diamond, Ref. [25] for inverted triangle, Ref. [26] for closed triangle, and Ref. [27] for open triangle.

PHYSICAL REVIEW C 94, 011602(R) (2016)

Parameter-free calculation of charge-changing cross sections at high energy

Y. Suzuki,^{1,2} W. Horiuchi,³ S. Terashima,⁴ R. Kanungo,⁵ F. Ameil,⁶ J. Atkinson,⁷ Y. Ayyad,⁷ D. Cortina-Gil,⁸ I. Dillmann,⁶

Fig.6: One-step direct and two-step transfer charge exchange cross sections for ${}^{12}C({}^{12}C,{}^{12}N){}^{12}B$ as a function of incident energy per nucleon. For ${}^{12}B(2^-)$ also the central-plus-tensor direct result (dashed) is shown.

Nuclear Physics A482 (1988) 343c–356c North-Holland, Amsterdam

Fig.7: One-step direct and two-step transfer charge exchange cross sections for ${}^{58}\text{Ni}({}^{13}\text{C},{}^{13}\text{N}){}^{58}\text{Co}$ as a function of incident energy per nucleon. Results for ${}^{58}\text{Co}(2^+,\text{g.s.})$ and ${}^{58}\text{Co}(1^+,1.86\text{MeV})$ are shown. For the ground state reaction the non-spinflip $\Delta S=0$ and spinflip $\Delta S=1$ partial cross sections are displayed.

THEORY OF HEAVY ION CHARGE EXCHANGE SCATTERING AT LOW AND INTERMEDIATE ENERGIES

H. LENSKE

^{207,208}Hg beams from molten-lead target at ISOLDE

²⁰⁸Pb(n,2p)²⁰⁷Hg₁₂₇? or/and ²⁰⁸Pb(,π⁺ p)²⁰⁷Hg₁₂₇ ? $(p--> \Delta^+ --> n + \pi^+)$

²⁰⁸Pb(t,3p)²⁰⁸Hg₁₂₈? or/and 208 Pb(α ,4p) 208 Hg₁₂₈ ? or/and 208 Pb(n, π^+ p) 208 Hg₁₂₈ ? or/and 208 Pb(, π^+ π^+) 208 Hg₁₂₈ ?

B. Jonson, O.B. Nielsen, J. Zylicz, CERN-81-09 (1981) (Proc. Int. Conf. Nuclei far from stability, Helsingor, Denmark. Vol.2 p.640 (1981))

the mercury isotopes, including ²⁰⁶Hg and ²⁰⁷Hg.

Volatile elements production rates in a proton-irradiated molten lead-bismuth target at ISOLDE

Y. Tall^{1,a}, S. Cormon¹, M. Fallot¹, Y. Foucher¹, A. Guertin¹, T. Kirchner¹, L. Zanini², M. Andersson², K. Berg^{2,3}, H. Frånberg^{2,3}, F. Gröschel², E. Manfrin², W. Wagner², M. Wohlmuther², P. Everaerts³, U. Köster^{3,4}, H. Ravn³, E. Noah Messomo³, C. Jost⁵, and Y. Kojima⁶

Interestingly also significant yields of $^{204-210}$ At isotopes were observed. At isotopes are produced either by (p, π^-xn) charge exchange reactions on 209 Bi or by secondary reactions involving ³He and ⁴He. Despite the non-release of

alpha, ³He and pions. These light particles play a major role in the production of astatine isotopes [11]. The dominating direct reactions are ²⁰⁹Bi(p, π^-x n)^{210-x}At. However, for a thick target as used in this experiment, secondary reactions must be taken into account: $n->\Delta^0 -> p + \pi^-$

- 209 Bi(3 He,*x*n) ${}^{212-x}$ At induced by spallation-produced 3 He, - 209 Bi(4 He,*x*n) ${}^{213-x}$ At induced by spallation-produced 4 He.

=> Importance of first-forbidden beta decay

Shell model space

Allowed GT: vh9/2 -> π h11/2

First-forbidden: vp1/2->πd3/2 vi13/2 -> π h11/2

²⁰⁸Pb+²⁰⁸Pb deep-inelastic reaction (thick target experiment)

Gammasphere at Argonne

C9

Spokespersons: Zs. P., B. Fornal. R. Janssens

Collective octupole phonons around 208Pb



FIGURE 6.9: Angular correlations between the 2614 keV E3 transition and the 1413







²⁰⁸TI₁₂₇: proton-neutron interaction



How was ²⁰⁸Hg produced in p+Pb?

ISOLDE exp. 2014, 2016

R. Carroll et al., to be published



Fig. 1 Production yield in the ISOLDE facility of the mercury isotopes, including $^{206}{\rm Hg}$ and $^{207}{\rm Hg}.$

B. Jonson, O.B. Nielsen, J. Zylicz, CERN-81-09 (1981) (Proc. Int. Conf. Nuclei far from stability, Helsingor, Denmark. Vol.2 p.640 (1981))









Fist beams in 2015

M. Wada et al., RIKEN Accel. Prog. Rep. 47 (2014) 203

M. Wada, RIKEN

Conclusions

-recently large amount of new experimental info on neutron-rich nuclei around ²⁰⁸Pb

-along Z=82 experimental information till ²¹⁶Pb (N=134)

-along N=126 experimental info till ²⁰³Ir (Z=77)

-so far it was easy; but now more dedicated setups needed

-shell model needs to be sharpened to improve predictive power

-consistent structure and beta decay calculations needed

Shell model space



Kuo-Herling interaction

Calculations: H. Grawe

²⁰⁸Pb states



=> Good description of 208Pb (Kuo-Herling interaction)

²⁰⁷TI states

Yrast states populated in ²⁰⁸Pb+²⁰⁸Pb at Gammasphere



=> Shift of ~600 keV

Shell model: H. Grawe









²⁰⁷Pb; comparison with shell model



Slide 12

Excitation Energy (MeV)

IoP Nuclear Physics Group Conference 2014 - 9th April 2014



Increasing number of core excitations

more core-excitations \Rightarrow better theoretical description





What about low-spin core excited states in ²⁰⁷TI?



Single-proton hole states







B. Jonson, O.B. Nielsen, J. Zylicz, CERN-81-09 (1981) (Proc. Int. Conf. Nuclei far from stability, Helsingor, Denmark. Vol.2 p.640 (1981))

Beyond N=126 and Z<82: what do we know?

208Pb Core	209Pb lot	210Pb lot	211Pb lot	212Pb 8+ isomer	213Pb From beta	214Pb 8+ isomer	215Pb	216Pb 8+ isomer
207TI lot	<mark>208TI</mark> From beta/α	209TI 17/2+ isomer	210Tl From α	211TI				
206Hg Yrast till (13-)		208Hg 8+ isomer		<mark>210Hg</mark> 8+ isomer				
205Au yrast								
204Pt yrast								
203Ir yrast					Excite	ed state	S	

Production of exotic nuclei (new isotopes)





Decay (internal and β , α) spectroscopy:

- decay correlated with the fragment
- *very sensitive* (ion beams > 1 ion/hour)

Identification



192W setting

RIKEN and heavy nuclei



Figure 5.1: Particle identification plot for the isomer setting of the experiment. Nuclei of interest are circled.

Z. Patel, PhD thesis, Univ. of Surrey, 2015



FIG. 4 (color online). Systematics of $E(2^+)$ and $E(4^+ \rightarrow 2^+)$ for Sm, Gd, Dy, Er, and Yb isotopes. All data points from [26] and this work. New: 166Gd, 164Sm

Z. Patel et al., Phys. Rev. Lett. 113, 262502 (2014)

Heaviest isomer in RIKEN: ¹⁷⁴Er (Z=68)



Fig. 2. Combined $\gamma\gamma$ -coincidence spectrum gated on the decays from the 8⁻ isomer in ¹⁷⁴Er.

P.-A. Soderstrom et al., RIKEN Accel. Prog. Rep 48 (2015), in print



FIG. 5. Cross sections for production of heavy neutron-rich nuclei in collisions of ¹³⁶Xe with ²⁰⁸Pb at $E_{c.m.} = 450$ MeV. Dashed curves show the yield of primary fragments, whereas the solid ones correspond to survival nuclei. Open circles indicate unknown isotopes.

V. Zagrebaev, W. Greiner, Phys. Rev. Lett. 101, 122701 (2008)



206Hg: B. Fornal et al., PRL 87, 212501 (2001) 204Pt: S.J. Steer et al., PRC 78, 061302 (2008) 205Au: Zs. Podolyák et al, PL B 672, 116 (2009)

Transition strengths in N=126 nuclei

Nucleus	Transition	B(EL) (W.u.)			
		exp.	SM	SM_{mod}	
²⁰⁶ Hg	$B(E3:10^+ \to 7^-)$	0.25(3)	0.17	0.21	
²⁰⁴ Pt	$B(E3:10^+ \rightarrow 7^-)$	0.19(3)	0.21	0.22	
203Ir	B(E2:23/2+->19/2+)	0.02(1) ^{b)}	3.58	0.013	
²⁰⁶ Hg	$B(E3:5^+ \to 2^+)$	0.18(2)	1.17	0.91	
²⁰⁴ Pt	$B(E3:5^+ \to 2^+)$	0.039(5)	0.713	0.612	
²⁰⁶ Hg	$B(E2:10^+ \rightarrow 8^+)$	0.94(15)	0.87	0.87	
²⁰⁴ Pt	$B(E2:10^+ \rightarrow 8^+)$	0.80(8)	2.64	1.22	
²⁰⁵ Au	$B(E2:19/2^+ \to 15/2^+)$	1.2(2)	3.1	1.7	
²⁰⁴ Pt	$B(E2:7^+ \to 5^-)$	$0.017 + \rightarrow 0.0034^{a})$	1.21	0.0037	

Effective charges: 1.5e for E2 and 2.0e for E3 (to reproduce 206Hg) $^{a)}$ Assuming a transition energy between $10 \rightarrow 78$ keV.

⇒ Good description of N=126 nuclei after small modifications of TBMEs



For N=126:

Below 203lr: 238U

Above 203lr: 208Pb

FIG. 3. Production cross sections of charge-exchange N = 127 isotones (dots, this work) and N = 126 fragmentation residues (triangles, from Ref. [10]) as a function of the number of protons removed from the projectile ²⁰⁸Pb. The lines represent fragmentation cross sections of N = 127 (solid line) and N = 126 (dashed line) isotones obtained with the COFRA [30] code for reactions induced by ²³⁸U and ²⁰⁸Pb projectiles, respectively.

A.I. Morales et al., Phys. Rev. C84, 011601 (R) (2011)

Beyond N=126 and Z<82: what do we know?

208Pb Core	209Pb Yrast + ~3	210Pb Yrast + ~4	211Pb From beta	212Pb 8+ isomer	213Pb From beta
207TI Up to~35/2	208TI From beta/α	209TI 17/2+is omer	210TI g.s. (5+)	211TI	
206Hg Yrast till (13-)		208Hg 8+ isomer		210Hg 8+ isomer	
205Au yrast		-			
204Pt yrast		-			
203Ir yrast		-			



²¹⁰Hg (N=130)



A. Gottardo et al., Phys. Lett. B 725, 292 (2013)



Fig. 1 Production yield in the ISOLDE facility of the mercury isotopes, including $^{206}{\rm Hg}$ and $^{207}{\rm Hg}.$

B. Jonson, O.B. Nielsen, J. Zylicz, CERN-81-09 (1981) (Proc. Int. Conf. Nuclei far from stability, Helsingor, Denmark. Vol.2 p.640 (1981))



FIG. 1 (color online). Neutron-rich $N \sim 126$ region analyzed during the stopped beam RISING campaign. Measured half-lives are shown in color scale. Inset: Identification plots for Z as a function of A/Z at the final focal plane of the separator (left) and in the active stopper (right).

A.I. Morales et al., Phys. Rev. Lett. 113, 022702 (2014)
Production of exotic nuclei (new isotopes)



Along Z=82: neutron-rich lead isotopes



vg²_{9/2} 8⁺ isomers

Kuo-Herling interaction

Transition strength explained by considering effective three-body forces

A. Gottardo et al., Phys. Rev. Lett. 109, 162502 (2012)







²¹⁰Hg (N=130)



A. Gottardo et al., Phys. Lett. B 725, 292 (2013)



Rare RI ring at RIKEN



SlowRI project: Slow Radioactive Ions at RIKEN



M. Wada et al., Hyperfine Int. 199, 269 (2011)

Multinucleon transfer reactions: experiment

=> Theory generally very good, but ...



J.S. Barrett et al., Phys. Rev. C91, 064615 (2015)

Future: e.g. KEK Isotope Separation System (KISS)

Z, A identification, clean



Y.X. Watanabe et al., Nucl. Instrum. Meth. B 317, 752 (2013)

Impact of the first-forbidden β decay on the A~195 r-process peak



N. Nishimura, , Zs. Podolyák, D.-L. Fang, T. Suzuki, Phys. Lett. B 756 (2016) 273

Future: e.g. KEK Isotope Separation System (KISS)



¹³⁶Xe+¹⁹⁸Pt

Figure 10: Accessible region for lifetime measurement on nuclear chart using the ¹³⁶Xe beam with the intensity of 10 pnA for different extraction efficiency. The color codes indicate the calculated half lifetime by the KUTY model [9].

______ U. U. U. U. L /U

Y.X. Watanabe et al., Nucl. Instrum. Meth. B 317, 752 (2013)



⁵⁶Fe beam at E/A=500 MeV.
⁵⁴Fe secondary beam stopped.
<u>Isomeric decays</u> detected with AGATA array.

γ-ray spectroscopy at GSI



AGATA 2012-2014

AGATA+HECTOR+LYCCA

LYCCA

AGATA

Hector

AGATA Tracking array 3x2+6x3 crystals R = 12 - 22 cm $\epsilon_{Ph} = 5 - 9\%$ $\Delta E = 0.4 - 1.2\%$

AGATA demonstrator at GSI (Germany) ~20 crystals

